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Defense Policies for Partially Observed Spreading Processes on Bayesian Attack Graphs

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Motivation

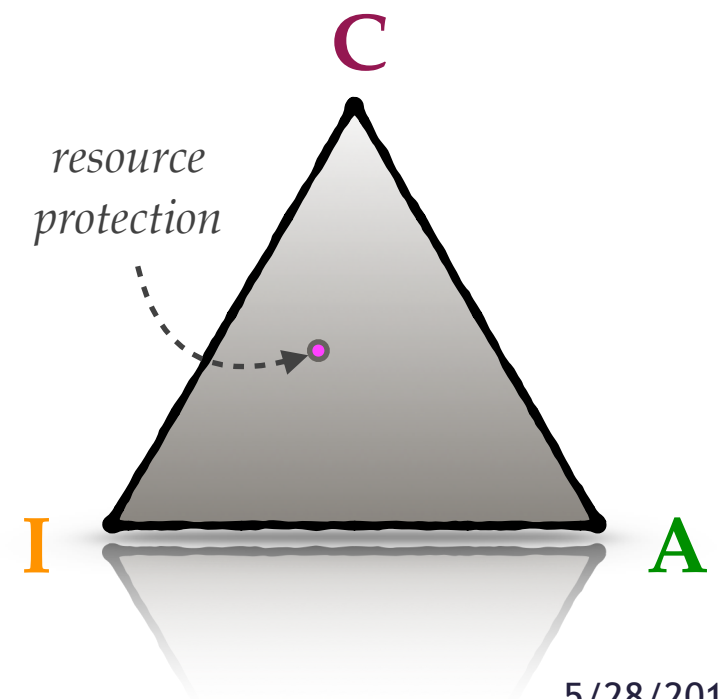
- ❖ Three key factors in *information security* problems:

Confidentiality (C) — Ensuring data does not get into the wrong hands, that is, maintaining privacy

Integrity (I) — Maintaining accuracy and trustworthiness of information

Availability (A) — Ensuring that data is always available to trusted users

- ❖ We are interested in the problem of protecting specific, important resources
 - ❖ Closely related to **confidentiality** and **integrity**
 - ❖ Need to ensure key resources are still **available** while protecting assets



The Conflict Environment

- ❖ We consider a dynamic setting where a network is continually being subjected to attacks with the objective of compromising some *target resources* through *exploits*
 - ❖ Resources that contain sensitive data
 - ❖ Resources that, when compromised, give an attacker control of a critical part of the system, potentially with catastrophic consequences
- ❖ Aspects of our model
 - ❖ *Progressive attacks* — recent exploits build upon previous exploits, progressively degrading the system
 - ❖ *Dynamic defense* — defender is choosing the best action based on *new* information
 - ❖ *Partial knowledge* — the defender only possesses a *guess* of the current exploits
- ❖ The defender can *control services* in the network to prevent the attacker from reaching the target resources

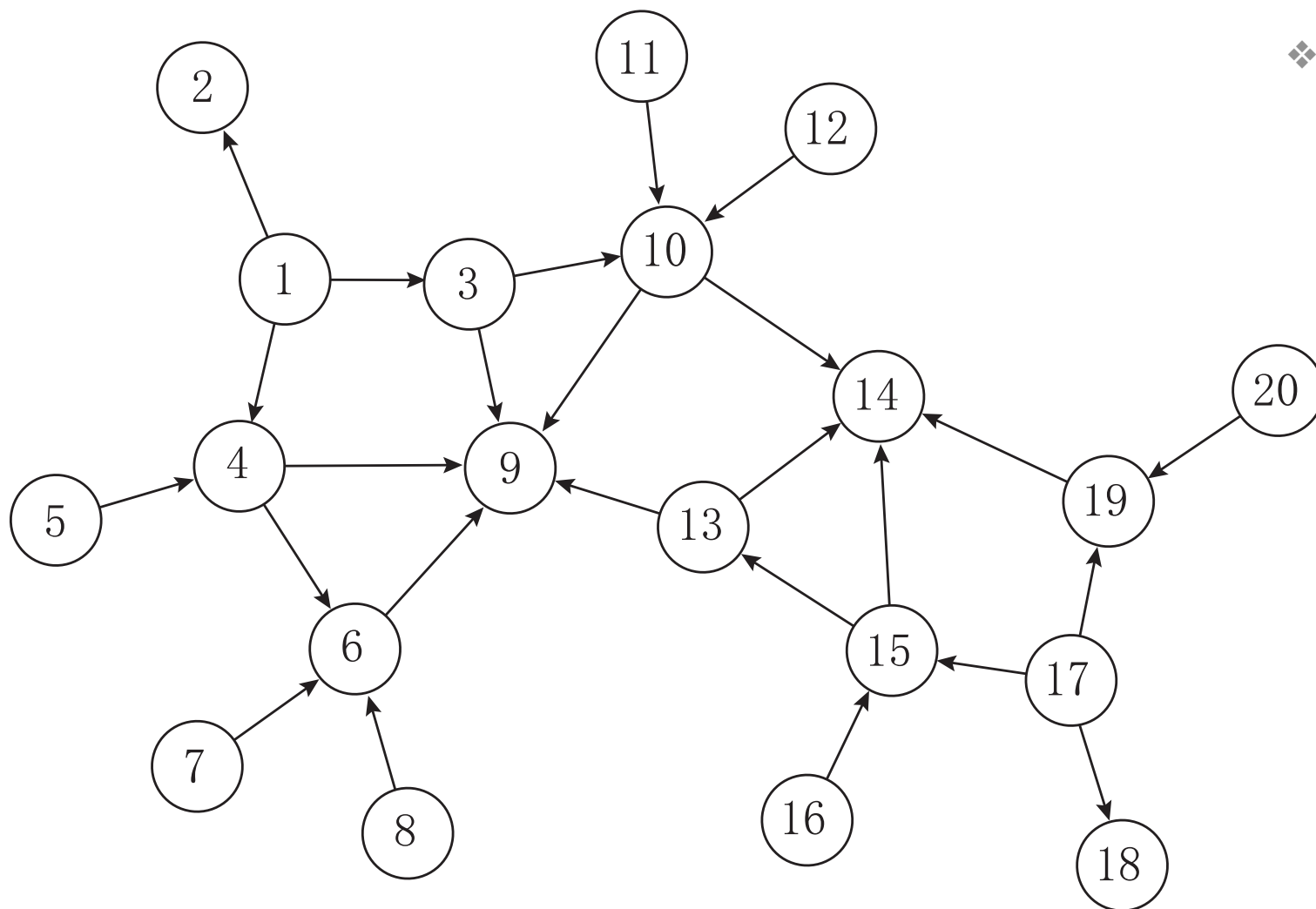
Attack Graphs

- ❖ Insufficient to look at single vulnerabilities when protecting a network
- ❖ Attackers combine vulnerabilities to penetrate the network
- ❖ *Attack graphs* model how multiple vulnerabilities can be combined and exploited by an attacker
- ❖ Explicitly takes into account *paths* that the attacker can take to reach the critical exploitation



