

# A Framework for Hierarchical, Probabilistic Planning and Learning

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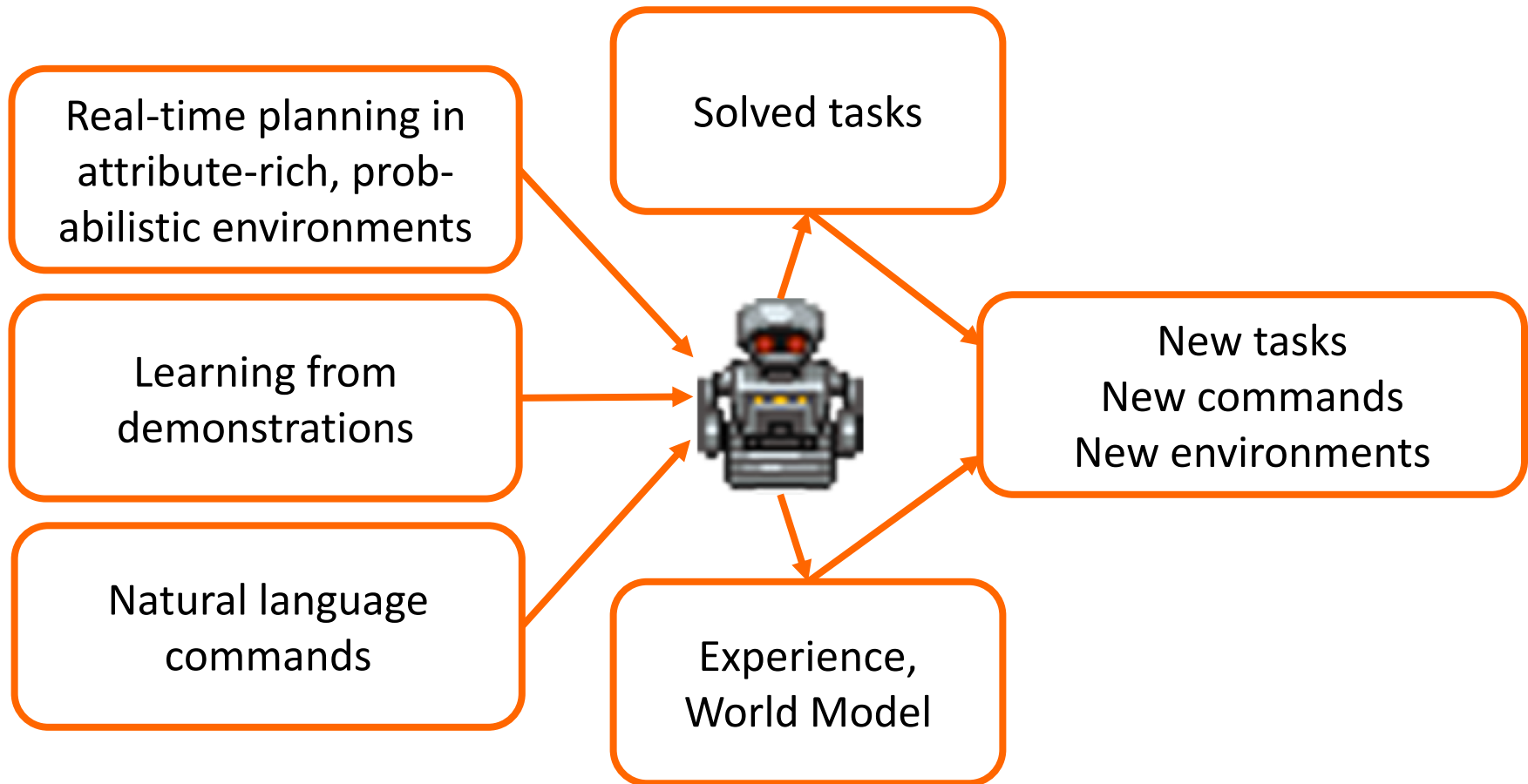
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# Planning in Robotics Domains

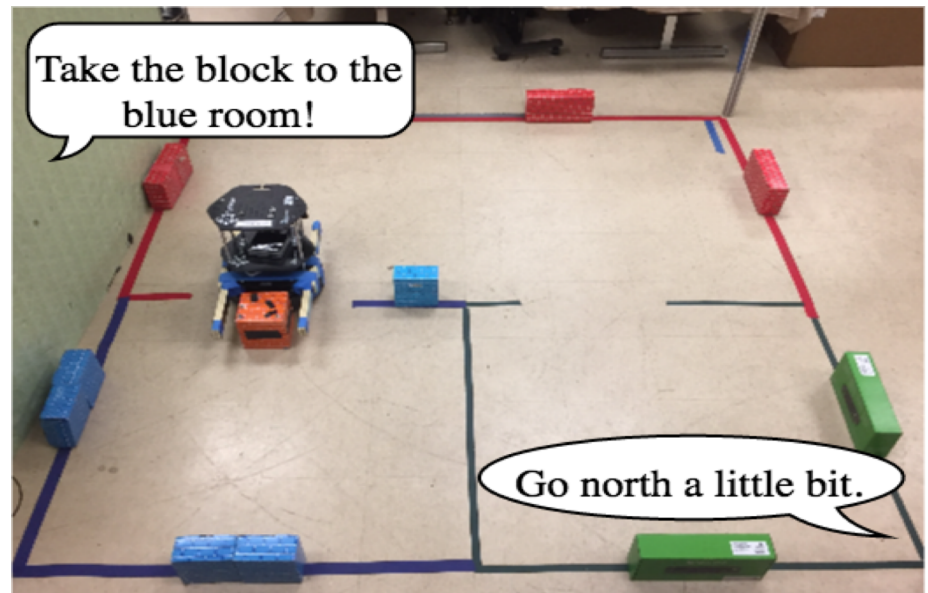
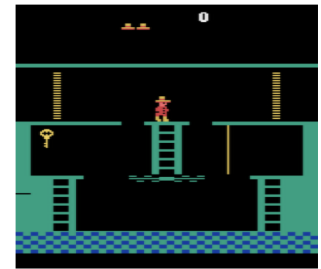
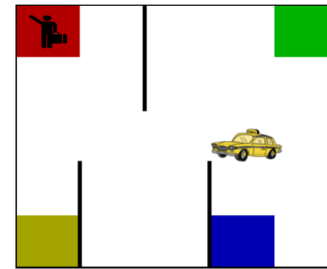
**Varied, huge, stochastic, and messy**



