Hybrid Systems Laborator

Constraint Aware Planning and Control for Cyber-Physical Systems Pls: Ricardo Sanfelice (UC Santa Cruz, Lead) and Shai Revzen (University of Michigan)

Overview

Challenge:

Enable robust, adaptive planning & control for nonlinear, nonsmooth, & constrained systems, while respecting their physical constraints and meeting specifications.

Significance:

The need for this project arises from the difficulty of combining planning, safety, and robustness in the control of physical systems in general and hybrid cyber-physical systems in particular.

Technical Approach

Thrust 1: From Specifications and Physics to Geometric Planning Informed by Constraints

Approach: Classical control focuses on physics based models, robustified against noise and modeling error using feedback. We enrich the tools available with: 1) hard constraints defined via a pullback from relevant output spaces; 2) soft constraints defined through the manipulation of the Riemannian pseudometric of the state-space; 3) learned constraints, defined in data-driven from using examples of desirable behaviors. The hard and soft constraints together can be used to solve for an actuation policy at high speeds, while still maintaining the semantic origins of each constraint, and informing the response to its violation

Thrust 2: Robust and Adaptive Constraint Satisfaction

Approach: Using the constraints determined from physics and specifications in Thrust 1, we will develop notions and tools to assure robust and adaptive satisfaction of those constraints.

We will investigate the following notions of robust safety:

- An "always robust" constraint satisfaction notion that preserves the satisfaction of the constraints in the presence of sufficiently small disturbances.
- An "approximate robust" notion guaranteeing that constraint satisfaction degrades gracefully.
- A "selective robust" notion.

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Intellectual merit

• Mathematical framework to rigorously formulate learning-based planning and control for CPS with awareness of its constraints. • Novel architectures that lead to robust adaptive constraint satisfaction.







Results Safety with Multiple Constraints [3] *Goal:* Design a switched reference governor framework to **Data Driven Constraints For Recovery From Damage** achieve high performance tracking under constraints. We designed a switched reference governor (RG) algorithm *Goal:* Demonstrate the utility of learning implicit constraints 1 and Thrust 2 to build a framework for robust and to achieve rapid and non-oscillatory convergence to a given from an example behavior, and using those constraints to reference signal while satisfying the imposed constraints by recover the behavior quickly once the robot suffers damage. switching between a fast controller and a non-oscillatory controller. We showed robust switching, recursive feasibility **Constraint Aware Motion Planning and Control** Specifications + additional data and convergence of the virtual reference to the reference Robust constraint (initial motion plan, Bumped trajectory -- Grid signal, among other key properties. Robot constraints, etc.) Bumped trajectory Reference traiector Bump location (s0) Bump radius=[3.5 Switch q RG Switched RO **Control of multi-contact slipping** [2] *Goal:* Collaborate with industry to extend multi-legged robot control and safety into domains where multiple legs slip on the ground. The "SpiderBot" platform is an 18 DOF hexapod with an on-We built a robot with 6DoF board PixyCam for tracking colored beacons. The robot is also force-torque sensors on each equipped with motion tracking markers allowing its true worldleg and developed a novel frame configuration to be recorded in real-time. calibration method to allow us to validate our method for We are currently exploring a biologically inspired method to modeling multi-legged slip. search the space of trajectories when recovering from damage using the approach explored in previous reporting periods. This We also applied this method to data method diffeomeophically deforms the space around the robot obtain under this grant from Ghost while leaving the robot kinematic model intact. Because the Robotics, consisting of robot slipping deformation is not related to robot's complexity, it can easily data and point cloud information. scale to 18 DOF or even much higher dimensions. Initially, we will test our ideas regarding rapid **Selected Products** [1] G. Council, S. Revzen "Recovery of Behaviors Encoded via Bilateral Constraints", arXiv:2005.00506, September 2022. [2] Z. Wu, D. Zhao, and S. Revzen "Modeling multi-legged robot locomotion with slipping and its experimental validation" (in review IJRR; arXiv:2310.20669 (2023)) [3] N. Wang, S. D. Cairano and R. G. Sanfelice "A Switched Reference Governor for High Performance Trajectory Tracking", to appear in American Control Conference, 2024. [4] N. Wang and R. G. Sanfelice "HySST: An Asymptotically Near-Optimal Motion Planning Algorithm for Hybrid Systems", IEEE Conference on Decision and Control, 2023. **Broader impacts** • Deep understanding of roles and priorities of system



Thrust 3: A Framework for Dynamic Constraint Aware Planning and Control Approach: We bring together the results from Thrust adaptive planning and control with awareness of the physical and specification constraints. This framework implements algorithms that make the decision of which constraints to use at each time while guaranteeing their robust satisfaction with adaptation to disturbances. These algorithms will be essentially ready-made for constrained motion planning. **Thrust 4: Evaluation/Experimentation Plan** Approach: We will test the effectiveness of our control methods with several legged robotic platforms: an 18-DOF kinematic hexapod robot (SpiderBot, see right), a 10-DOF dynamically running hexapod robot with ground contact detection, and a commercial ``dog-like'' dynamic quadruped with 12-DOF actuation. recovery from damage using the slowly moving SpiderBot. We will test the feasibility of quickly updating constraint lists using the ground-contact detecting hexapod, and apply the principles we learnt to larger Ghost Robotics Spirit robot.

- constraints in CPS. • Tools and design techniques that permit engineers to deploy constraint aware algorithms.
- transportation.



Solutions:

- Generate a framework for the design of algorithms that self-adapt to jointly plan the motion and control the CPS, with robustness.
- Design algorithms that self-learn and selfadapt in real time to cope with unexpected changes in the physics and in the specification to enable autonomous systems to perform tasks robustly and safely.
- Formulate tools that reason about specifications and physics as verticallyintegrated modular and reconfigurable constraints.





Motion Planning for Hybrid Dynamical Systems [4] *Goal:* Design a sampling-based motion planning algorithm for hybrid systems with optimality guarantee.

We formulated the optimal motion planning problems for hybrid systems where the hybrid systems and the cost function can be formulated as follows:

$$\mathcal{H}: \left\{ \begin{array}{ll} \dot{x} = f(x, u) & (x, u) \in C \\ x^+ = g(x, u) & (x, u) \in D \end{array} \right\} \stackrel{c(\phi) := \left(\sum_{j=0}^J \int_{t_j}^{t_{j+1}} L_C(\phi(t, j)) dt\right)$$

We proposed a stable sparse rapidly-exploring random trees (SST) algorithm, called HySST, to solve optimal motion planning problem for hybrid systems with proven asymptotically near-optimality.

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We applied the HySST algorithm in a collision-resilient aerial vehicle system and showed its capacity of utilizing the collision with the walls to decrease the cost.



Educational and Outreach Impacts:

- Collaboration with colleagues at the University of Bologna.
- Outreach to high school students through Summer outreach and STEM mentoring.
- Publishing of teacher resources online and offering of teacher training

• Broad application of the results to CPS that require planning and control, especially autonomous systems in air and ground

• Benefit to industry developing multi-legged robotic systems and solutions for real-time planning & control under dynamic obstacles.













