

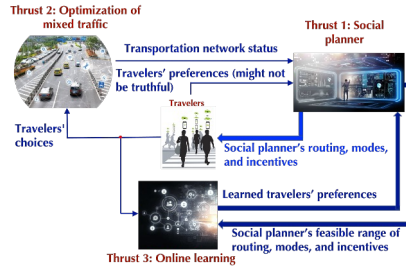
# Collaborative Research: CPS: Medium: An Online Learning Framework for Socially Emerging Mixed Mobility

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## Objective

- The overarching goal is to develop an **online framework** that will aim at well distributing vehicle flow in a mixed traffic environment, where connected and automated vehicles (CAVs) co-exist with human-driven vehicles, resulting in a **socially-optimal mobility system** that travelers would be willing to accept.
- A “socially-optimal mobility system,” is a mobility system that is efficient (in terms of energy consumption and travel time) and ensures **equity in transportation**.



## Technical Approach

### Quantification of Mobility Equity

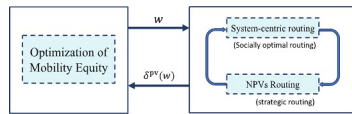
- We aim to design **mobility equity metric (MEM)** at a city-wide level that is agnostic to preferences of individuals, evaluable with publicly available data, and capable of capturing multi-modal transportation and other aspects such as accessibility, costs, and societal factors.
- Mobility index (MI)** represents mobility (or accessibility) from an origin  $i$  with respect to the different parameters from social, economic, and spatial factors, i.e., price sensitivity  $\kappa$ , user cost  $c_m$ , and accessible services  $\sigma_{i,m}^S(\tau_m)$  within a time threshold.

- Mobility equity metric (MEM)** evaluates how emerging mobility systems are equitably provided at a city-wide level using Gini index.

Mobility Metric (MEM)  
 Given MI  $\epsilon_i$  for residential node  $i \in \mathcal{O}$ , MEM is

$$MEM = 1 - \frac{\sum_{i \in \mathcal{O}} \sum_{j \in \mathcal{O}} P_i P_j |\epsilon_i - \epsilon_j|}{2(\sum_{i \in \mathcal{O}} P_i)(\sum_{i \in \mathcal{O}} P_i \epsilon_i)}$$

### Improving Mobility Equity via Routing in Mixed Mobility Systems



**Mobility Equity Maximization**  
 For a given compliance rate, we solve the following problem:  
 Maximize MEM  
 subject to:  $\delta P^*(w) \leq \gamma$

**Problem (System-Centric Routing)**

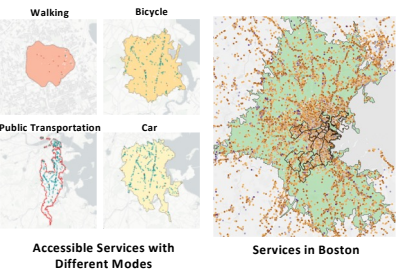
Minimize  $\sum_{i \in \mathcal{O}} \sum_{j \in \mathcal{O}} w_{ij} \left\{ \sum_{(n,j) \in \mathcal{E}} \ell^j(x^j + q^j) \cdot x_{i,n}^j \right\}$   
 subject to: (Flow constraints),  
 where  $w_{ij}$  is the weight for transportation mode  $m$ .

**Problem (Strategic Routing of  $\ell$ -Level NPV)**

Minimize  $\sum_{i \in \mathcal{O}} \sum_{(k,j) \in \mathcal{E}} \ell^j \left( x^j + \sum_{t=0}^{\ell-1} q_t^j \right) \cdot a_{i,n}^j$   
 subject to: (Flow constraints),  
 where  $a_{i,n}^j = \sum_{k \in \mathcal{N}} \theta_{k,n} \cdot a_{i,n}^j$ .

Mobility Index of Node  $i \in \mathcal{O}$

$$\epsilon_i = \sum_{m \in \mathcal{M}} e^{-\kappa c_m} \left\{ \sum_{i \in \mathcal{S}} \beta^S \sigma_{i,m}^S(\tau_m) \right\}$$

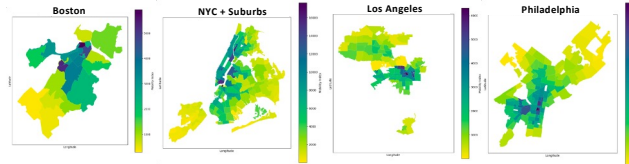


## Results

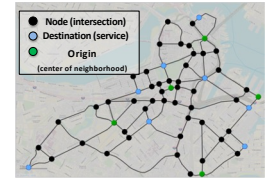
- MI tends to be better in downtown and worse in suburban areas and cities with better public transportation have higher MEM values.
- Numerical simulation shows that MEM can be improved via routing in emerging mobility systems or by having higher compliance rate.