# Objectives

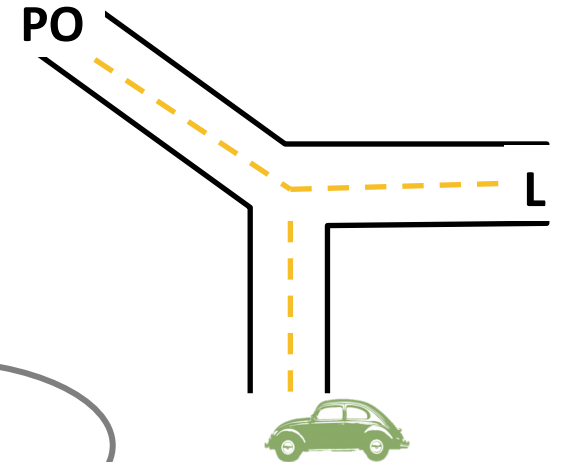
## Efficient, non-domain-specific planning

1. Learn hierarchies from data
2. Plan efficiently within them
3. Learn language groundings to drive tasking



# Non-Hierarchical Planning

- Without hierarchy, consider all possible action sequences from all states



Go to Post Office

Go to Library

**Post office:**

- Turn L 60°
- Turn R 90°
- Straight
- Turn R 90°

**There yet?**

Turn L  
60°

Turn L  
90°

Turn R  
60°

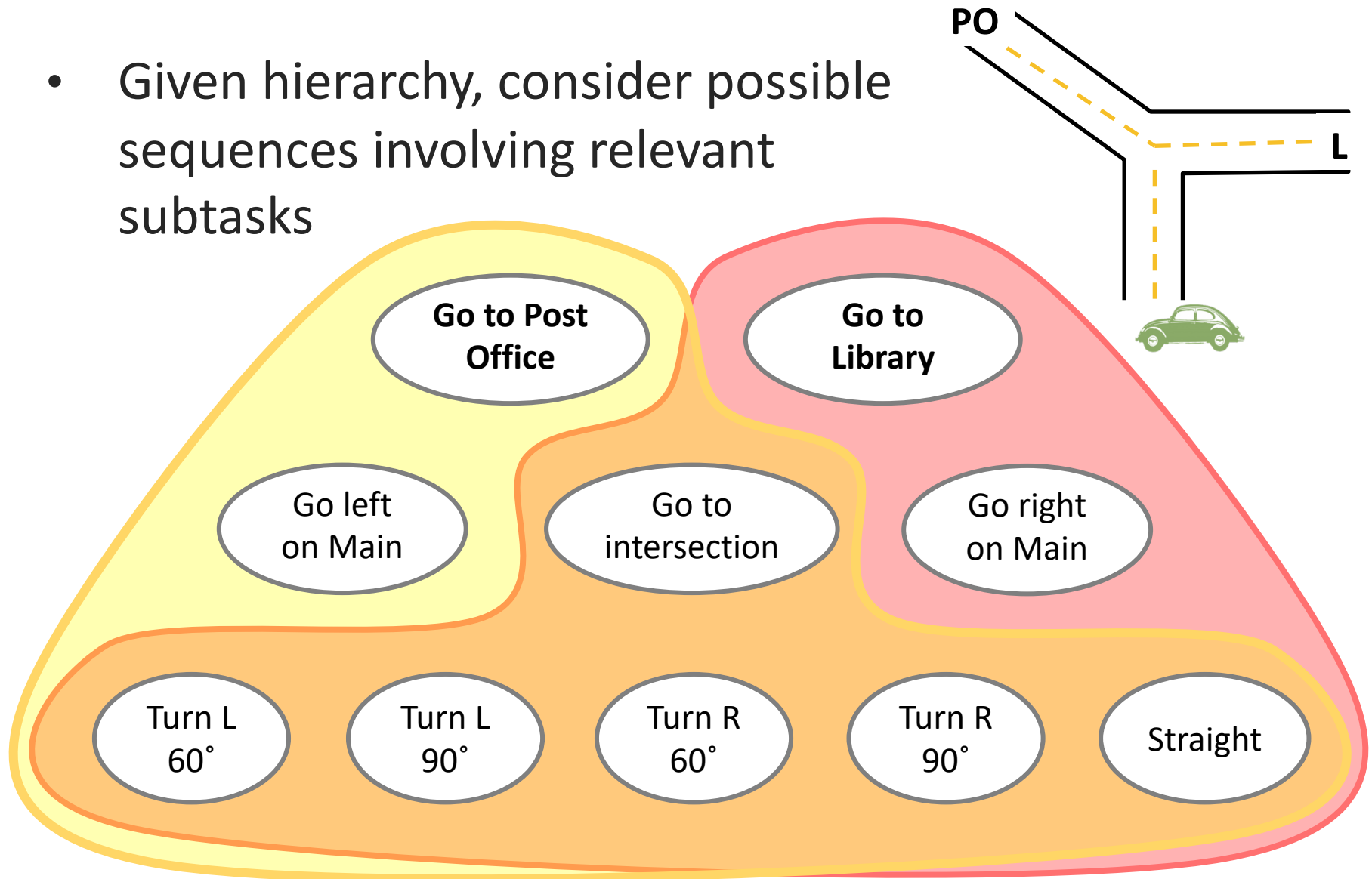
Turn R  
90°

Straight



# Top-Down Hierarchical Planning

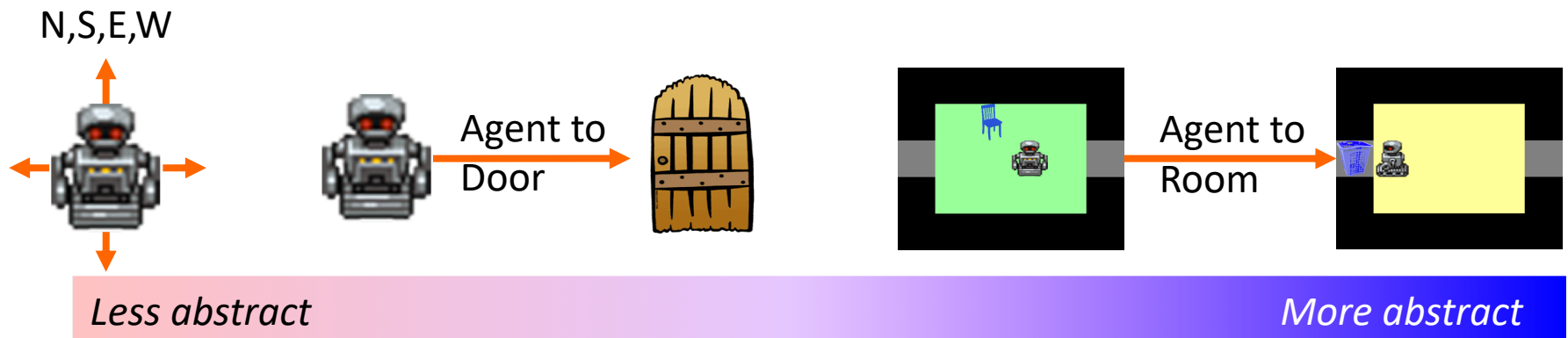
- Given hierarchy, consider possible sequences involving relevant subtasks



