



Responsive Load Control

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- ▶ The electrical power drawn by plug-in electric vehicle (PEV) chargers will (eventually?) begin to impact the grid.
- ▶ At the system-wide level, control objectives tend to focus on filling the overnight valley in background demand.
- ▶ At the distribution level, proposed control strategies address:
 - ▶ Transformer overloads
 - ▶ Loss minimization
 - ▶ Voltage degradation
 - ▶ Tap-change minimization
- ▶ Few control strategies also take into account the effects of charging on battery health.

Goals

- ▶ A decentralized approach to scheduling PEV charging that considers trade-offs between:
 - ▶ Energy price
 - ▶ Battery degradation
 - ▶ Distribution network effects
- ▶ The resulting collection of PEV charging strategies should be efficient (socially optimal).
- ▶ Convergence should only require a few iterations.

- ▶ PEV population: $\mathcal{N} \equiv \{1, \dots, N\}$.
- ▶ Horizon: $\mathcal{T} \equiv \{0, \dots, T - 1\}$.
- ▶ Admissible charging strategies:

$$u_{nt} \geq 0, \quad t \in \mathcal{T}$$
$$\|\mathbf{u}_n\|_1 \equiv \sum_{t \in \mathcal{T}} u_{nt} \leq \Gamma_n$$

where Γ_n is the energy capacity of the n -th PEV.

- ▶ The set of admissible charging controls is denoted \mathcal{U}_n .

Demand charge

- ▶ Distribution-level impacts are largely a consequence of coincident high charger power demand u_{nt} .
- ▶ Undesirable effects can be minimized by encouraging lower power levels,

$$Cost_{demand,nt} = g_{demand,nt}(u_{nt})$$

where $g_{demand,nt}(\cdot)$ is a strictly increasing function.

Battery degradation cost

Experimentation with LiFePO_4 lithium-ion batteries gave a degradation model:

$$\partial_{\text{cell}}(I, V) = \beta_1 + \beta_2 I + \beta_3 V + \beta_4 I^2 + \beta_5 V^2 + \beta_6 IV + \beta_7 V^3$$

relating energy capacity loss per second (in $\text{Amp} \times \text{Hour} \times \text{Sec}^{-1}$) to charging current I and voltage V .

- ▶ Degradation cost:

$$g_{\text{cell}}(I, V) = P_{\text{cell}} \Delta TV \partial_{\text{cell}}(I, V)$$

where P_{cell} is the price (\$/Wh) of battery cell capacity.

- ▶ Over the useable state of charge (SoC) range, $V \approx V_{\text{nom}}$.
- ▶ Battery degradation cost can be expressed as:

$$\begin{aligned} \text{Cost}_{\text{degrad},nt} &= g_{\text{cell},n}(u_{nt}) = M_n g_{\text{cell}}\left(\frac{10^3 u_{nt}}{M_n V_{\text{nom}}}, V_{\text{nom}}\right) \\ &= a_n u_{nt}^2 + b_n u_{nt} + c_n \end{aligned}$$

System cost:

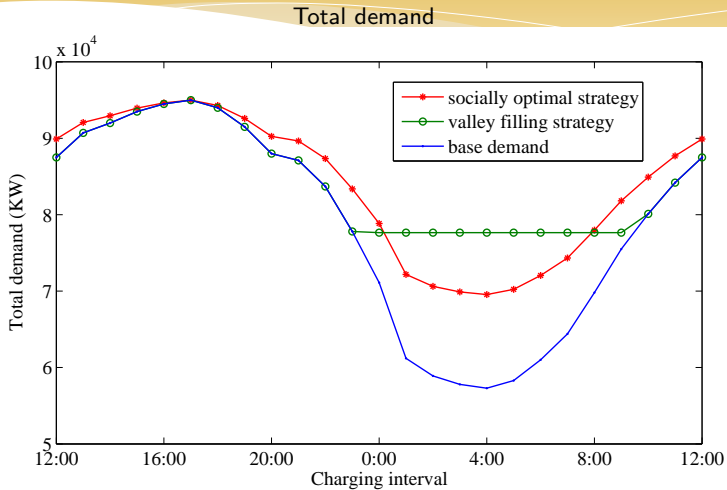
$$J(\mathbf{u}) \triangleq \sum_{t \in \mathcal{T}} \left\{ c \left(d_t + \sum_{n \in \mathcal{N}} u_{nt} \right) + \sum_{n \in \mathcal{N}} g_{nt}(u_{nt}) \right\} - \sum_{n \in \mathcal{N}} \left\{ h_n(\|\mathbf{u}_n\|_1) \right\}$$

where:

