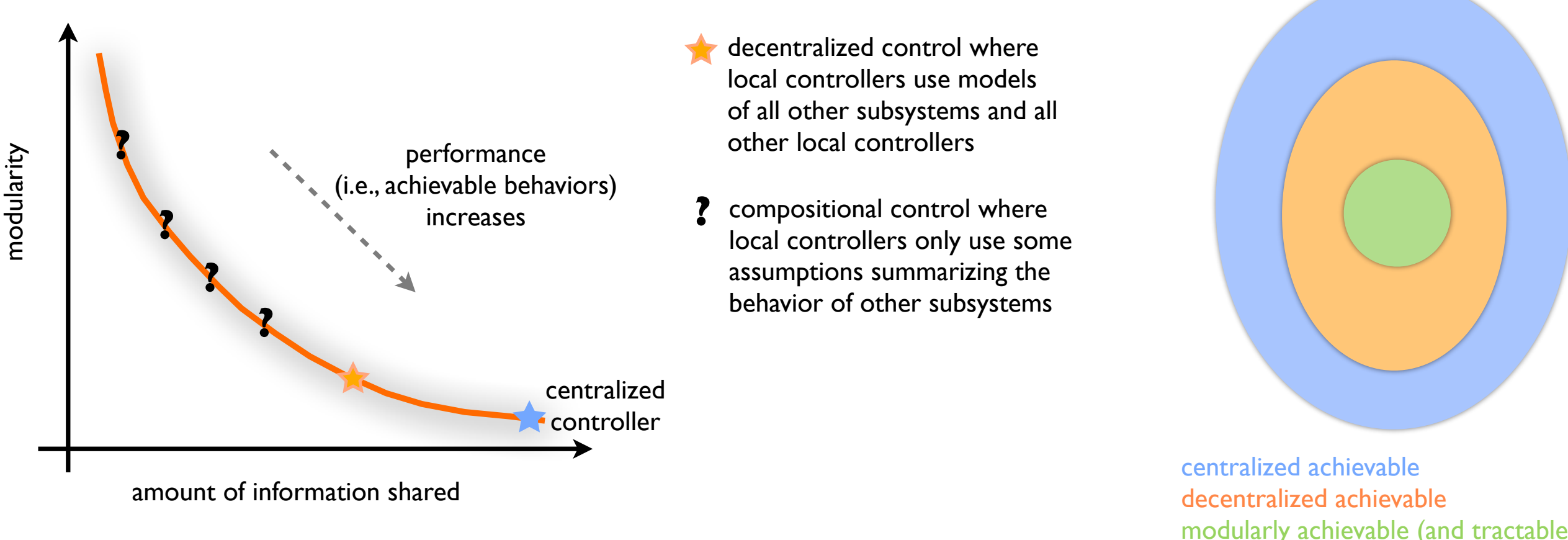


# CAREER: A Compositional Approach to Modular Cyber-Physical Control System Design

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## Overall Objective:

- Modularity to manage complexity during both design- and life-cycles for CPSs
- At the discrete-level: computing local assume-guarantee specifications per subsystem from a global specification
- At the continuous-level: decomposing a system into possibly uncertain subsystems
- Developing correct-by-construction control synthesis techniques that can handle uncertainty and partial information
- Understanding structural system properties that facilitate composition and decomposition



**Project Start Date: January 2016**

## Industry Interactions:

Toyota Research Institute, Ford, Mathworks

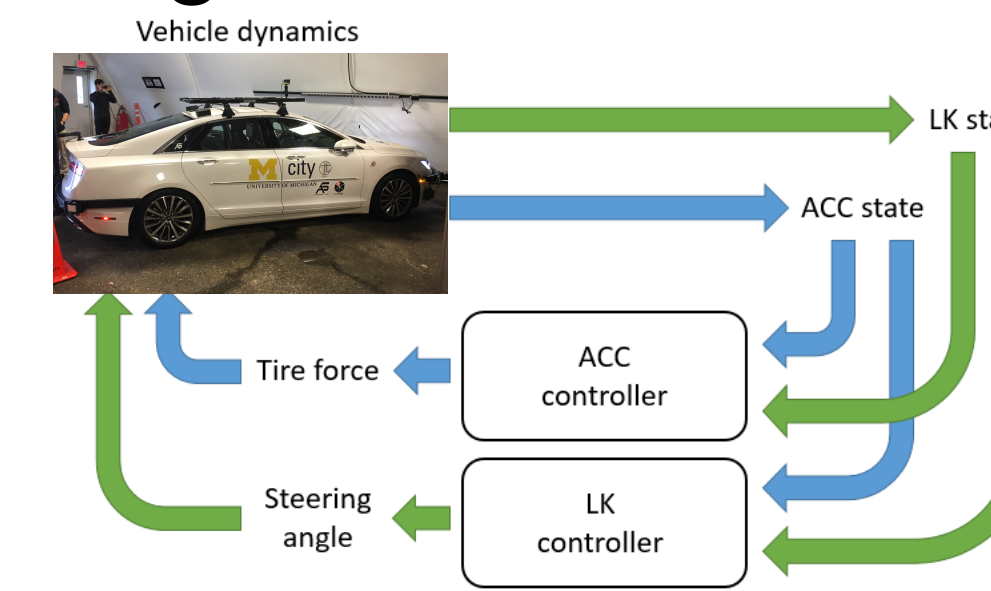
## Participants:

- Graduate Students  
Yunus E. Sahin, Petter Nilsson, Kwesi Rutledge
- Undergraduate Students  
Stanley W. Smith, Andrew Wagenmaker, Ryan Wunderly