# Abstract MDPs (AMDPs)

## Markov Decision Processes, plus abstraction:

- MDP (MDP):  $\langle \mathcal{S}, \mathcal{A}, T, R, \epsilon \rangle$ :
  - States, actions, transitions, rewards, terminal states
- Abstract MDPs add **state mapping functions**:  
 $\langle \mathcal{S}, \mathcal{A}, T, R, \epsilon, F \rangle$
- $F^l : s \rightarrow s^l$  projects states from ground level to current level of abstraction

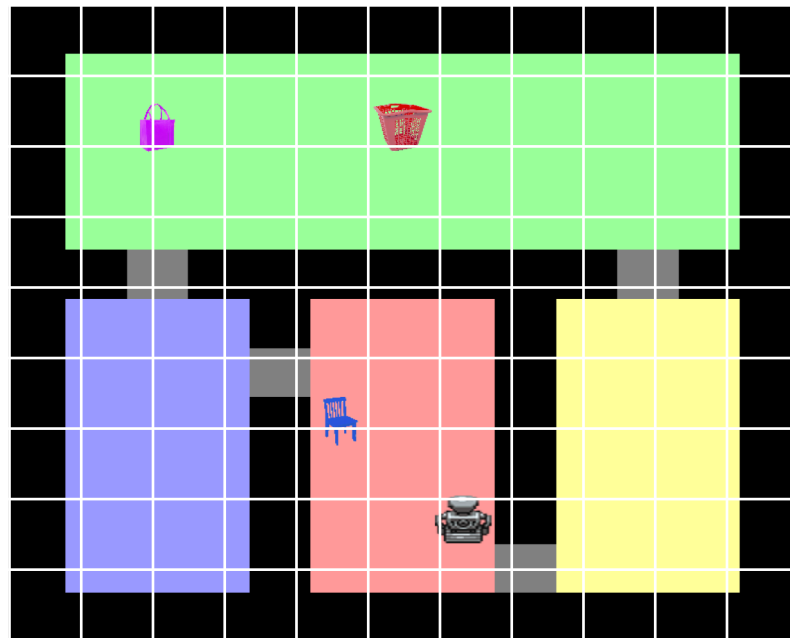


# Projecting to Abstract States

- Cleanup task requires going **red** → **green** → **blue**

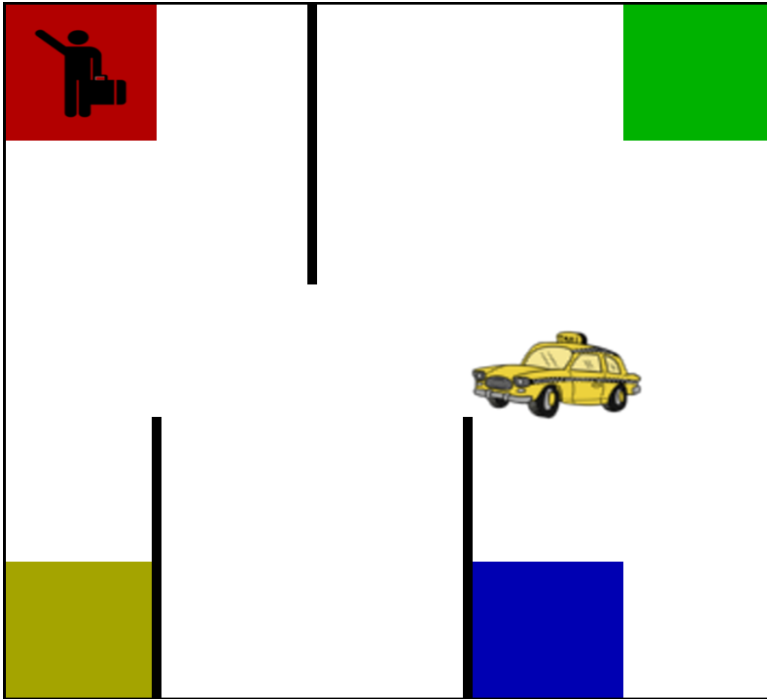
- Don't need exact location when planning next room to visit

