

# Sequential Contracts for Uncertain Electricity Resources

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- Motivation & Background

# Outline

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- Propose two (flexible) sequential contracts with and without monitoring
- Comparison of the three different contract schemes
- Conclusion & future work

# Smart Grids

- Introduction of new electricity resources into the grid
  - Renewable energy (RE) resources: wind, solar
  - Flexible/responsive demands: deferrable loads



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33% penetration by 2020 in California



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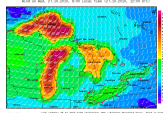
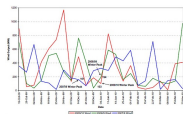
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- **Key characteristics:**

- **Uncertainty:** cannot follow a predetermined schedule (non-dispatchable resources)
- **Dynamic information:** Information arrives over time. Wind generation can be precisely predicted only 15min in advance.



**“Develop rules for market evolution that enable system flexibility”** is listed as an area of intervention to accommodate high renewable energy penetration. NREL, “Integrating Variable Renewable Energy in Electric Power Markets”, 2012.

*Actions to Support Flexibility: lead the development and innovation of market designs; encourage market operators to adopt rules to improve system efficiency; and play a leading role in negotiating a framework for integration that optimizes flexibility across regions*

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**Question:** What is an appropriate market mechanism that addresses **uncertainty** and **dynamic varying** nature of new resources in addition to **strategic behavior** and **private information** considerations?

## Current Practice (in the U.S.)

Small share of RE  $\sim$  4% penetration

Uncertain resources (mostly wind) are integrated into the RT market

- Participating Intermittent Resource Program (PIRP) in California requires SO to accept all produced wind power
- Highly Subsidized, e.g. 30% subsidy for investment, guaranteed grid-access
- No (mild) imbalance penalties
- Fixed feed-in tariffs
- Costs of reserved are socialized among load serving entities (LSE)

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This approach cannot be sustained for higher penetration levels

- Reliability and stability concerns
- LSEs are reluctant to undertake the increased cost of reserves
- Social welfare loss
- Uncertain resources need to be exposed to market mechanisms

## Alternative Practice (in the U.K.)

**Firm contract** : The RE generator commits to a firm quantity  $q$  in advance, upon deviation it pays penalty at marginal rate  $\lambda$ .

Example: wind generator  $C(q) := \mathbb{E}_W \{ \lambda \max(q - g(W), 0) \}$

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- Fits to the current two-settlement market structure

**Related Literature:** Bitar *et al.* (2012), Goldsmith *et al.* (2014), Bitar *et al.* (2014), Nayyar *et al.* (2014), Jain *et al.* (2014)



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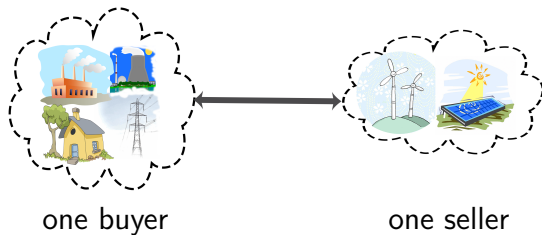
- Fits to the current two-settlement market structure
- Treats uncertain resources as conventional resources

**Ignores the available information that arrives after the contract signing**

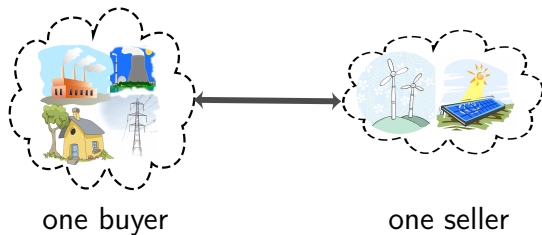
**Provides no flexibility for uncertain resources**