Graph Theoretic Representation

- ❖ Consider a directed graph, denoted by $\mathcal{G} = \{\mathcal{N}, \mathcal{E}\}$



$$\mathcal{N}_R = \{1, 5, 7, 8, 11, 12, 16, 17, 20\}$$
$$\mathcal{N}_C = \{9, 14\} \subseteq \mathcal{N}_L = \{2, 9, 14, 18\}$$

- ❖ Nodes, \mathcal{N} , represent attributes
 - $\mathcal{N}_R \subseteq \mathcal{N}$: root nodes
 - ❖ No prior exploit occurred
 - ❖ Outer layer of network (exposed to world)
 - $\mathcal{N}_C \subseteq \mathcal{N}$: critical nodes
 - ❖ Deepest exploit level
 - ❖ Attacker is attempting to achieve one of the attributes
- ❖ Directed edges, \mathcal{E} , denote *exploits* (transitions between attributes)

Spreading Process

❖ The attacker's behavior is assumed to follow a *probabilistic spreading process* (i.e. **Bayesian** attack graph)

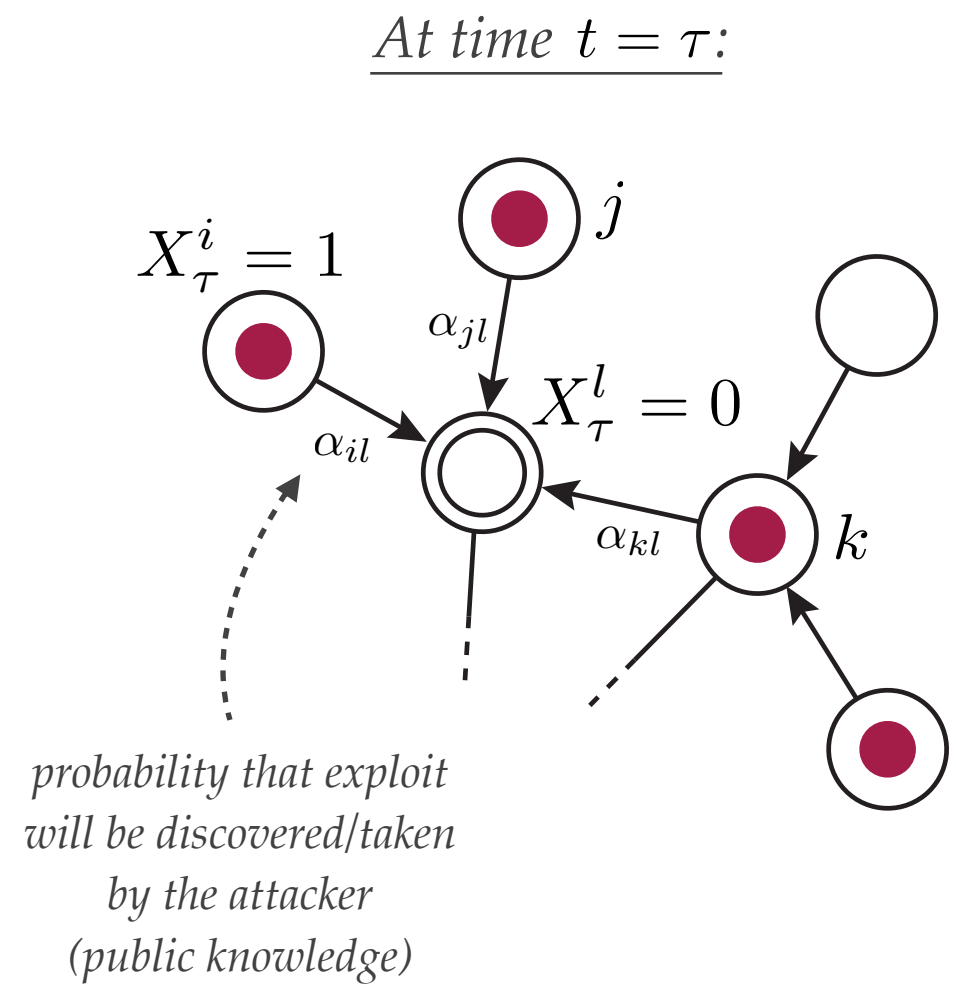
❖ Each attribute (node) i can be in one of two states

Disabled: $X_t^i = 0$ **Enabled:** $X_t^i = 1$

❖ Infection seed and spread: At each time t

A. Each root attribute is enabled with probability α_i

B. Infection spreads according to “predecessor rules”



Spreading Process – Predecessor Rules

❖ Each attribute (node) is one of two types

❖ **AND** attribute

❖ **OR** attribute

❖ The type of the attribute dictates the nature of the spreading process

❖ For **AND** attributes, e.g. node l

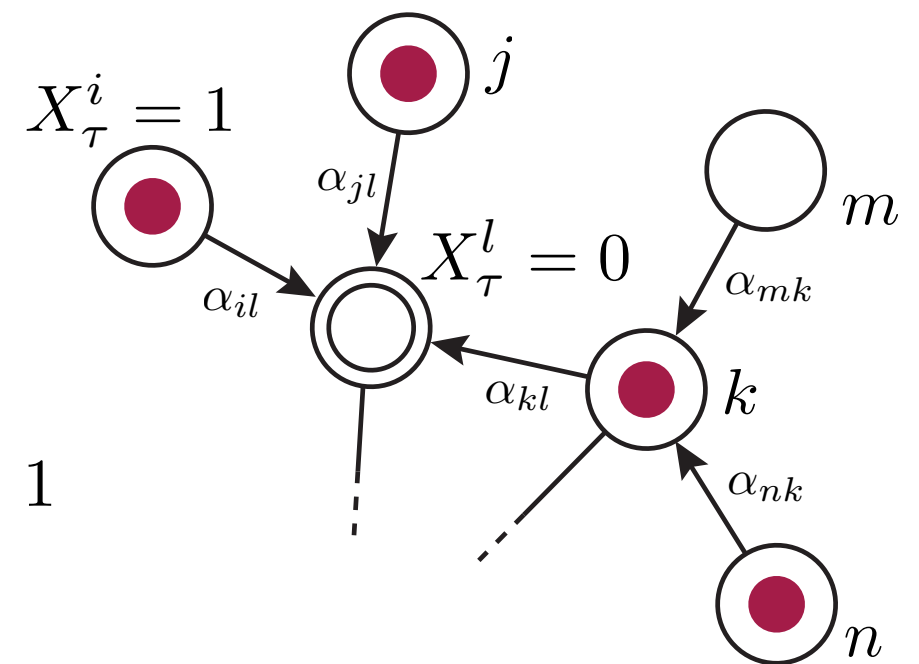
$$P(X_{t+1}^l = 1 | X_t^l = 0, X_t) = \begin{cases} \prod_{p \in \bar{\mathcal{D}}_l} \alpha_{pl} & \text{if } \bigwedge_{p \in \bar{\mathcal{D}}_l} X_t^p = 1 \\ 0 & \text{otherwise} \end{cases}$$

set of direct predecessors

❖ For **OR** attributes, e.g. node k

$$P(X_{t+1}^k = 1 | X_t^k = 0, X_t) = \begin{cases} 1 - \prod_{p \in \bar{\mathcal{D}}_k} (1 - \alpha_{pk}) & \text{if } \bigvee_{p \in \bar{\mathcal{D}}_k} X_t^p = 1 \\ 0 & \text{otherwise} \end{cases}$$