- X, Y coordinates **projected up to** appropriate level

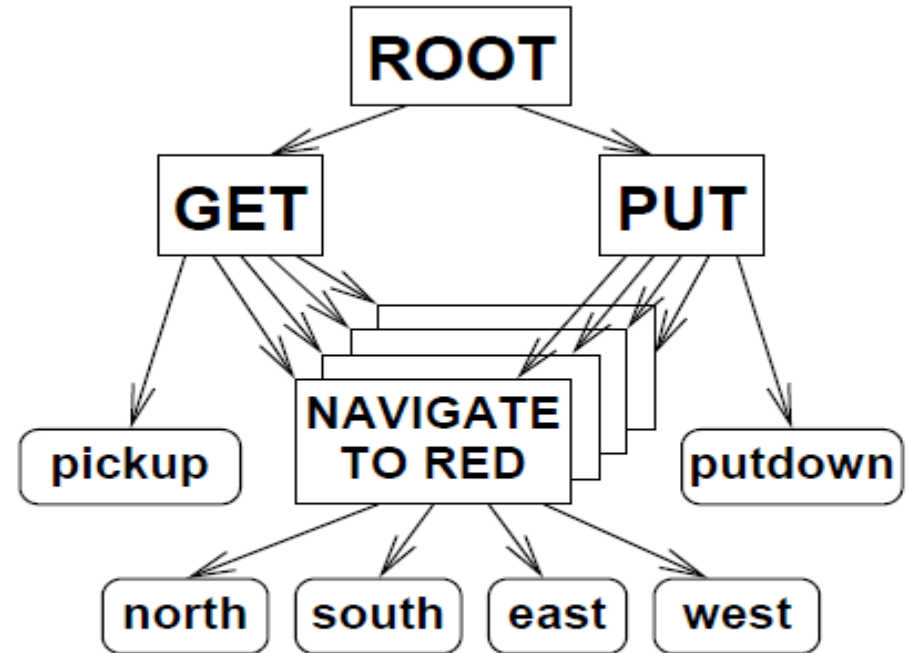


- $\text{loc}\langle 7, 2 \rangle \xrightarrow{F^1} \text{loc}\langle \text{"red room"} \rangle$

# Classic Taxi Domain + Task Hierarchy

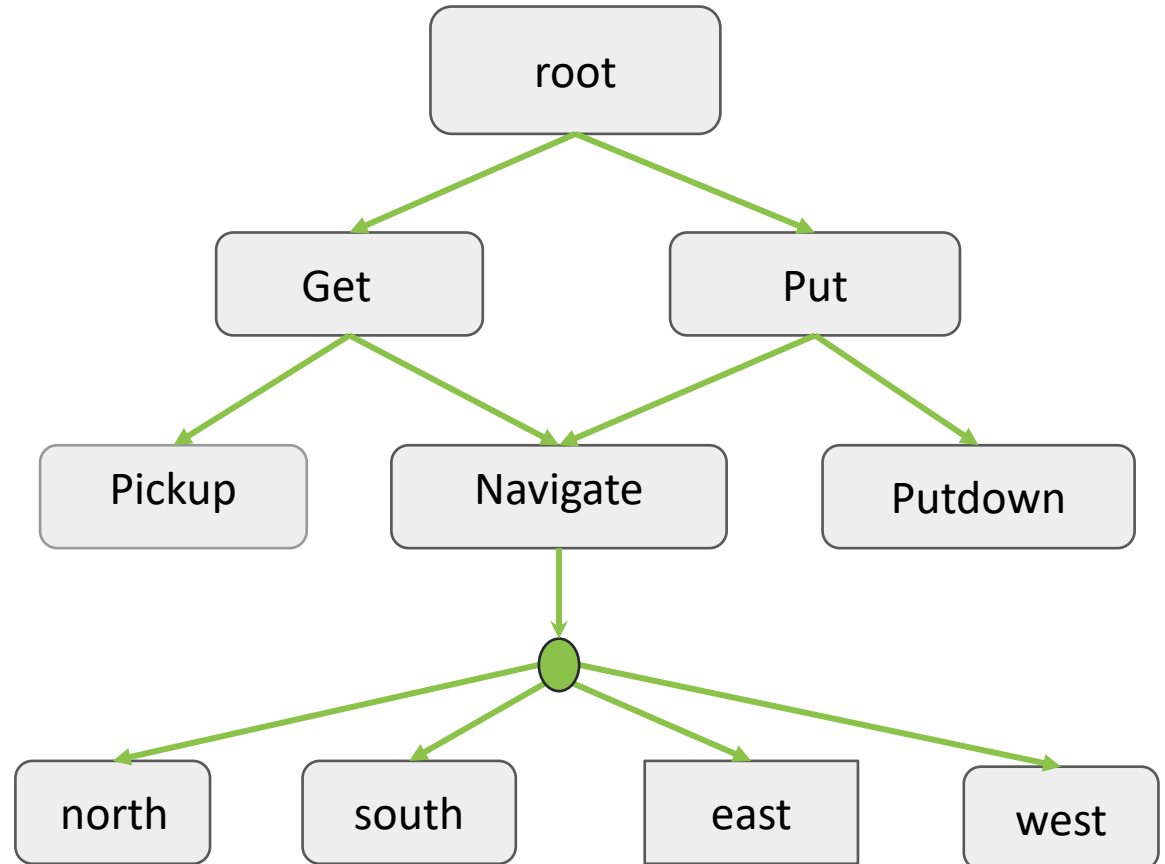
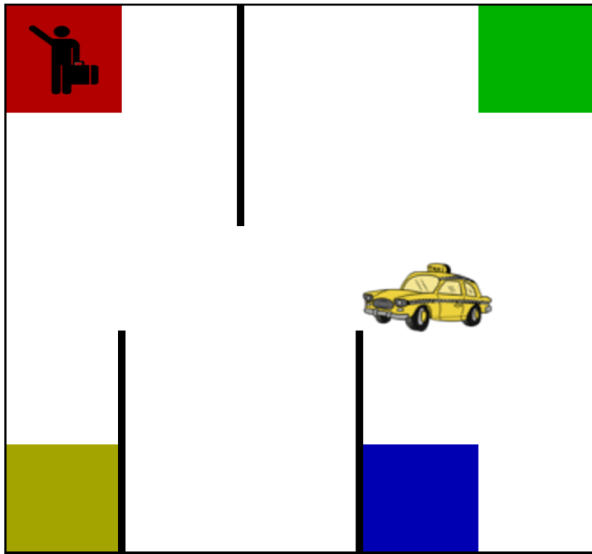


Taxi Domain (Dietterich, 2000)  
Agent is taxi, must take passenger to depot (red, yellow, green, blue)



