

Against Coordinated Cyber and Physical Attacks: Unified Theory and Technologies

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MOTIVATION

Challenge: Signal processing, robust fault-tolerant control (RFTC) theory and software assurance technologies: developed under different assumptions and models

- Software assurance technologies: model based, require no changes in the profile of the physical dynamics and observations
- RFTC techniques: compensate for the physical damage, assuming control software and sensor data are not compromised



• Extension to the time-critical multi-agent systems:

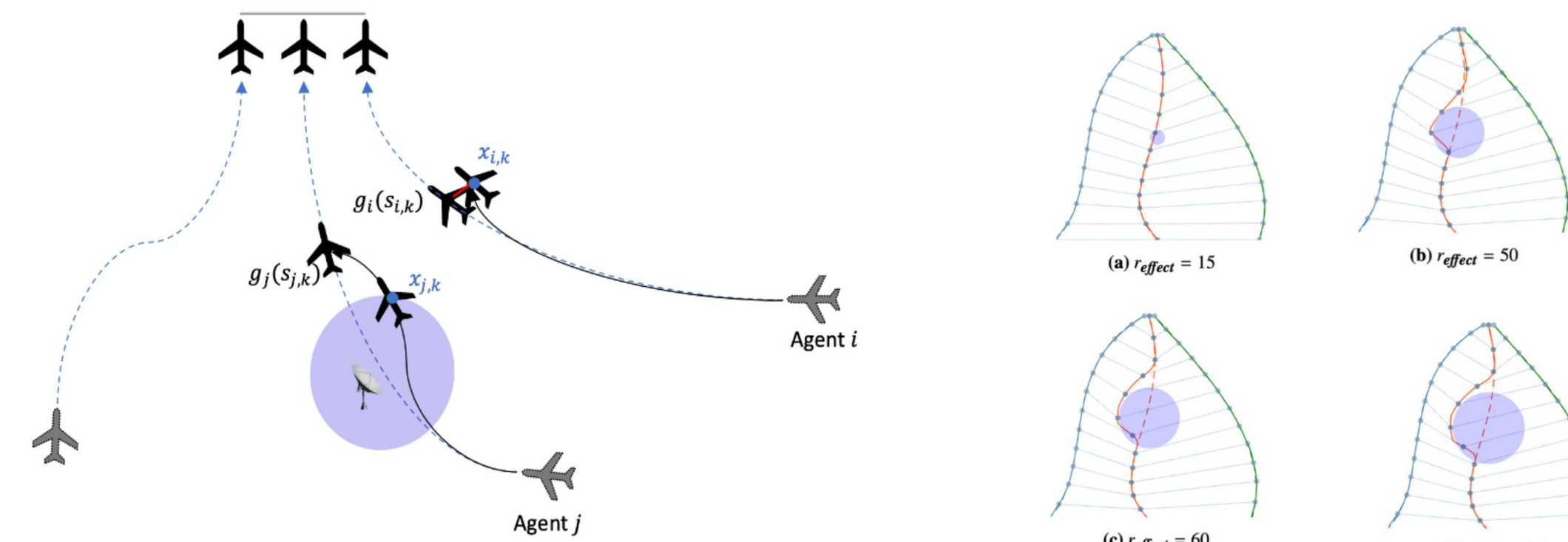
➤ Trajectory following: $g_i(s_{i,k}) - x_{i,k} \xrightarrow{k \rightarrow \infty} 0$; $s_{i,k+1} - s_{i,k} \xrightarrow{k \rightarrow \infty} \rho$

➤ Time coordination: $s_{i,k} - s_{j,k} \xrightarrow{k \rightarrow \infty} 0$

➤ Consensus model: $s_{i,k+1} = s_{i,k} + z_{i,k}$

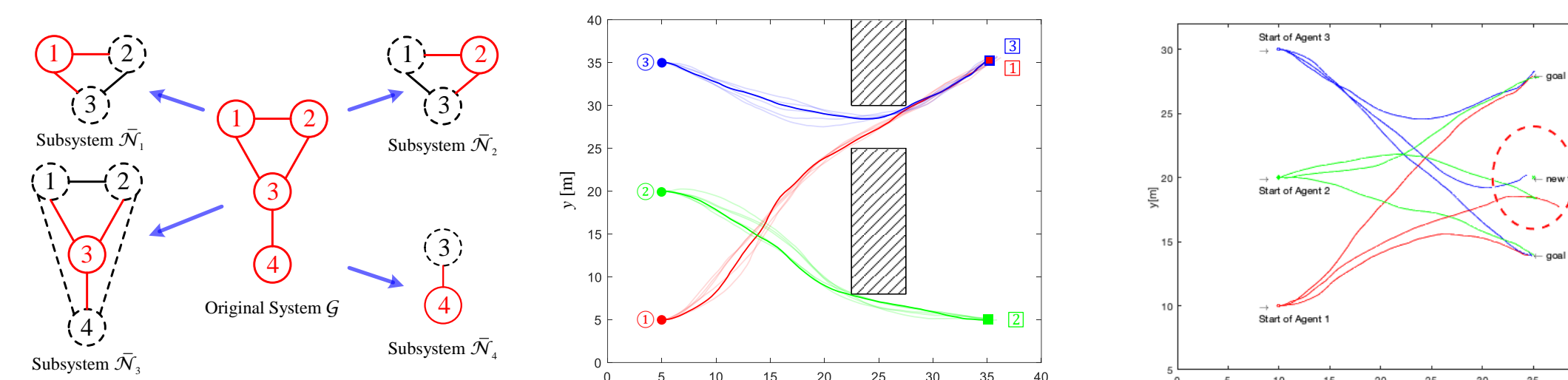
$$z_{i,k} = \max \left\{ -k_e \|g_i(s_{i,k}) - x_{i,k}\| - k_s \sum_{j \in \mathcal{N}(i)} (s_{i,k} - s_{j,k}) + \rho + \mathbf{1}_{\text{attacked}} \hat{z}_{i,k}, 0 \right\}$$