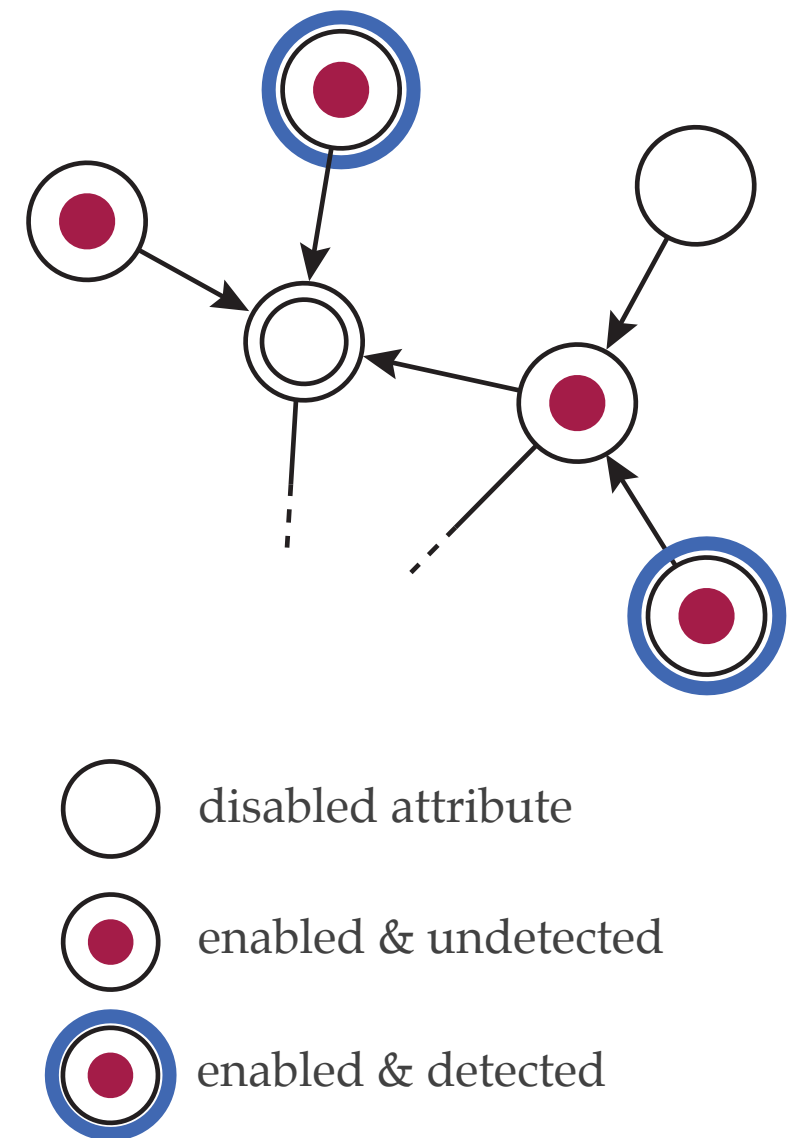
At time $t = \tau$:



Defender's Observations

- ❖ Defender only **partially observes** this process
- ❖ The *probability of detection* at node i is β_i
- ❖ **Rationale:** defender may not know the full capability of the attacker at any given time
- ❖ Defender thus observes a subset of **enabled attributes** that have been **discovered** at each time-step

$$Y_t \in \{0, 1\}^N$$



Defense Actions

- ❖ We employ a *moving target defense* scheme, termed *network hardening* to protect against exploits
- ❖ Existence of exploits depend on protocols (services)
 - ❖ Secure Shell (SSH)
 - ❖ File Transfer Protocol (FTP)
 - ❖ **Port scanning**
 - ❖ **etc.**
- ❖ Defender can thus temporarily block or disable these services to stop the attacker from progressing

Defense Actions

- ❖ Suppose there are a set of M services $\{u^1, \dots, u^M\}$
- ❖ Taking action u^m corresponds to disabling service m
 - ❖ u^m disables a subset of the attributes \mathcal{W}_{u^m}