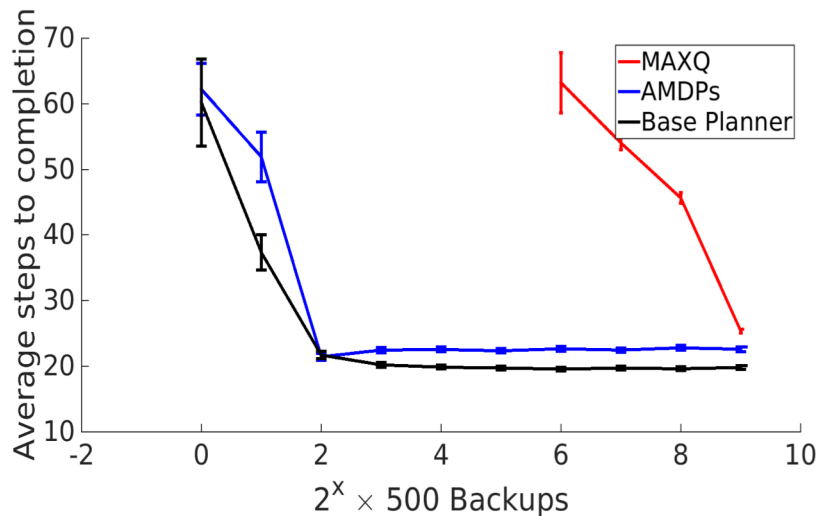
A Task Hierarchy for Taxi  
(rectangles are subgoals, leaf nodes are ground actions)

# Taxi Representation as AMDP

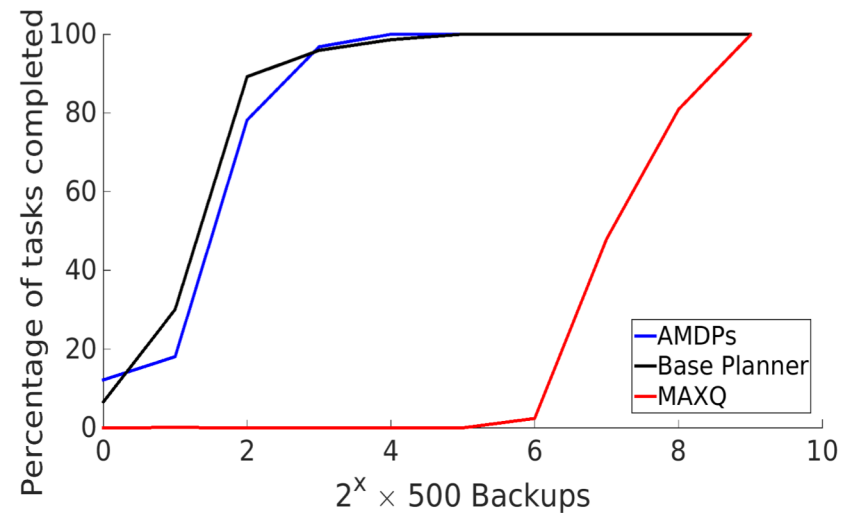


# AMDP Planning: Taxi

- Domain is too small to benefit

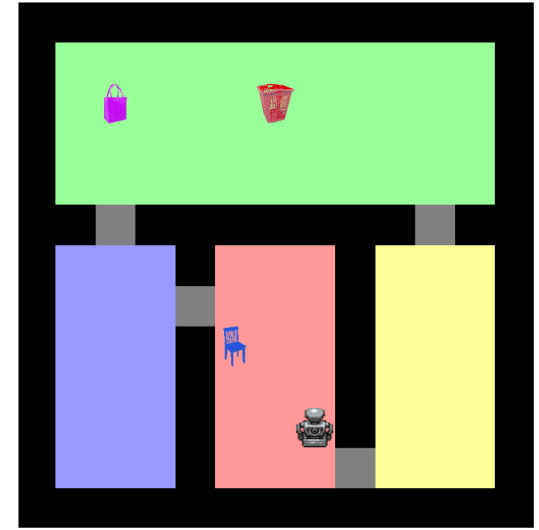
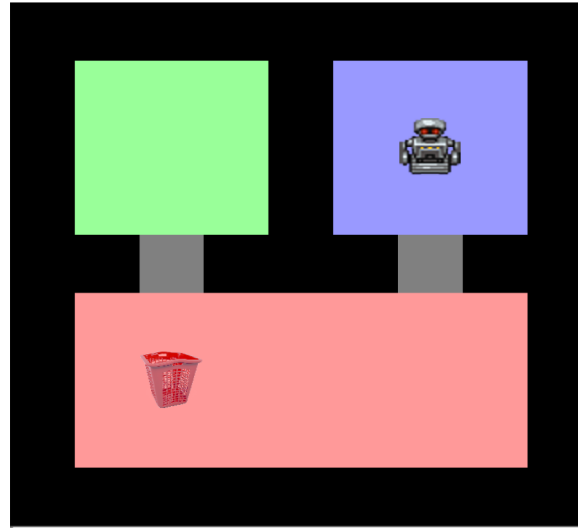
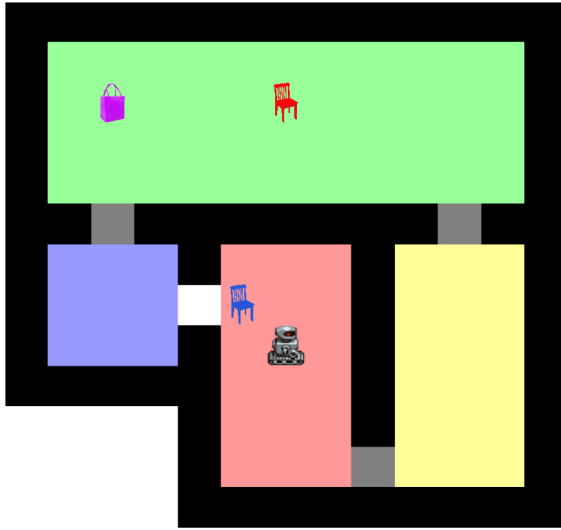