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# Model

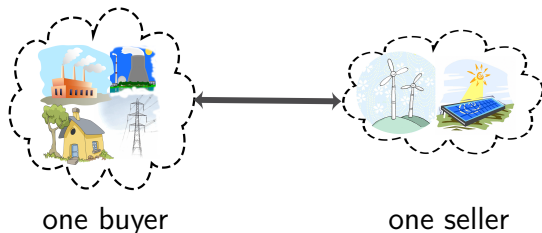


# Model



- Buyer's utility  $\mathcal{V}(q)$  with marginal utility  $v(q)$

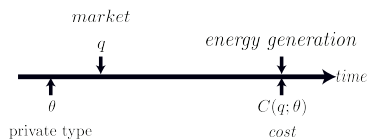
# Model



- Buyer's utility  $\mathcal{V}(q)$  with marginal utility  $v(q)$
- Seller's cost  $C(q; \theta)$  with marginal cost  $c(q; \theta)$   
 $\theta$ : seller's type

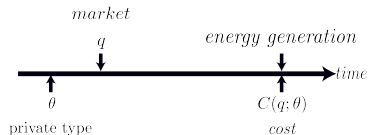
# Time Diagram

- Conventional generators

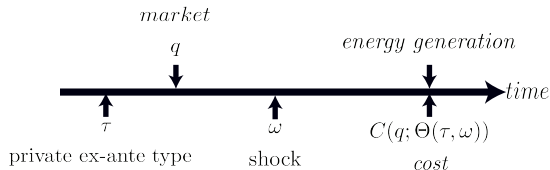


# Time Diagram

- Conventional generators



- Uncertain Resources (e.g. wind farm)



- Ex-ante type  $\tau$  (time=1) *e.g. wind speed*
- Shock  $\omega$  (time=2)
- (Ex-post) type  $\theta = \Theta(\tau, \omega)$  increasing in  $\tau$  and  $\omega$ .

## Model

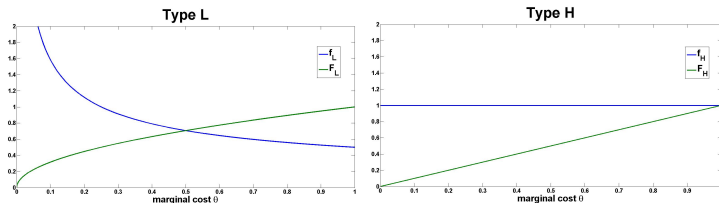
- **time = 1**,  $\tau$  takes two values:  $H$  and  $L$  with prob.  $p_L$  and  $p_H$   
 $F_L(\theta)$  and  $F_H(\theta)$ : conditional cdf of ex-post type  $\theta$
- **time = 1<sup>+</sup>**: buyer and seller sign a contract  
agree on quantity and payment (functions)  $(q, t)$
- **time = 2**:  $\omega$  is observed with cdf  $G(\omega)$ ,  $\omega$  is independent of  $\tau$

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- **Type L has a lower cost on average (FSD):**

$F_H(\theta) \leq F_L(\theta)$  for all  $\theta \in [\underline{\theta}, \bar{\theta}]$  (first order stochastic dominance)

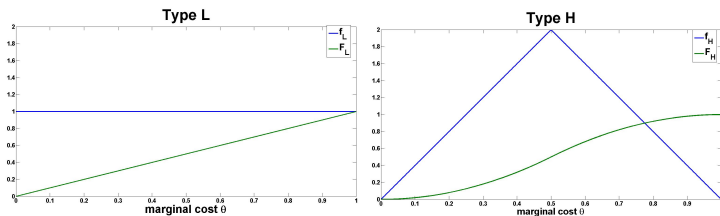


Example: wind farm  $C(q; \Theta(\tau, \omega)) = \lambda \max \{q - \gamma_\tau \omega^3, 0\}$ ,  $\gamma_L > \gamma_H$



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 $F_L(\theta)$  and  $F_H(\theta)$ : conditional cdf of ex-post type  $\theta$
- **Type L has higher uncertainty, same expected cost (MPS):**  
 $\theta_L = \theta_H + \xi$  where  $\mathbb{E}\{\xi|\theta_H\} = 0$  (mean preserving spread)