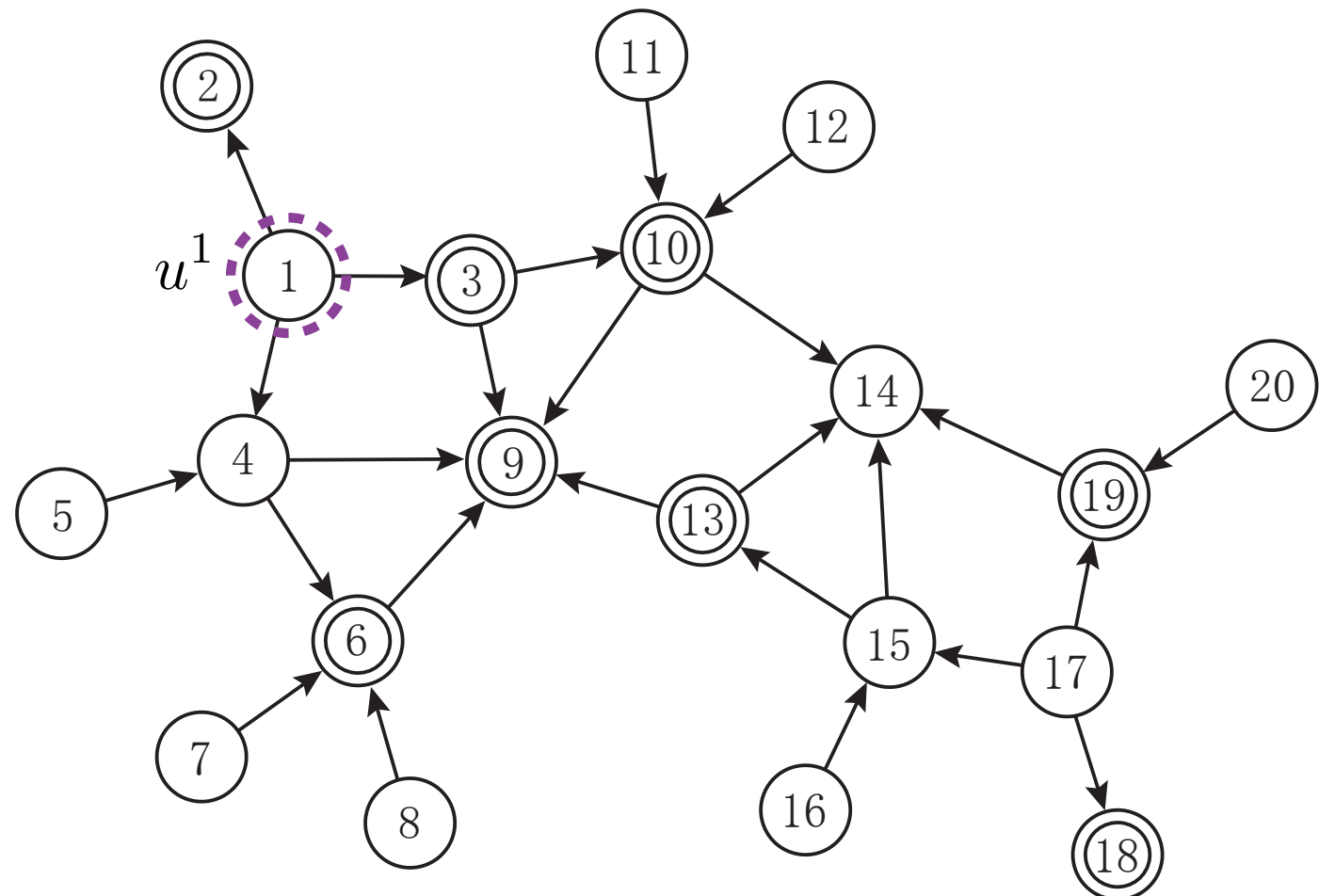
$$X^i = 0, i \in \mathcal{W}_{u^m}$$

- ❖ Action at time t

$$u_t \in \mathcal{U} = \mathcal{P}(\{u^1, \dots, u^M\})$$

$$\mathcal{W}_{u^1} = \{1\}$$

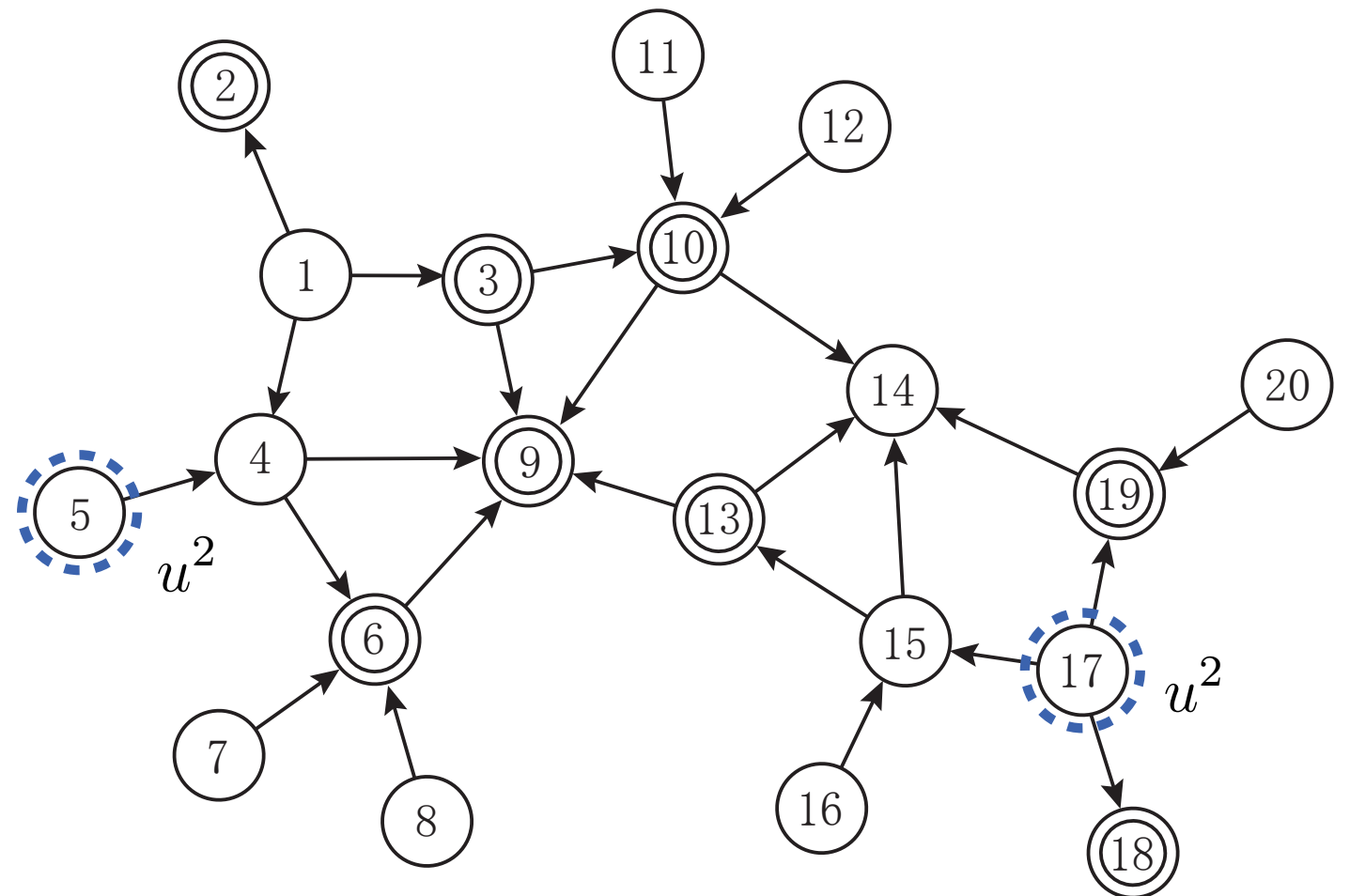
- ❖ Assume that all root attributes are covered by at least one service



Defense Actions

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$$X^i = 0, i \in \mathcal{W}_{u^m}$$