City	MEM
Manhattan	0.881
Chicago	0.788
Boston	0.708
Philadelphia	0.643
NYC + Suburbs	0.623
LA	0.623

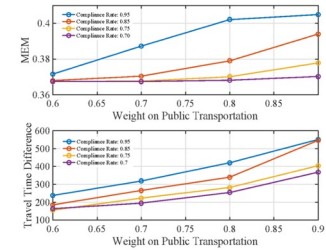
Mobility Equity Metric across Cities



Mobility Indices at Neighborhoods



Transportation Network in Boston City



Simulation Results with Different Compliance Rate

## Cooperation Compliance Control

- Incentivize noncompliant vehicles to comply with the guidance by penalizing the noncompliant behaviors. We define a global cost  $C$  to control the behavior of all users, and local cost  $C_i$  to ensure individuals being priced based on their own behavior.

Goal: Achieve Desired Compliance Probability

$$P(k) = p(q_i + C(k) + c_i(k))$$

where  $p: \mathbb{R} \rightarrow [0, 1]$  is a monotone increasing function,  $q_i$  is the agent's initial proximity of compliance.

How: Adopt Cooperation Compliance Control

$$C(k+1) = C(k) + \alpha(Q^* - \frac{1}{N} \sum_{i=1}^N M_i(k))$$

$$c_i(k+1) = c_i(k) + \beta(Q^* - M_i(k))$$

## Online Preference Learning

- Devise expert with clustering algorithm

Algorithm 1 Expert With Cluster

Require: Number of clusters  $K$ , offline training data  $\mathcal{D}$ , learning rate  $\eta$

Train with data  $\mathcal{D}$ , receive  $\{\theta_i\}_{i \in [N]}$

Apply clustering on  $\{\theta_i\}_{i \in [N]}$ , receive centroids  $\{c_k\}_{k \in [K]}$

Initialize weight  $p_{i,1}(k) \leftarrow \frac{1}{K}$  for all  $i \in [N]$ ,  $k \in [K]$

for  $\ell = 1, \dots, T$  do

  for  $i = 1, \dots, N$  do

    Receive  $x_{i,t}$

    Sample  $E_{i,t} \sim p_{i,t}$ , submit  $Rec_{i,t} = \hat{y}(C_{R_{i,t}}, x_{i,t})$ .

    Receive  $y_{i,t}$ , compute loss  $L_{i,t}(k) = l(\hat{y}(c_k, x_{i,t}), y_{i,t})$  for all  $k \in [K]$

$p_{i,t+1}(k) \leftarrow \frac{p_{i,t}(k)e^{-\eta L_{i,t}(k)}}{\sum_{k' \in [K]} p_{i,t}(k')e^{-\eta L_{i,t}(k')}}$  for all  $k \in [K]$

  end for

end for

## Scientific Impact

- Merging learning and control approaches for CPS and bridging the gap between optimal planning and safe-critical control in CPS.
- Develop a framework addressing societal challenges within CPS.

## Broader Impact

- Develop a new **mobility equity metric** and equity-prioritized control framework for emerging mobility systems.
- Develop a holistic and rigorous framework to capture the **societal impact** of CAVs and provide solutions that enhance accessibility, safety, and equity in transportation.

## References

- Bang, H., Dave, A., and Malikopoulos, A.A., "Routing in Mixed Transportation Systems for Mobility Equity," Proc. of 2024 American Control Conference, 2024 (to appear).
- Chremos, I.V. and Malikopoulos, A.A., "A Traveler-centric Mobility Game: Efficiency and Stability Under Rationality and Prospect Theory," PLoS ONE, 18 (5), 2023.
- Chremos, I.V., and Malikopoulos, A.A., "Mobility Equity and Economic Sustainability Using Game Theory," Proc. of 2023 American Control Conference, pp. 1698-1703, 2023.
- Jayawardana, V., Tang, C., Li, S., Suo, D., and Wu, C., "The Impact of Task Underspecification in Evaluating Deep Reinforcement Learning," Advances in Neural Information Processing Systems, pp. 23881-23893, 2022.
- Li, S., Dong, R., and Wu, C., "Stabilization Guarantees of Human-Compatible Control via Lyapunov Analysis," European Control Conference, pp. 1-8, 2023.
- Qu, A., Valiveru, A., Tang, C., Jayawardana, V., Freydt, B., and Wu, C., "What is a Typical Signalized Intersection in a City? A Pipeline for Intersection Data Imputation from OpenStreetMap," Transportation Research Board Annual Meeting, 2023.
- Hamdipoor, V., Meskin, N., and Cassandras, C.G., "Safe Merging Control in Mixed Vehicular Traffic," Proc. of 2023 American Control Conference, pp. 4386-4392, 2023.
- Xiu, K., and Cassandras, C.G., "Scaling up the Optimal Safe Control of Connected and Automated Vehicles to a Traffic Network: A Hierarchical Framework of Modular Control Zones," Proc. of 2023 IEEE Intl. Intelligent Transportation Systems Conf., 2023.
- Li, A., Chavez Arrijos, A., and Cassandras, C.G., "Cooperative Lane Changing in Mixed Traffic can be Robust to Human Driver Behavior," Proc. of 62nd IEEE Conference on Decision and Control, 2023.