Lower is better

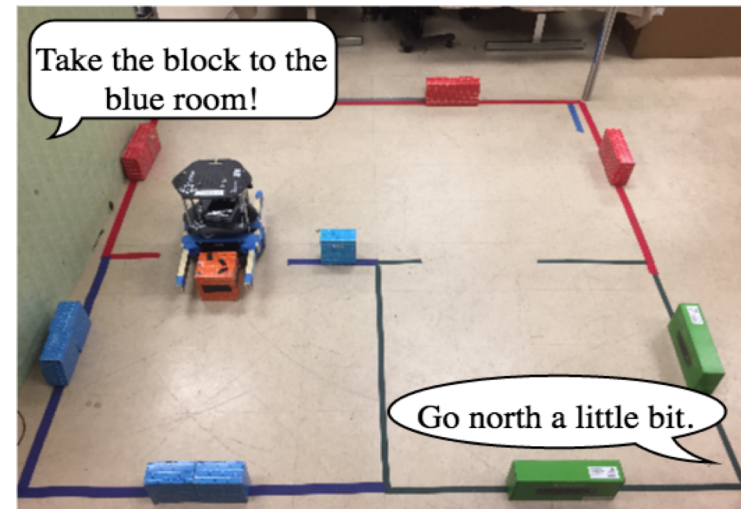


Higher is better

# Cleanup Domain

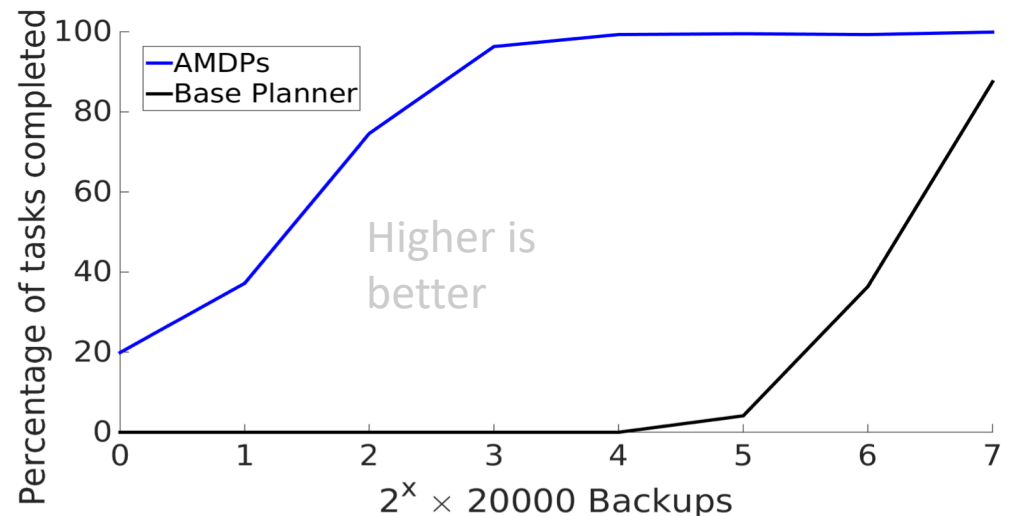
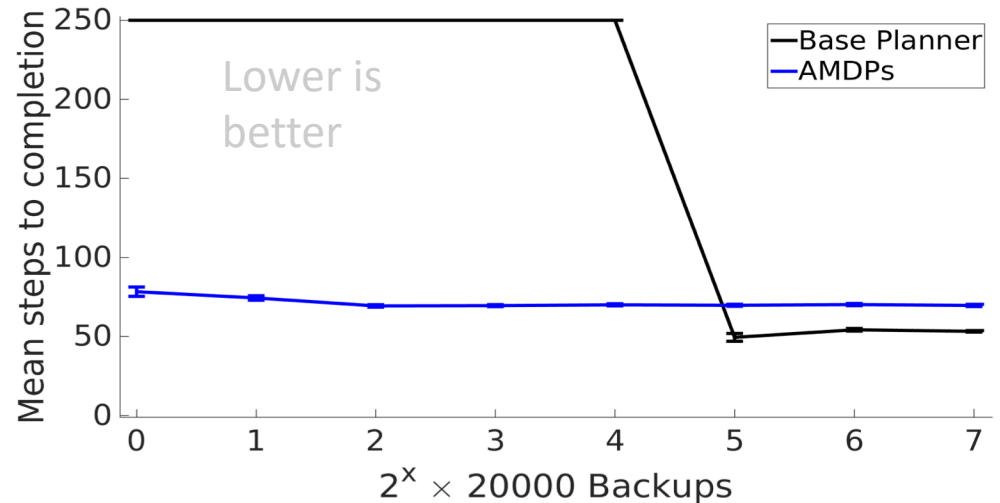


- **State:** Agent and object location / orientation, door lock boolean
- **Actions:** N, S, E, W, Pull
  - Stochastic transitions possible.
- **Objectives:** Take specified object or agent to specified room



# Planning over AMDPs in Cleanup

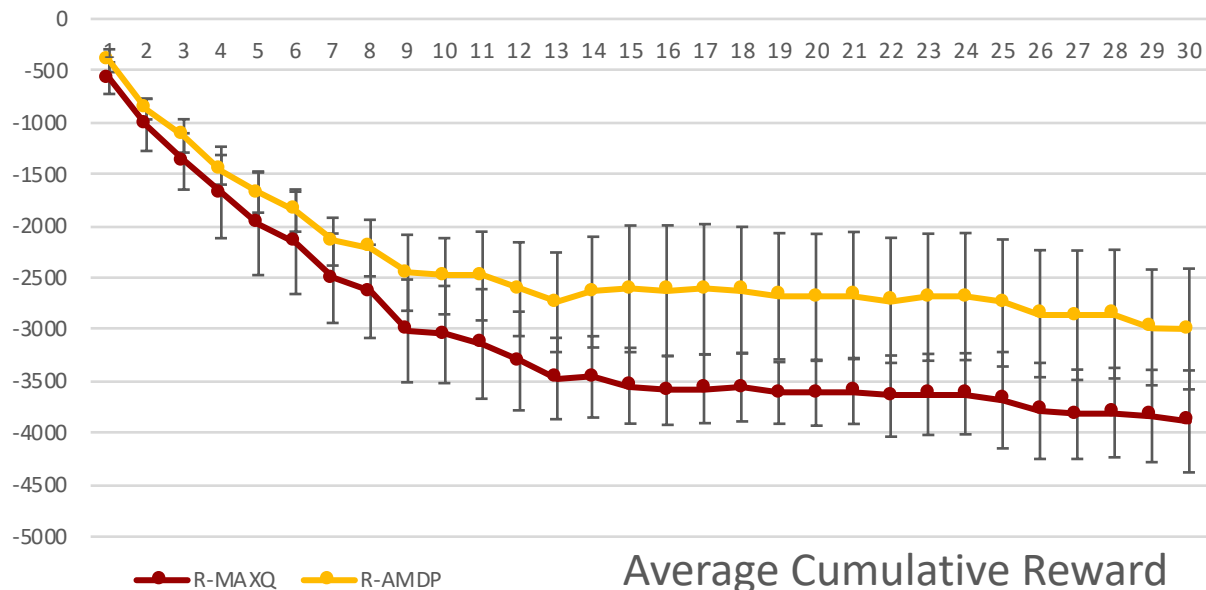
- Complex task
  - Many objects
  - Highly combinatorial
- AMDPs **start** finding solutions much faster
  - Fewer backups compared to optimal solver