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The difference between ex-ante types:

- (i) FSD: type  $L$  has a lower cost on average
- (ii) MPS: same expected cost, type  $L$  has a higher uncertainty

## Model - Assumption

Both buyer and seller are risk neutral (quasi-linear utility)

Buyer is the mechanism designer

Technical assumptions:

- *Non-shifting support*
- *Monotone cross hazard rate*

## Mechanism Design Problem

Buyer's objective (from the revelation principle):

$$\underset{(q,t)}{\text{maximize}} \quad \mathbb{E}\{\mathcal{V}(q(\tau, \omega)) - t(\tau, \omega)\}$$

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- **IC**: the seller has incentive to report truthfully its private information
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We have  $\mathcal{S} - \mathcal{R} = \mathbb{E}\{\mathcal{V}(q(\tau, \omega)) - t(\tau, \omega)\}$

$\mathcal{S}$ : social welfare (buyer's utility + seller's utility)

$\mathcal{R}$ : seller's utility (information rent)

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# Efficient Allocation

Full information, no strategic behavior ( $\mathcal{R} = 0$ )

$$\underset{(q,t)}{\text{maximize}} \quad \mathcal{S}$$

Efficient allocation

$$v(\tilde{q}^{e*}(\tau, \theta)) = c(\tilde{q}^{e*}(\tau, \theta))$$

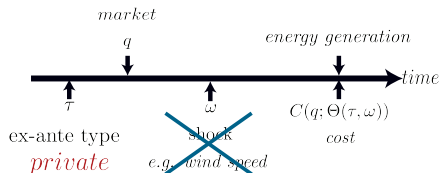


## Firm Contract

- **Firm allocation:**  $q^f(\tau)$  is fixed and independent of  $\omega$   
 $t^f(\tau)$  denote the expected payment.

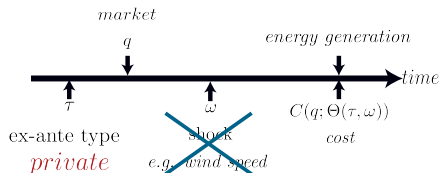
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The optimal firm forward contract:

$$\begin{aligned} & \underset{(q^f, t^f)}{\text{maximize}} && \mathcal{S} - \mathcal{R} \\ & \text{subject to} && \text{IC for ex-ante type } \tau \\ & && IR \end{aligned}$$

# Firm Contract

## Theorem

With two ex-ante types, the allocation  $q^{f*}(\tau)$  of the optimal firm forward contract satisfies

$$v(\tilde{q}^{f*}(L)) = \mathbb{E}_{F_L}\{c(\tilde{q}^{f*}(L); \theta)\},$$

$$v(\tilde{q}^{f*}(H)) = \mathbb{E}_{F_H}\{c(\tilde{q}^{f*}(H); \theta)\} + \frac{p_L}{p_H} [\mathbb{E}_{F_H}\{c(\tilde{q}^{f*}(H); \theta)\} - \mathbb{E}_{F_L}\{c(\tilde{q}^{f*}(H); \theta)\}];$$

**distortion due to exclusion new information (shock  $\omega$ )**  
**distortion due to strategic behavior**

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the associated payment function  $t^{f*}(\tau)$  is given by

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**cost compensation**

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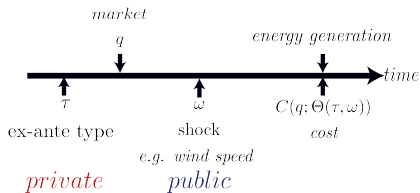
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**cost compensation**  
**incentive for truth-telling of ex-ante type L**

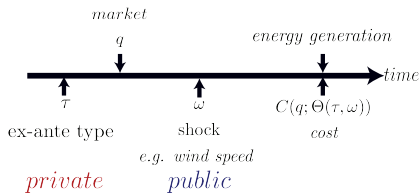
## Flexible Contract with Public Shock

- **Flexible contract with public shock:** ex-ante type  $\tau$  is private and shock  $\omega$  is publicly observed (e.g. wind speed).



