

CPS: CAREER: Formal Synthesis for Provably Correct Cyber-Physical Defense with Asymmetric Information

PI: Jie Fu, University of Florida

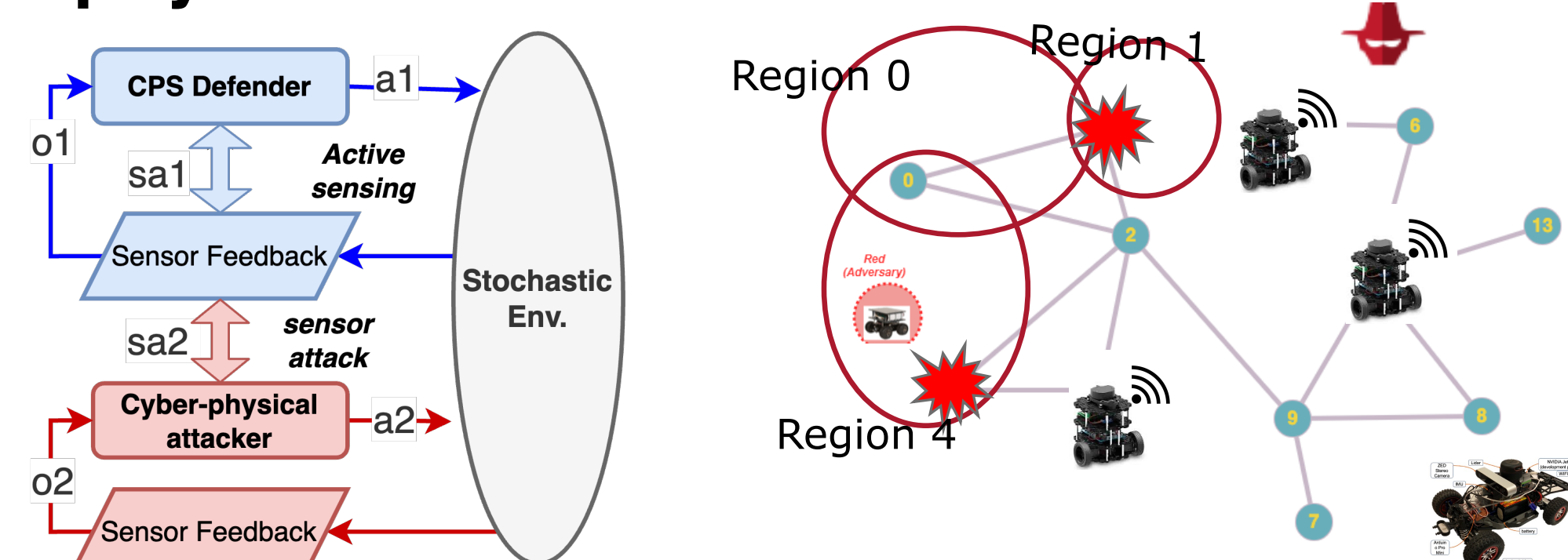


Motivation:

- **Information and knowledge** play a key role in interaction between the CPS defender and attacker.
- Need **assurance** for mission- and safety-critical CPSs.
- Possibility to use **advanced cyber defense with deception** for CPS defense.

CPS Attack-defend games on graphs:

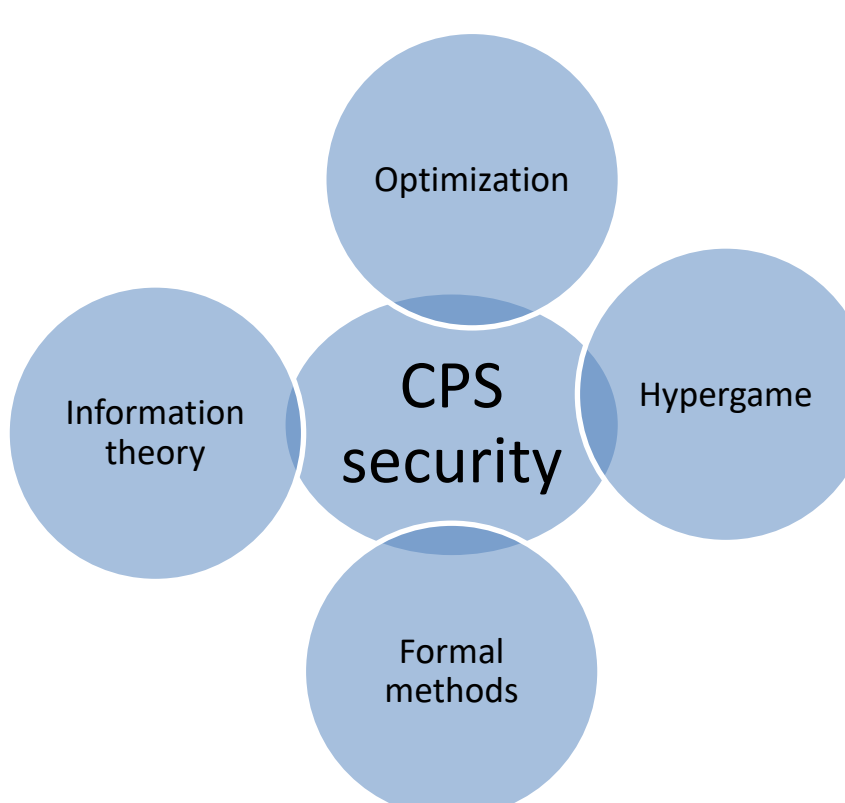
- Games on graphs with partial information $T = (S, A_1, U, A_2, P, s_0, O_1, O_2)$
- Missions in temporal logic objective.
- **Asymmetric information**: Sensor randomization, task randomization, honey sensors/robots.
- **Joint perception and control against coordinated cyber-physical attacks.**



Research thrusts:

- Thrust I: imperfect information CPS games and symbiotic defense.**
- Thrust II: Asymmetric information CPS games.**
- Thrust III: CPS games against coordinated attackers and preference-aware defense.**

Scientific Impact:



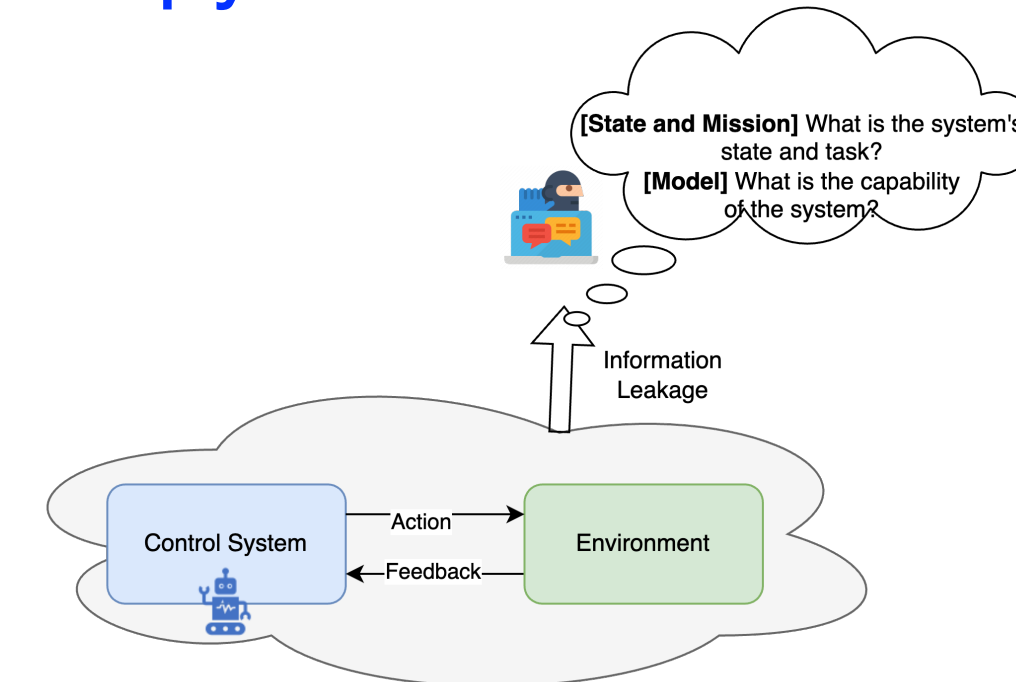
- Bi-level optimization for proactive defense game and adaptive incentive design.
- Hypergame theory for synthesizing CPS deception.
- Information-theory and formal methods for secured- and correct-by-construction.