# R-MAX + AMDP<sub>s</sub> (R-AMDP<sub>s</sub>) / PALM

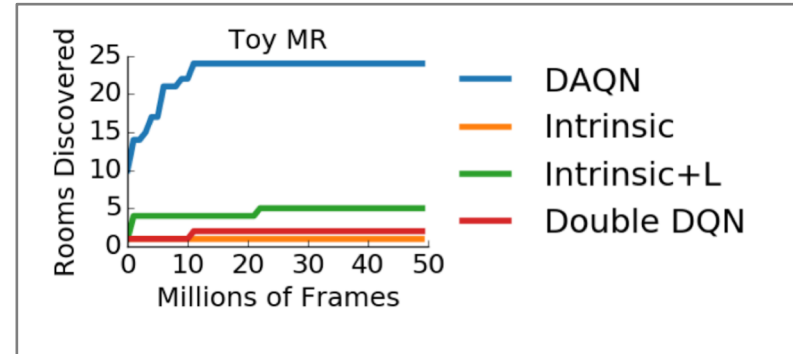
- Plan top-down starting at R-AMDP-Plan( $H$ ,  $Root$ )
  - Determine next action
  - Ground to subgoal (A)MDP
  - Recurse to ground MDP
  - On return, update model for  $T$  and  $R$



## 2. Learning Hierarchies

### Strategies:

- Quality of behaviors derived from types of approximate abstractions (ICML 2016)
- Combine deep reinforcement learning with model-based approaches using expert-provided state abstractions (AAMAS 2018)
- Learn AMDP hierarchies, rewards, and transition functions directly from data (AAAI 2019, *under submission*)



$$\eta_{model} = \frac{(1-\gamma)^2}{1 + \gamma(|\mathcal{S}_G| - 1)} \frac{1}{(1-\gamma)^3}$$
$$\eta_{bolt} = \frac{\left(\frac{|\mathcal{A}|}{1-\gamma} + \varepsilon k_{bolt} + k_{bolt}\right)}{(1-\gamma)^2}$$
$$\eta_{mult} = \frac{\left(\frac{|\mathcal{A}|}{1-\gamma} + k_{mult}\right)}{(1-\gamma)^2}$$

**None of these is perfect!**

# Approximate State Abstractions

- **Approximate state abstractions:** nearly-identical situations  $\equiv$  equivalent

$$\forall s \in \mathcal{S}_G \quad V_G^{\pi_G^*}(s) - V_G^{\pi^{GA}}(s) \leq 2\epsilon\eta_f$$

- Q functions

$$\eta_{Q^*} = \frac{1}{(1 - \gamma)^2}$$

- Transition and Reward Function

$$\eta_{model} = \frac{1 + \gamma(|\mathcal{S}_G| - 1)}{(1 - \gamma)^3}$$

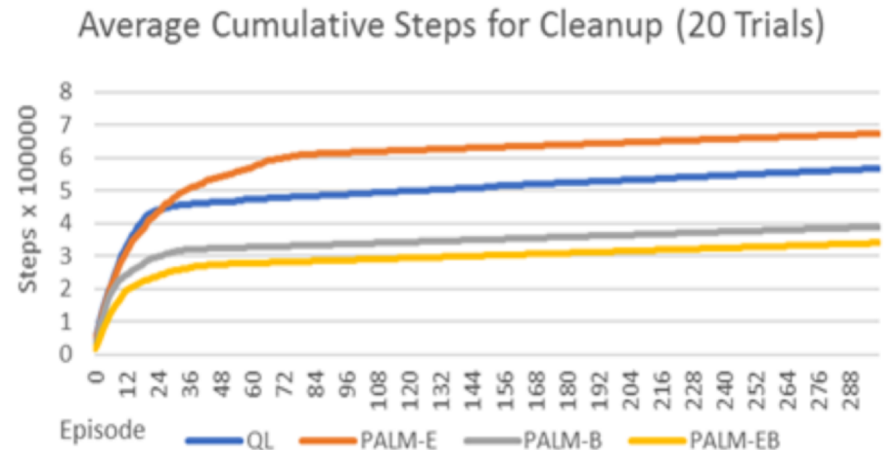
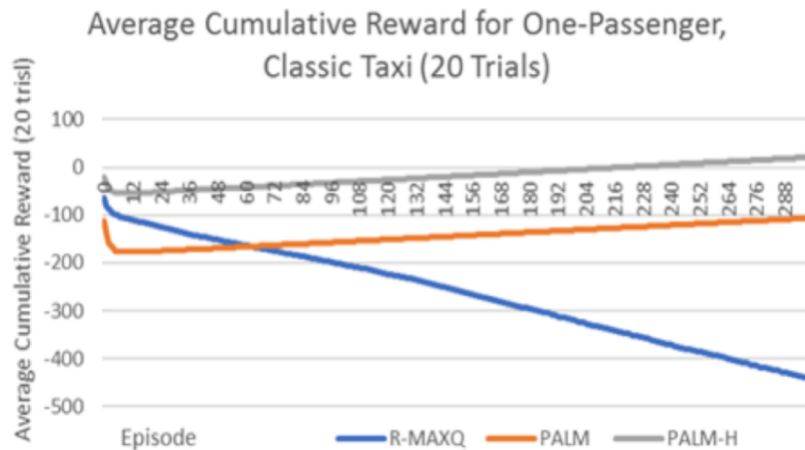
- Boltzmann Distributions over agent actions

$$\eta_{bolt} = \frac{\left(\frac{|\mathcal{A}|}{1 - \gamma} + \epsilon k_{bolt} + k_{bolt}\right)}{(1 - \gamma)^2}$$