- ❖ Action at time t

$$u_t \in \mathcal{U} = \mathcal{P}(\{u^1, \dots, u^M\})$$

$$\mathcal{W}_{u^2} = \{5, 17\}$$

- ❖ Assume that all root attributes are covered by at least one service

Defense Actions

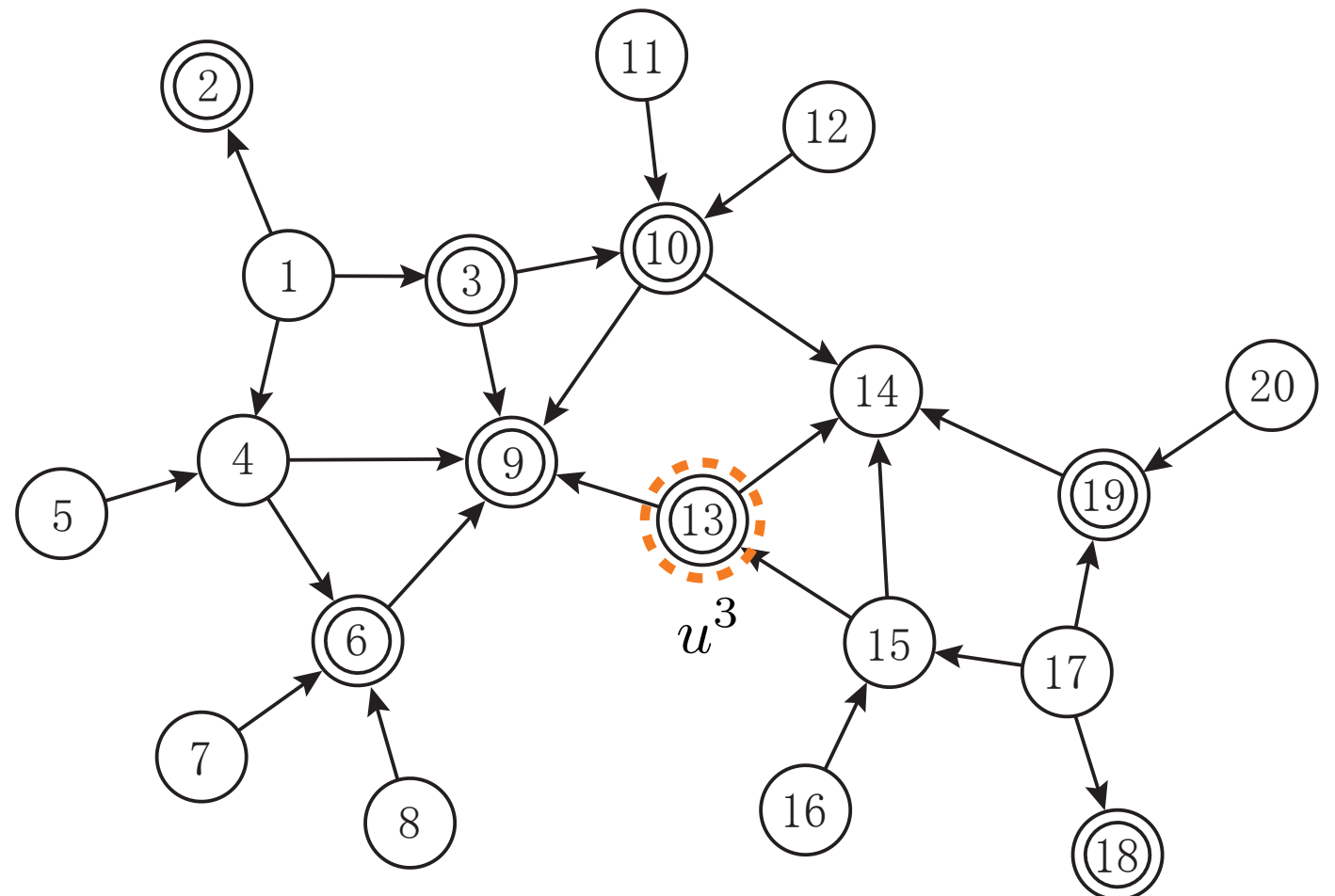
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- ❖ Action at time t

$$u_t \in \mathcal{U} = \mathcal{P}(\{u^1, \dots, u^M\})$$

- ❖ Assume that all root attributes are covered by at least one service



$$\mathcal{W}_{u^3} = \{13\}$$

Defense Actions

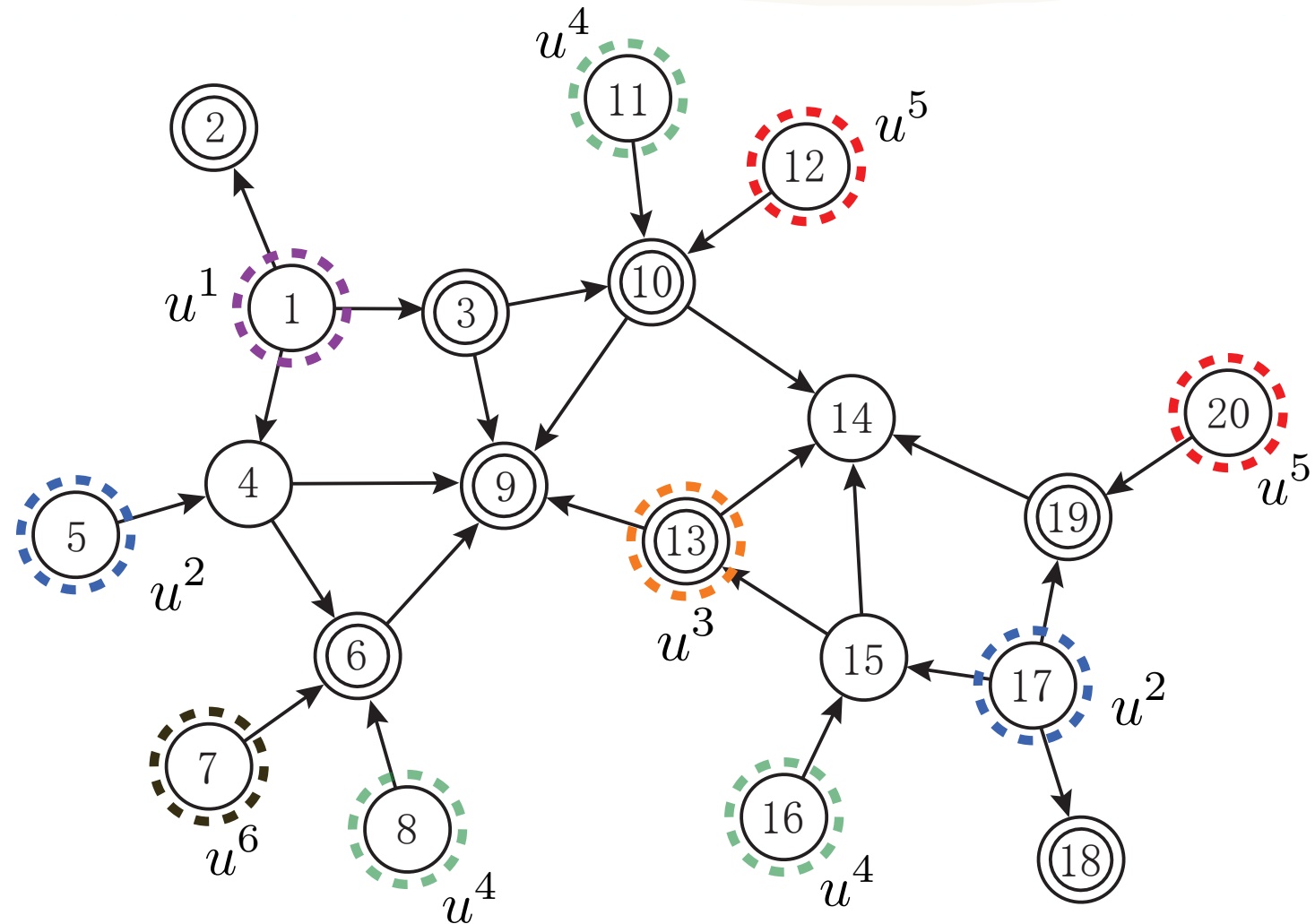
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$$X^i = 0, i \in \mathcal{W}_{u^m}$$