## Results-to-date:

### Compositional Invariant Synthesis via Contracts

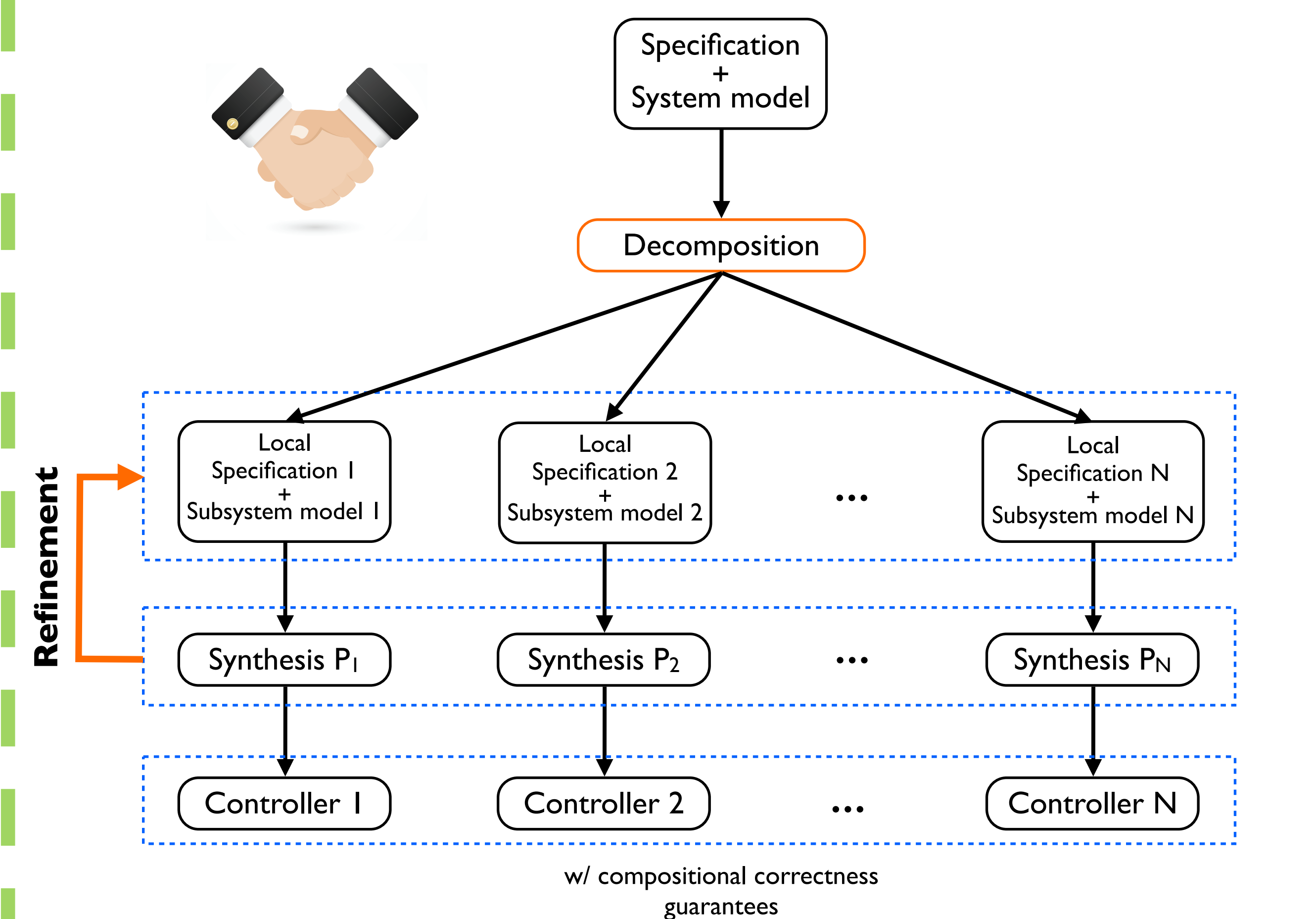
- Main idea: separately synthesize controllers for interdependent subsystems with guarantees on composition
- Interdependence quantification via convex over-approximation
- Ability to handle nonlinear terms in uncertain system dynamics exploiting monotonicity or convexity



$$\text{LK: } \frac{d}{dt} \begin{bmatrix} y \\ v \\ \Delta\Psi \\ r \end{bmatrix} = \begin{pmatrix} A_{LK,0} + A_{LK,1} \frac{1}{v} + A_{LK,2} v \end{pmatrix} \begin{bmatrix} y \\ v \\ \Delta\Psi \\ r \end{bmatrix} + B_{LK} \delta_f + E_{LK} v r_d$$

$$\text{ACC: } \frac{d}{dt} \begin{bmatrix} v \\ h \end{bmatrix} = A_{ACC}(vr) \begin{bmatrix} v \\ h \end{bmatrix}$$

- Two methods for computing separable invariant sets:
  - Iterative decoupled computation
  - LMI-based centralized computation



- Handles input and state constraints, external disturbances
- Takes advantage of disturbances that can be measured at run-time
- Handles *arbitrary information sharing patterns* (e.g., which subsystem has access to which other subsystems' states)
- Allows trading off between online vs offline computation

### Correct-by-construction Controllers in Mcity

- Setup for quick deployment
- Synthesized code is automatically integrated to Simulink (enables C code generation)
- Collaboration with Mathworks to build a bridge: same code runs with high fidelity simulators (e.g., Carsim) and on the real car with Polysync as middleware