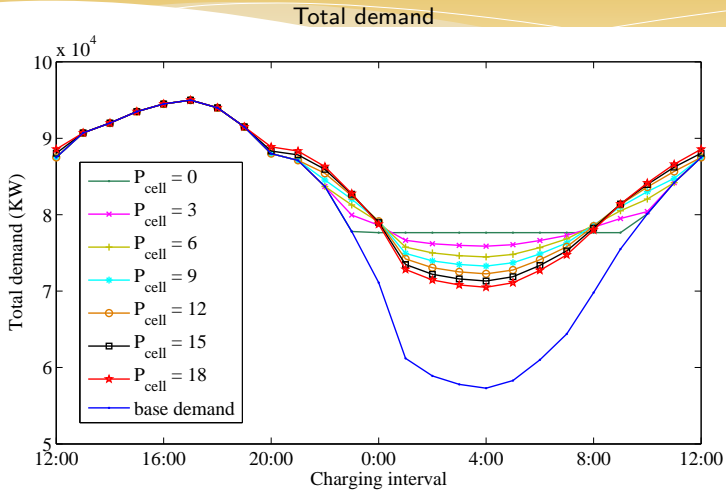
- ▶ $\mathbf{u}_n \in \mathcal{U}_n$ for all $n \in \mathcal{N}$.
- ▶ $c(\cdot)$ gives the generation cost with respect to the total demand $d_t + \sum_{n \in \mathcal{N}} u_{nt}$, and d_t denotes the aggregate inelastic base demand at time t .
- ▶ $g_{nt}(u_{nt}) = g_{demand,nt}(u_{nt}) + g_{cell,n}(u_{nt})$ captures the demand charge and battery degradation cost of the n -th PEV.
- ▶ $h_n(\|\mathbf{u}_n\|_1)$ denotes the benefit function of the n -th PEV with respect to the total energy delivered over the charging horizon, with:

$$h_n(\|\mathbf{u}_n\|_1) = -\delta_n(\|\mathbf{u}_n\|_1 - \Gamma_n)^2$$

Example

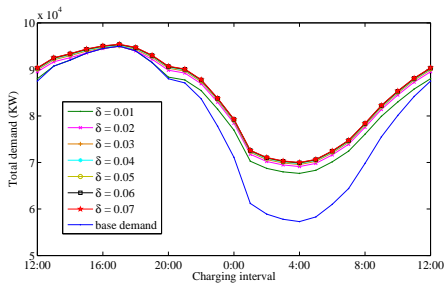


Example - varying P_{cell}

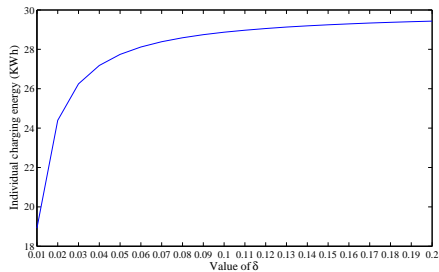


Example - varying terminal penalty, δ_n

Total demand



Delivered energy



Decentralized charging coordination

- (S1) Each PEV autonomously determines its optimal charging strategy with respect to a given electricity price profile $\mathbf{p} \equiv (p_t, t \in \mathcal{T})$. This optimal strategy takes into account the trade-off between the electricity cost and local (demand and battery degradation) costs over the entire charging horizon.
 - (S2) The electricity price profile \mathbf{p} is updated to reflect the latest charging strategies determined by the PEV population in (S1).
 - (S3) Steps (S1) and (S2) are repeated until the change in the price profile at (S2) is negligible.
- Using an appropriate individual cost function and price update mechanism, (S1)-(S3) is convergent and achieves the socially optimal (centralized) solution.

Individual cost function

$$J_n(\mathbf{u}_n; \mathbf{p}) \triangleq \sum_{t \in \mathcal{T}} \left\{ p_t u_{nt} + g_{nt}(u_{nt}) \right\} - h_n \left(\sum_{t \in \mathcal{T}} u_{nt} \right)$$

- ▶ Cost is composed of energy cost, local (demand and battery degradation) cost, and the benefit derived from the total delivered energy.
- ▶ The optimal charging strategy of the n -th PEV, with respect to \mathbf{p} :

$$\mathbf{u}_n^*(\mathbf{p}) = \underset{\mathbf{u}_n \in \mathcal{U}_n}{\operatorname{argmin}} J_n(\mathbf{u}_n; \mathbf{p})$$

- ▶ This optimal response has the form:

$$u_{nt}(\mathbf{p}, A_n) = \max \left\{ 0, [g'_{nt}]^{-1}(A_n - p_t) \right\}, \quad t \in \mathcal{T}$$

for some A_n , where g'_{nt} is the derivative of g_{nt} , and $[g'_{nt}]^{-1}$ denotes the corresponding inverse function.