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$q^c(\tau, \omega)$ : allocation function

$t^c(\tau, \omega)$ : payment function

The optimal flexible contract with public shock

$$\underset{(q^c, t^c)}{\text{maximize}} \quad \mathcal{S} - \mathcal{R}$$

subject to IC for ex-ante type  $\tau$

IR



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$$v(q^{c^*}(L, \omega)) = c(q^{c^*}(L, \omega); \Theta(L, \omega)),$$

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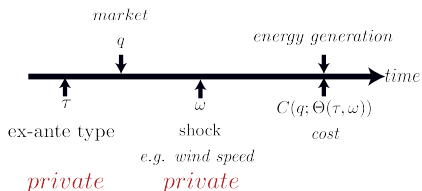
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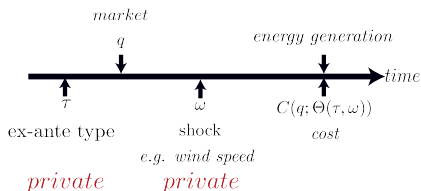
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The optimal flexible contract with public shock

$$\text{maximize}_{(q^P, t^P)} \mathcal{S} - \mathcal{R}$$

subject to IC for ex-ante type  $\tau$ , IC for shock  $\omega$

$IR$

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the associated payment function  $\tilde{t}^{P^*}(\tau, \theta)$  is given by

$$\tilde{t}^{P^*}(L, \theta) = C(\tilde{q}^{P^*}(L, \theta); \theta) + \int [F_L(\hat{\theta}) - F_H(\hat{\theta})] C_\theta(\tilde{q}^{P^*}(H, \hat{\theta}); \hat{\theta}) d\hat{\theta}$$

$$+ \left[ \int_{\theta}^{\bar{\theta}} C_\theta(\tilde{q}^{P^*}(L, \hat{\theta}); \hat{\theta}) d\hat{\theta} - \int F_L(\hat{\theta}) C_\theta(\tilde{q}^{P^*}(L, \hat{\theta}); \hat{\theta}) d\hat{\theta} \right]$$

cost compensation

incentive for ex-ante  
type L

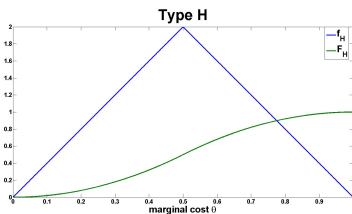
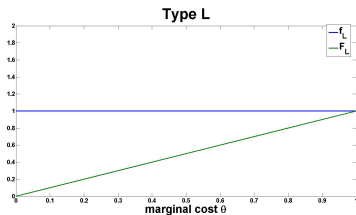
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incentive for shock  $\omega$

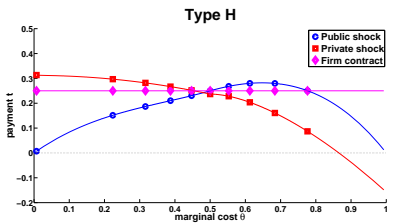
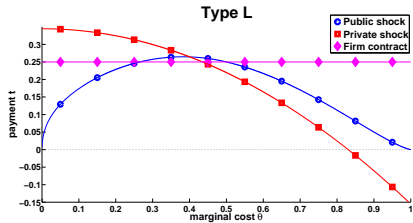
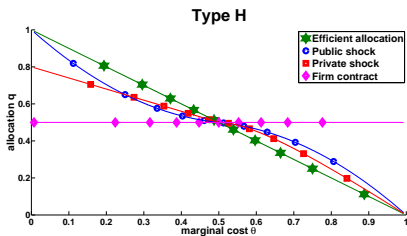
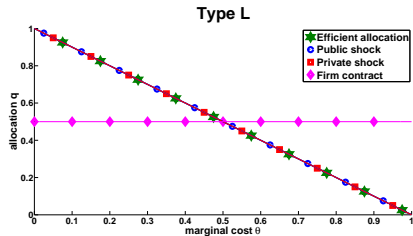
# Example