- ❖ Action at time t

$$u_t \in \mathcal{U} = \mathcal{P}(\{u^1, \dots, u^M\})$$

- ❖ Assume that all root attributes are covered by at least one service



Cost Function

- ❖ Cost of taking action $u \in \mathcal{U}$ in state $X \in \{0, 1\}^N$

$$C(X, u) = C(X) + D(u)$$

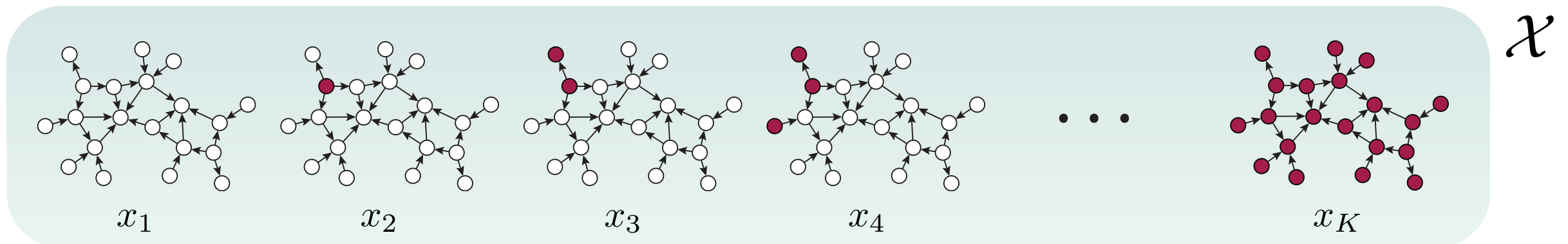
state cost   *availability cost*

- ❖ **State cost, $C(X)$:** cost of being in a particular state
- ❖ **Availability cost, $D(u)$:** cost dependent upon how many resources the defense action renders unusable (due to the disabling of the service)
- ❖ The costs capture the confidentiality, integrity, and availability factors

Defender's Information States

- ❖ Define the history up to time t as $H_t = (\pi_0, u_1, y_1, u_2, y_2, \dots, u_{t-1}, y_t)$
- ❖ We capture H_t by an *information state* $\pi_t = (\pi_t^1, \dots, \pi_t^K) \in \Delta(\mathcal{X})$

$$\pi_t^i = P(X_t = x_i | H_t)$$



- ❖ Information state obeys the update rule $\mathcal{T} : \Delta(\mathcal{X}) \times \mathcal{Y} \times \mathcal{U} \rightarrow \Delta(\mathcal{X})$

$$\pi_{t+1} = \mathcal{T}(\pi_t, y_{t+1}, u_t)$$

Defender's Optimization Problem

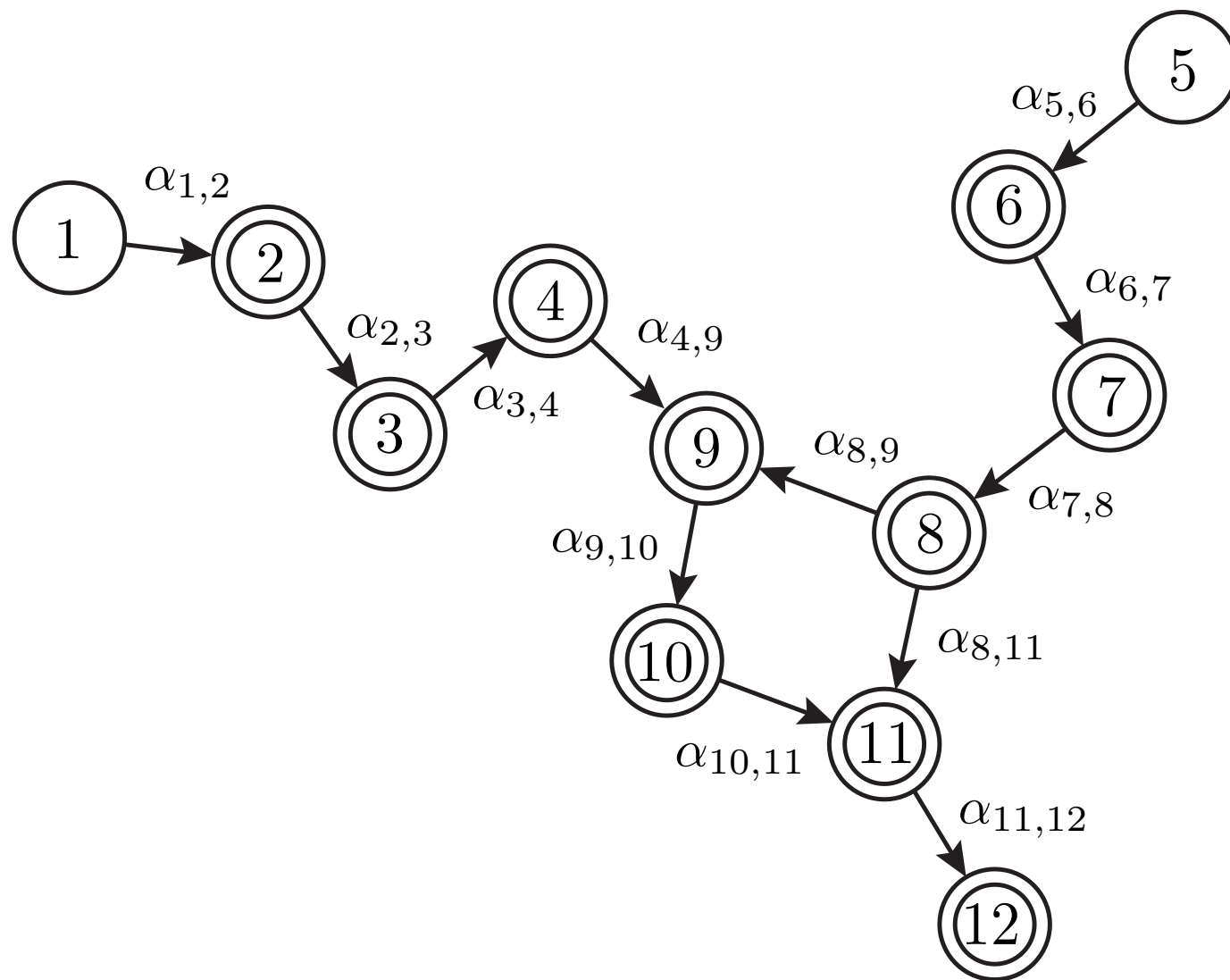
- ❖ Choose a control policy $g : \Delta(\mathcal{X}) \rightarrow \mathcal{U}$, $g \in \mathcal{G}$ that solves