Key innovation 1: Opacity-by-construction

Maximizing the opacity = Minimize the conditional entropy of the secret

Z: The random variable from the intruder's estimator. (current-state, initial-state, or certain events)

Y: the observations about the system.



$$\begin{aligned} & \text{maximize}_{\theta} H(Z|Y; \pi_{\theta}) \\ & \text{s.t.} : V(s_0, \pi_{\theta}) \geq \alpha. \end{aligned}$$

- Opacity in uncontrollable environments.
- Information-theoretic opacity- enforcing control

Key innovation 2: Proactive defense with deception

Defense countermeasures:

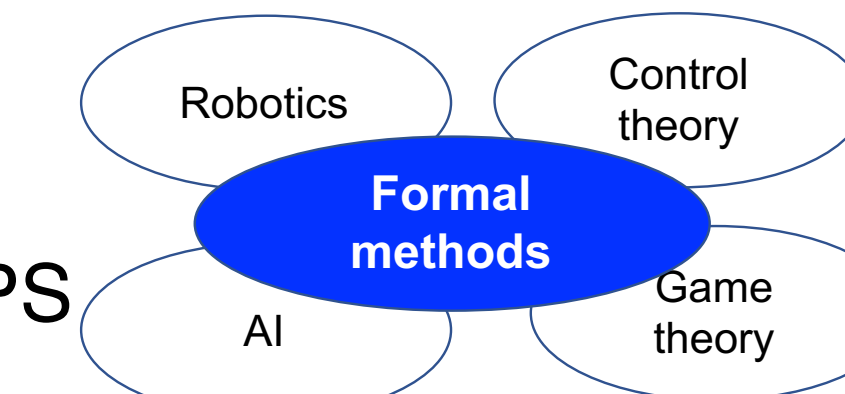
- \vec{x} : Increased attack action cost.
- \vec{y} : Decoy resource allocation (fictitious rewards)

$$\begin{aligned} M &= (S, A, P, v, \gamma, R_2). & M_2 &= (S, A, P^{\vec{y}}, v, \gamma, R_2^{\vec{x}, \vec{y}}). \\ & & & \text{Evaluating the attacker's best response for the defender's payoff} \\ & & & \max_{x,y} V_1^{\pi^*}(s_0; y) \\ & & & \text{s.t.} : \pi^* \in \arg \max_{\pi} V_2^{\pi}(s_0; x, y) \\ & & & \text{Attacker's best response to the misperceived attack graph.} \end{aligned}$$

- Defense synthesis against the best response of the attacker.
- Robust defense synthesis with uncertain attack intention.
- Adaptive defense synthesis against persistent attacks.

Broader Impacts:

- Course development:
 - Formal methods for CPS
- Enhance the security of CPS applications. Provide tools for practitioners to assess the safety and security issues.
- Project-based curriculum to train students of security practice.



References:

1. H. Ma, S. Han, C. Kamhoua, and J. Fu, "Optimal Resource Allocation for Proactive Defense with Deception in Probabilistic Attack Graphs," in *Decision and Game Theory for Security*, Springer Nature Switzerland, 2023, pp. 215–233.
2. H. Ma, S. Han, C. A. Kamhoua, and J. Fu, "Optimizing Sensor Allocation Against Attackers With Uncertain Intentions: A Worst-Case Regret Minimization Approach," *IEEE Control Systems Letters*, vol. 7, pp. 2863–2868, 2023.
3. H. Ma, S. Han, A. Hemida, C. Kamhoua, and J. Fu, "Adaptive Incentive Design for Markov Decision Processes with Unknown Rewards," presented at the *International Joint Conference on Artificial Intelligence*, Under Review 2024.
4. S. Udupa, H. Rahmani, and J. Fu, "Opacity-enforcing active perception and control against eavesdropping attacks," in *Decision and Game Theory for Security*, Avignon, France: Springer, Oct. 2023.
5. C. Shi, A. N. Kulkarni, H. Rahmani, and J. Fu, "Synthesis of Opacity-Enforcing Winning Strategies Against Colluded Opponent," in *IEEE Conference on Decision and Control*, 2023.
6. C. Shi, Y. Bu, and J. Fu, "Information-Theoretic Opacity-Enforcement in Markov Decision Processes," presented at the *International Joint Conference on Artificial Intelligence*, Under review 2024.

Asymmetric information

