

# Multi-Dimensional Forward Contracts under Uncertainty for Electricity Markets

**H. Tavafoghi and D. Teneketzis**

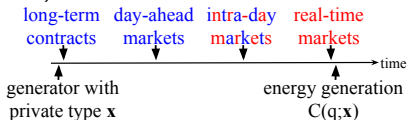
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# Electricity Markets under Uncertainty

- ▶ Conventional energy generators (e.g. thermal)

- ▶ Forward markets and real-time markets are similar



- ▶ Renewable energy generators (e.g. wind, solar)

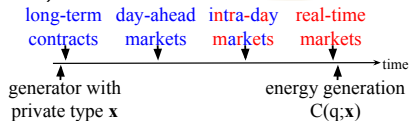
- ▶ Forward markets and real-time markets are different

- ▶ Renewable generators (3% share) participate in RT markets (5% share of markets)
- ▶ Gradually (required) participate in forward markets (95% share of markets)
- ▶ Need to rethink electricity market mechanisms
  - ▶ Non-strategic aspects: stochastic optimal power flow problem
  - ▶ Strategic aspects: market design & analysis

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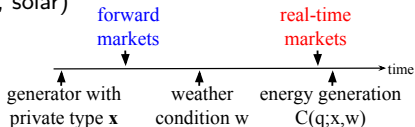
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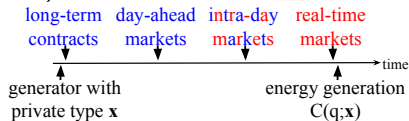


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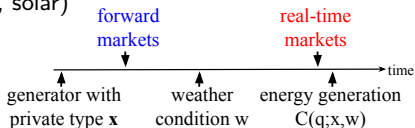
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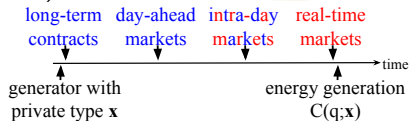
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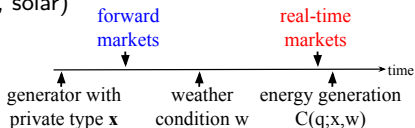
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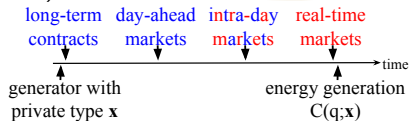


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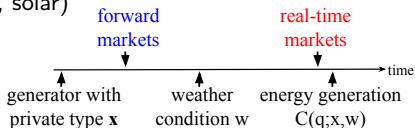
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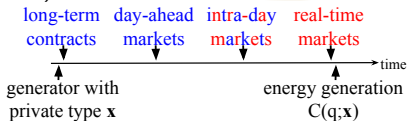


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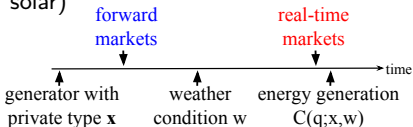
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# Multi-Dimensional Forward Contracts under Uncertainty

- ▶ **Our approach:** contract design
  - ▶ Strategic behavior
  - ▶ Multi-dimensional private information
  - ▶ Uncertainty and satisfies
    - ▶ Interim voluntary participation (in expectation)
    - ▶ Ex-post voluntary participation (for every realization of uncertainty)
  - ▶ The optimal mechanism is a menu of pricing schemes:  
First, the buyer offers them and the seller chooses one  
Second, according to realization  $w$  of the uncertainty one point from the selected pricing scheme is implemented.
- ▶ Contract with deterministic allocation
  - ▶ Contract with incentive payments for demand response (DR) program
- ▶ Contracts with random allocation that depends on the uncertainty
  - ▶ Bilateral trade between a buyer and a wind generator



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