$$\min_{g \in \mathcal{G}} \mathbb{E} \left\{ \sum_{t=0}^{\infty} \rho^t C(\pi_t, g(\pi_t)) \mid \pi_0 \right\}$$

subject to $u_t = g(\pi_t)$

$$\pi_{t+1} = T(\pi_t, y_{t+1}, u_t)$$

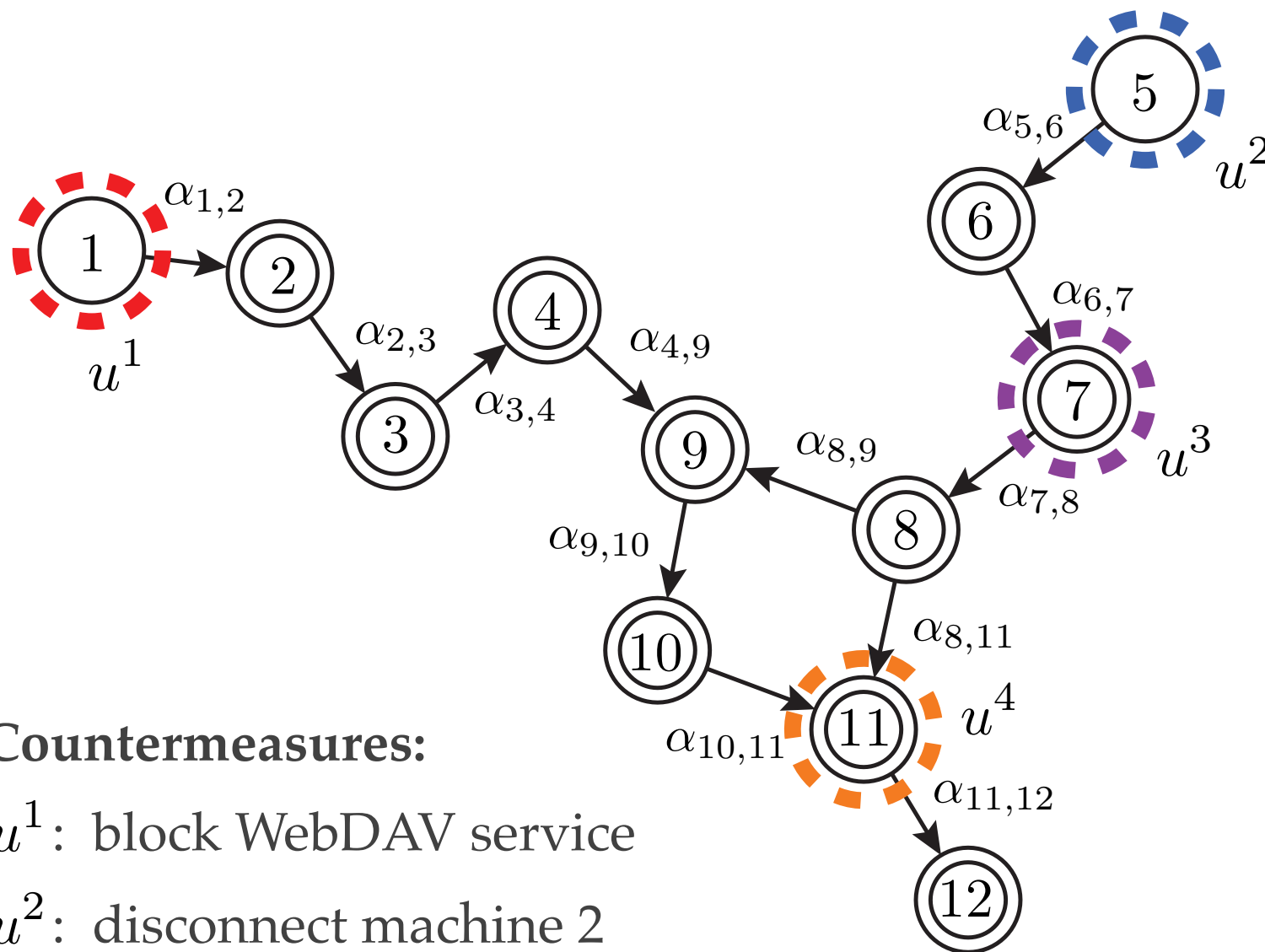
Example



Attributes:

1. Vulnerability in WebDAV on machine 1
2. User access on machine 1
3. Heap corruption SSH on machine 1
4. Root access on machine 1
5. Buffer overflow on machine 2
6. Root access on machine 2
7. Squid portscan on machine 2
8. Network topology leakage from machine 2
9. Buffer overflow on machine 3
10. Root access on machine 3
11. Buffer overflow on machine 4
12. Root access on machine 4

Example - Countermeasures



Attributes:

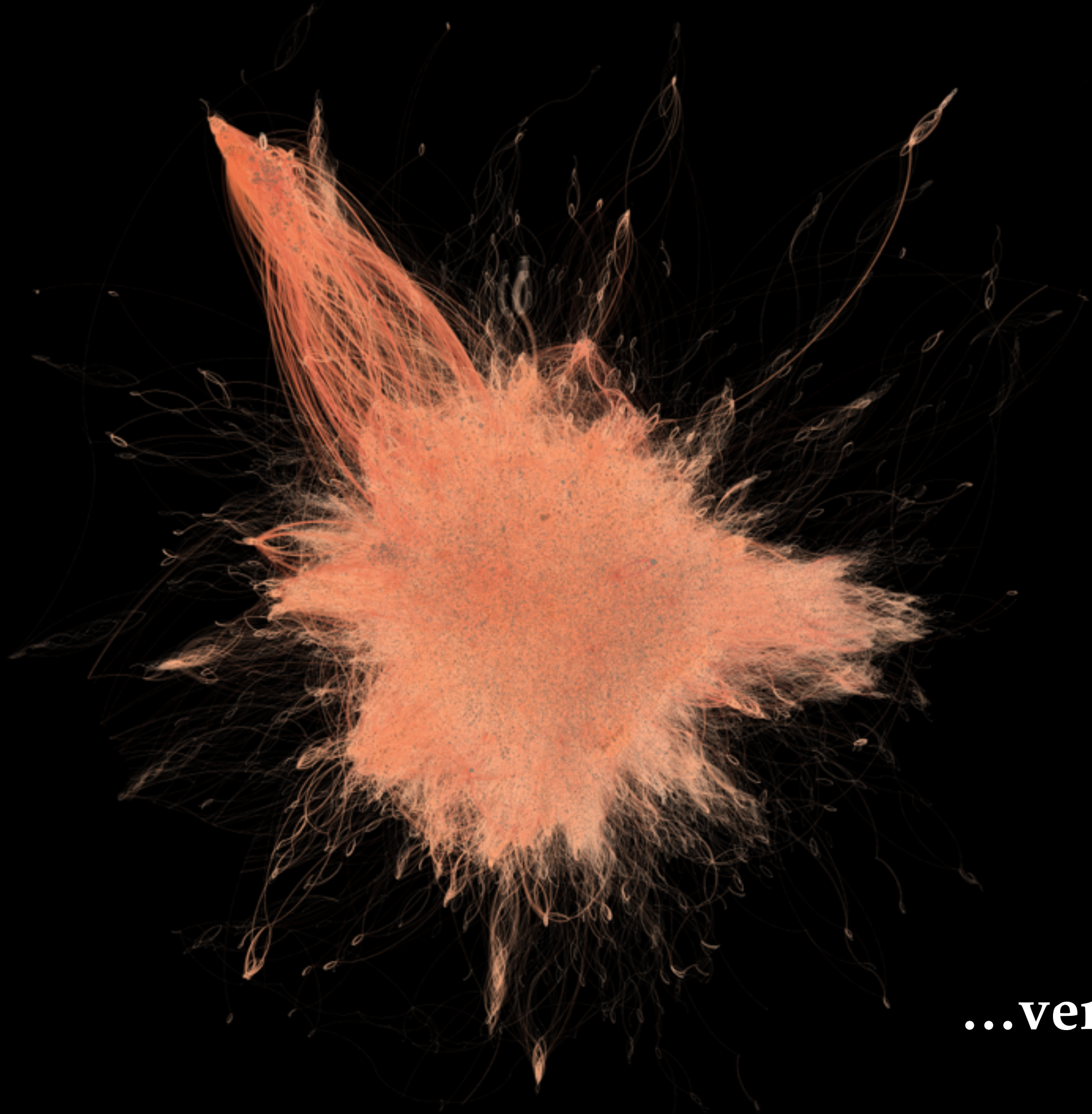
1. Vulnerability in WebDAV on machine 1
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8. Network topology leakage from machine 2
9. Buffer overflow on machine 3
10. Root access on machine 3
11. Buffer overflow on machine 4
12. Root access on machine 4

Countermeasures:

- u^1 : block WebDAV service
- u^2 : disconnect machine 2
- u^3 : block port scanning
- u^4 : disconnect machine 4

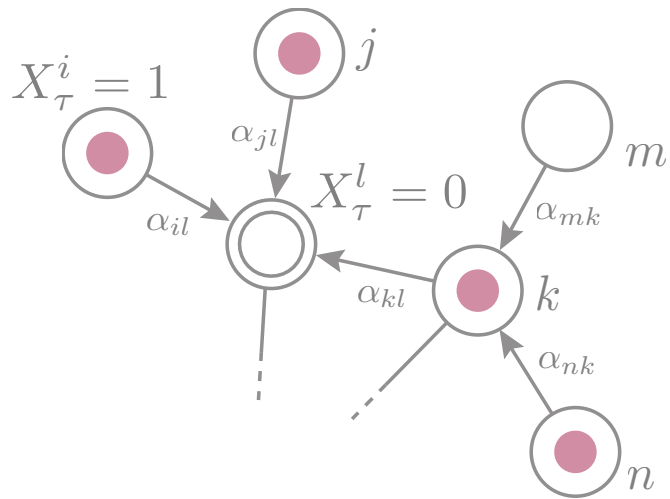
Future Work

- ❖ **Structural results**
 - ❖ Directed acyclic graphs give rise to a natural partial order
 - ❖ Can we use this to show threshold properties of the optimal policy?
 - ❖ If so, determining an approximately optimal policy would reduce to estimating these thresholds
- ❖ **Scaling the problem**
 - ❖ Exact POMDP solvers only capable of handling small examples
 - ❖ Realistic attack graphs are big...

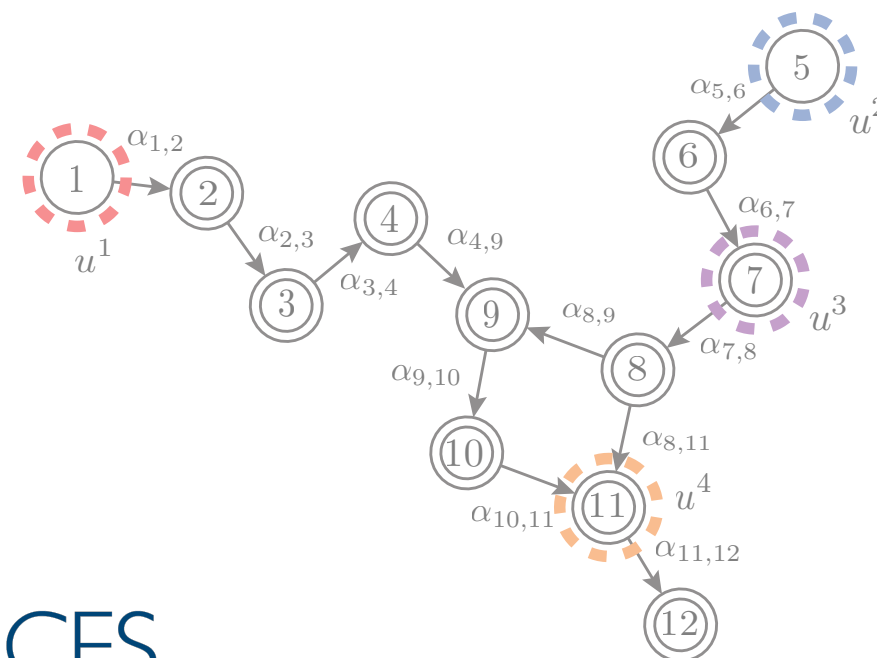
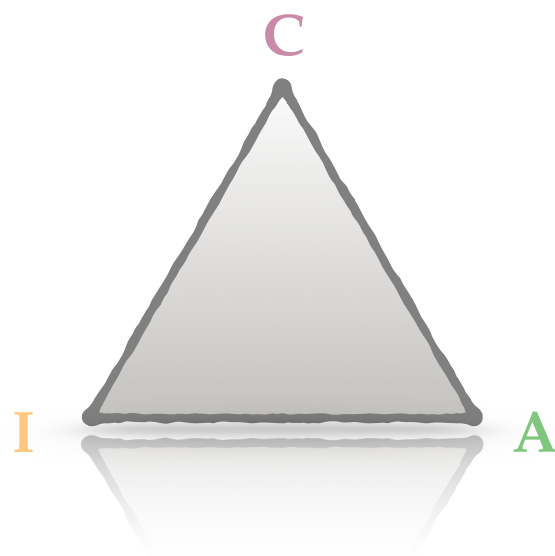


...very big.

Thank You!



Questions?



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- ❖ **NSF** — Foundations Of Resilient CybEr-physical Systems (FORCES)

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Grant: [W911NF-13-1-0421](#)

