

# Metrization, Simulation, and First–Order Approximation for Networked CPS

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#### Nonclassical dynamics in CPS

## Arises from abrupt physical and logical transitions

Nonsmooth and discontinuous transitions:

- Voltage and current limits in electrical power transmission systems.

- Topology switches and shocks in water and electrical infrastructures.

- Queue saturation in air and street traffic.
- Mode transition in supervisory control.



**Isolated transitions can be "smoothed"** (arXiv:1308.4158) enables direct generalization of classical control techniques to *hybrid* systems.



### New challenges for interconnected CPS

#### Networked CPS undergo interdependent transitions



**Combinatorial increase in complexity**  $D_0 \xrightarrow{D_0} 1$   $D_2$ Exponential number of discrete modes; factorial number of mode sequences

#### **Intrinsically nonsmooth dynamics**

In contrast to previous case, coupled dynamics cannot be "smoothed"

**New challenges require new tools** We derive techniques for stability, sensitivity, controllability, & optimality.