## MPS case



# Example

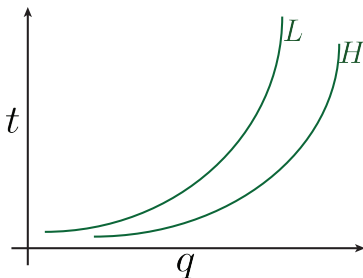
## MPS case



# Sequential Contracts as Menus of Contracts

## Flexible contracts:

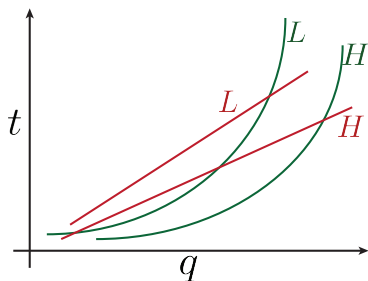
- At  $t=1^+$ , seller chooses curve  $L$  or  $H$   
curve  $\tau$  is parameterized by  $\omega$  as  $\{q(\tau, \omega), t(\tau, \omega)\}$
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## Firm contracts:

- At  $t=1^+$ , seller chooses  $\{q(L), t(L)\}$  or  $\{q(H), t(H)\}$
- At  $t=2$ , seller is penalized at fixed rate  $\lambda$

# Comparison

## Theorem

*Among the three different optimal contract schemes, the buyer's total utility is the highest from the forward contract under uncertainty with public shock and is the lowest from the firm forward contract. That is,*

$$S_c^* - \mathcal{R}_c^* \geq S_p^* - \mathcal{R}_p^* \geq S_f^* - \mathcal{R}_f^*.^a$$

*flexible with public shock   flexible with private shock   firm contract*

---

<sup>a</sup>The result holds for any finite number of ex-ante type  $\tau$ .

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*flexible with flexible with firm  
public shock private shock contract*

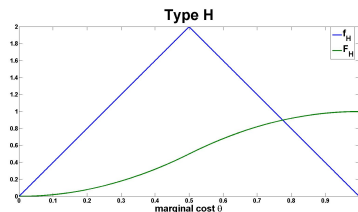
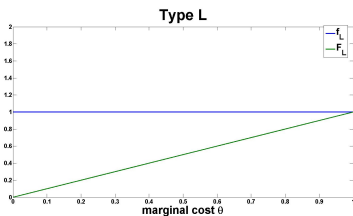
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**Theorem does not imply a similar ranking for social welfare or information rent!**

# Monitoring May Hurt!

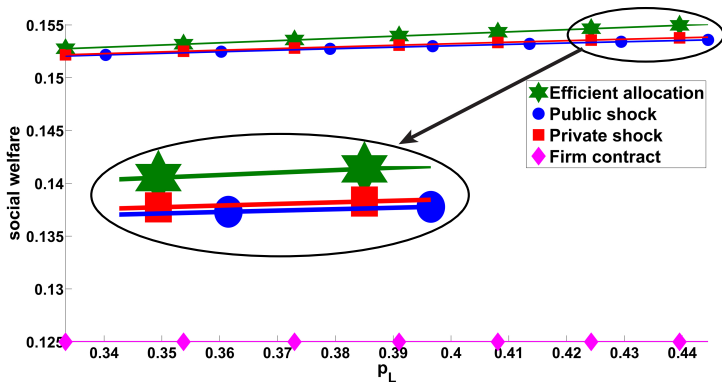
## Example: MPS case





# Monitoring May Hurt!

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- With flexible contracts one can distinguish between sellers with different uncertainty levels, while firm contracts treat them the same
- We showed that monitoring does not necessarily improve the social welfare



## Ongoing & Future Work

- Investigate the value of penalty instrument and risk exposure
- Extension to multiple buyers/sellers

### Reference:

H. Tavafoghi and D. Teneketzis, "Sequential Contracts for Uncertain Electricity Resources", NetEcon, 2015.