



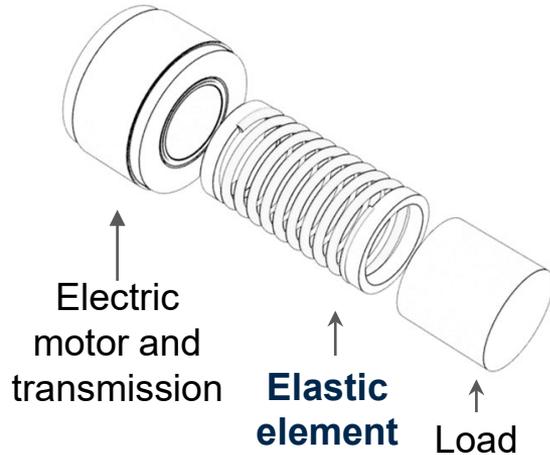
# **NRI: FND: COLLAB: Optimal Design of Robust Compliant Actuators for Ubiquitous Co-Robots**



NSF Awards  
1830360 → 1953908  
(Gregg/Rezazadeh)  
1830338 (Rouse)

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April 19, 2022

# Series elastic actuators

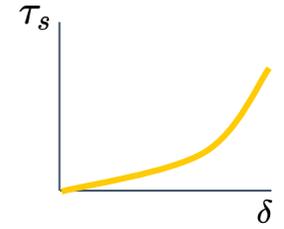
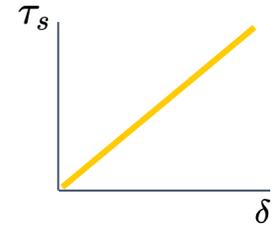


Poor selection of stiffness for given task may:

- Increase peak power
- Increase energy consumption

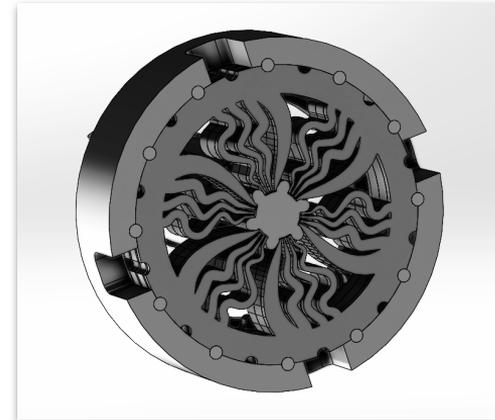
**We lack fundamental understanding for robust design!**

1. Design of **energy efficient series springs** as a **convex** optimization program



2. **Robust feasible** design of SEAs

3. Mechanical design of **optimal nonlinear springs**



# Quadratic expression for energy consumption

$$E_m = a\alpha^2 + b\alpha + c$$

for spring compliance  $\alpha = 1/k$

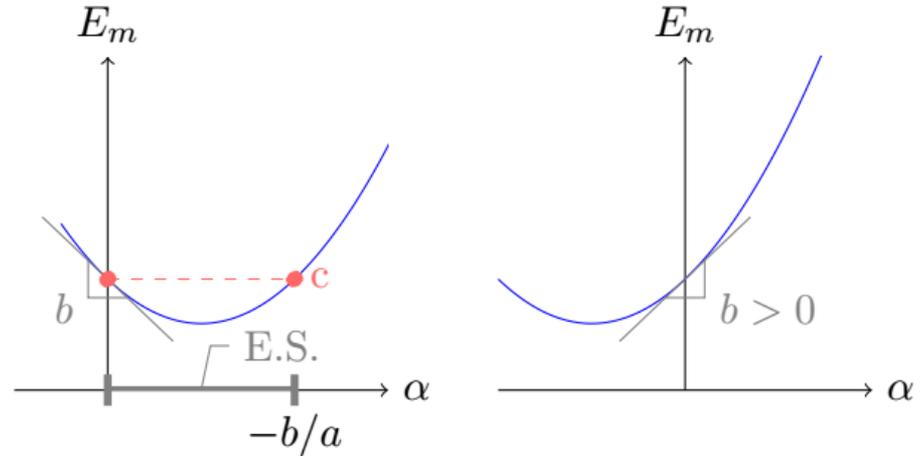
The quadratic expression is **convex**:

$$\frac{d^2 E_m}{d\alpha^2} = 2a \geq 0$$

**C** is the energy consumption of a **rigid** actuator:

$$\lim_{k \rightarrow \infty} E_m = c$$

The **necessary** condition for a linear series elastic element to **save energy**:  $b < 0$



# Thank you!



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See you at our poster!

Project website: <http://mysite.du.edu/~srezazad/SEA-Optimization.html>