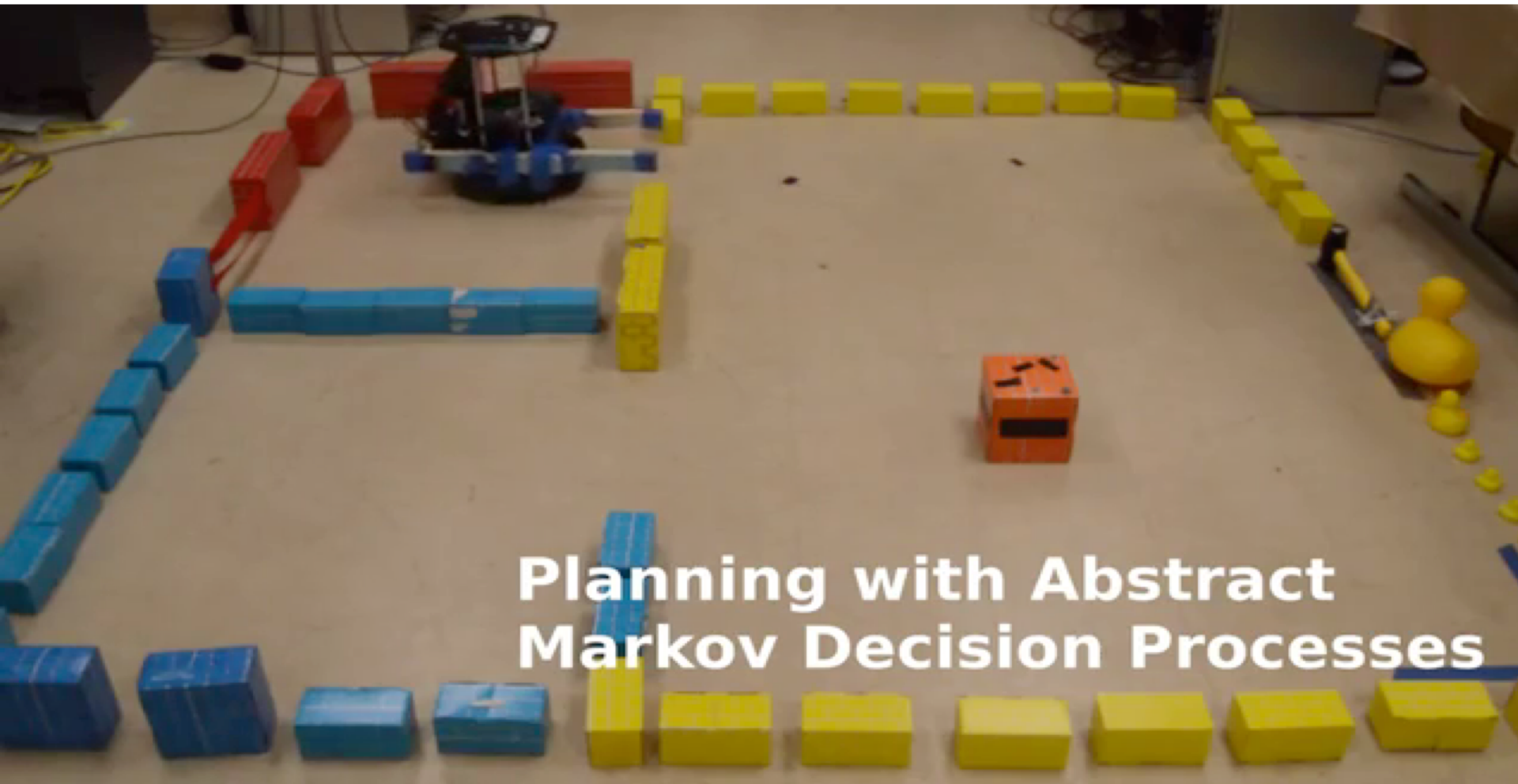
$$\eta_{mult} = \frac{\left(\frac{|\mathcal{A}|}{1 - \gamma} + k_{mult}\right)}{(1 - \gamma)^2}$$

# Deep Abstract Q Networks

- Model learning with R-Max to learn AMDP transition and reward models.
- HierGen to learn hierarchies for tasks using data provided by example solution trajectories



# Planning Example



**Planning with Abstract  
Markov Decision Processes**

# Publications

- Near Optimal Behavior via Approximate State Abstraction - David Abel, D. Ellis Hershkowitz, Michael L. Littman. ICML 2016
- Planning with Abstract Markov Decision Processes - Nakul Gopalan, Marie desJardins, Michael L. Littman, James MacGlashan, Shawn Squire, Stefanie Tellex, John Winder, Lawson L.S. Wong. Abstraction in Reinforcement Learning Workshop @ ICML 2016.
- Planning with Abstract Markov Decision Processes - Nakul Gopalan, Marie desJardins, Michael L. Littman, James MacGlashan, Shawn Squire, Stefanie Tellex, John Winder, Lawson L.S. Wong. ICAPS 2017.
- Deep Abstract Q-Networks - Melrose Roderick, Christopher Grimm, Stefanie Tellex. Hierarchical RL workshop @ NIPS 2017.
- RAMDP: Model-Based Learning for Abstract Markov Decision Process Hierarchies - Shawn Squire, John Winder, Matthew Landen, Stephanie Milani, and Marie desJardins). Third Multidisciplinary Conference on Reinforcement Learning and Decision Making (RLDM).
- Towards Planning With Hierarchies of Learned Markov Decision Processes - John Winder, Shawn Squire, Matthew Landen, Stephanie Milani, and Marie desJardins. ICAPS workshop on Integrated Execution (IntEx) 2017.
- Deep Abstract Q-Networks - Melrose Roderick, Christopher Grimm, Stefanie Tellex. AAMAS 2018.

# Future Work

*Questions?*

**Our language model grounds natural language commands to plans in real time.**

"Go to the Green room"