Price profile update mechanism

- ▶ Let

$$p_t^+(\mathbf{p}) = p_t + \eta \left(c'(d_t + \sum_{n \in \mathcal{N}} u_{nt}^*(\mathbf{p})) - p_t \right), \quad t \in \mathcal{T}$$

where $\eta > 0$ is a fixed parameter, and $\mathbf{u}_n^*(\mathbf{p})$ is the optimal charging strategy for the n -th PEV with respect to \mathbf{p} .

- ▶ Assuming the terminal valuation function h_n is increasing and strictly concave:

$$\|\mathbf{u}_n^*(\mathbf{p}) - \mathbf{u}_n^*(\mathbf{q})\|_1 \leq 2\nu \|\mathbf{p} - \mathbf{q}\|_1$$

Theorem: The decentralized algorithm converges to the efficient (centralized) solution \mathbf{u}^{**} .

- ▶ The proof establishes that

$$\|\mathbf{p}^+ - \mathbf{q}^+\|_1 < \|\mathbf{p} - \mathbf{q}\|_1$$

so the price update operator $\mathbf{p}^+(\mathbf{p})$ is a contraction map.

Illustration - convergence

Evolution of $\|\mathbf{p}^{(k)} - \mathbf{p}^{**}\|_1$ for various values of the price update parameter η .

- ▶ Convergence is guaranteed for $0 < \eta < 1.017$.

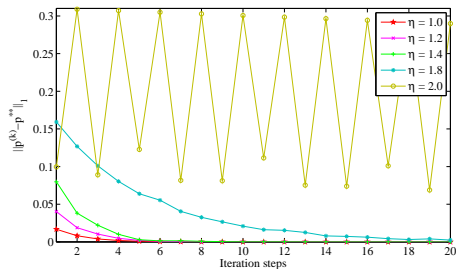
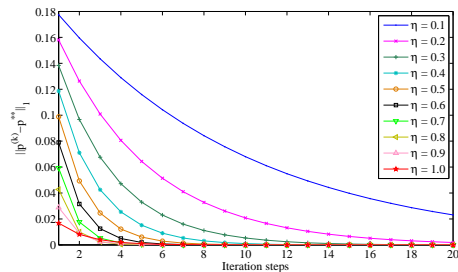
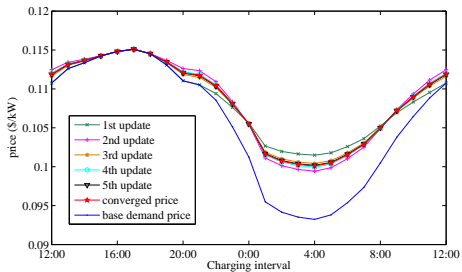


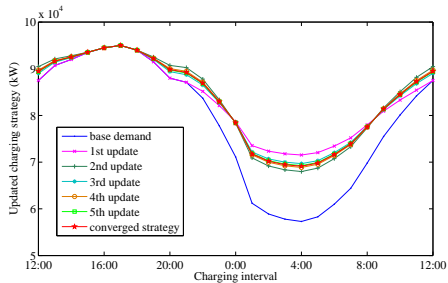
Illustration - algorithm updates

Price update parameter $\eta = 1$.

Price

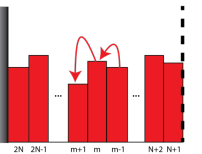
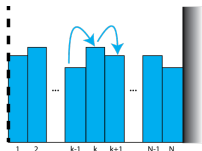


Total demand



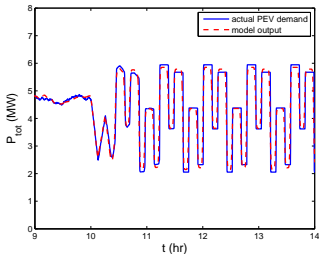
Ensemble control of hysteretic loads

- ▶ Example: thermostatically controlled loads.
- ▶ State-space modelling results in a nonlinear hybrid dynamical system.
 - ▶ Nonlinear because states and inputs multiple together.
 - ▶ Hybrid due to the influence of rapidly changing inputs.

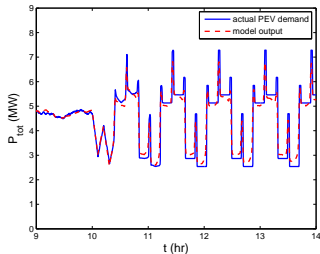


θ_- Temperature θ_+

Period-3 orbit
(Input period = 15.6 min)



Period-4 orbit
(Input period = 12.4 min)



Conclusions

- ▶ Responsive load control offers an effective approach to compensating for the variability inherent in large-scale renewable generation and mitigating the effects of unplanned generation and transmission outages.
- ▶ Expansive communications networks and advances in distributed control algorithms facilitate precise, non-disruptive forms of load control.
- ▶ Numerous challenges remain though:
 - ▶ Highly distributed, heterogeneous, uncertain resources.
 - ▶ Control structure, nonlinearity, latency, inter-operability.
 - ▶ Data security.
 - ▶ Modelling and analysis.

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