• Attack detection / State estimation with confidence / Escape away from the spoofer



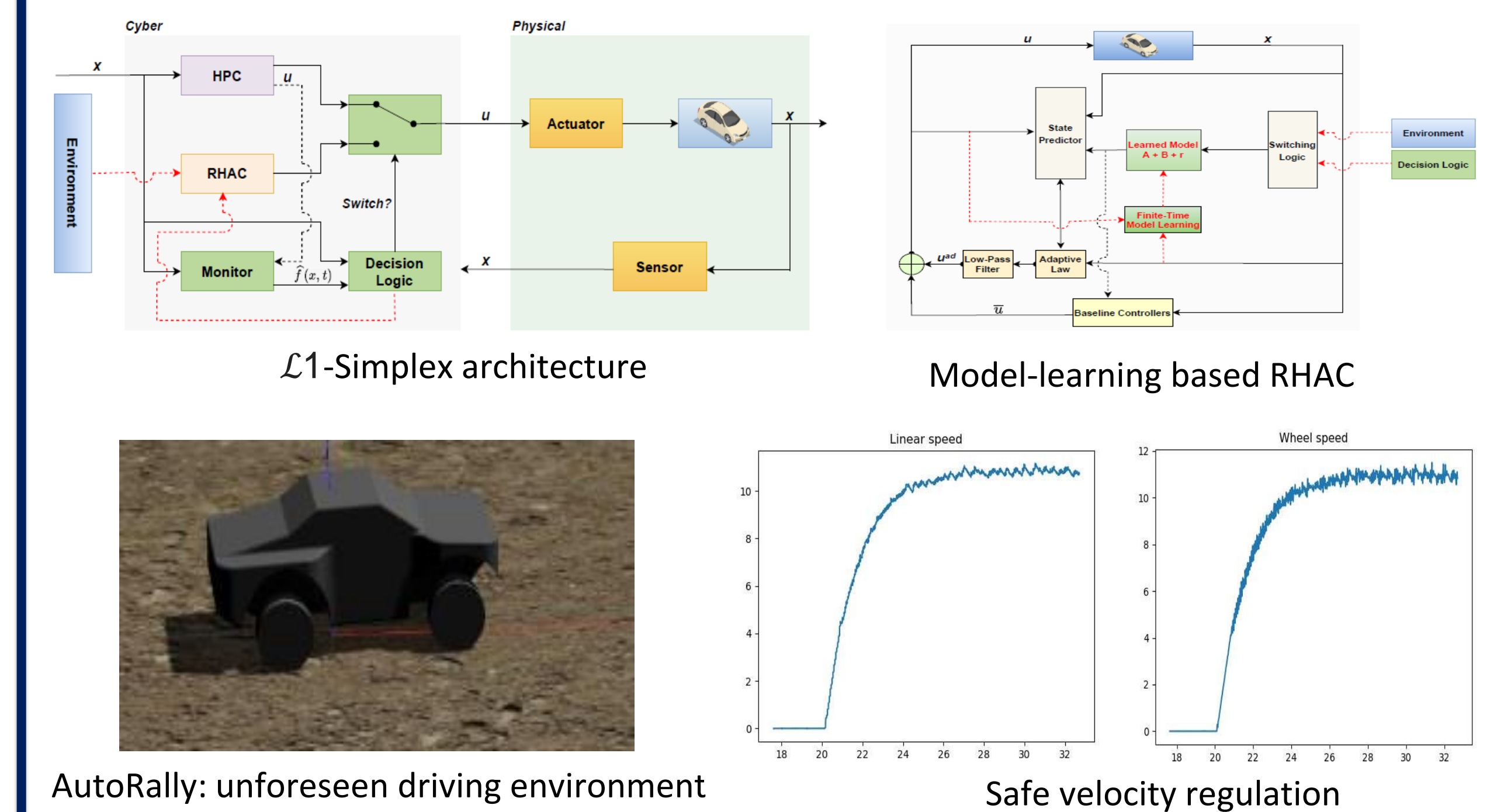
Cooperative Control and Generalization

- **Decentralized** framework and learning algorithms are proposed for stochastic multi-agent systems with **moderate requirements on computation and communication**.
- Generalization algorithms that immediately generate cooperative control law for unlearned tasks from previously learned control tasks using compositionality is derived.



Finite-Time Model-Learning Based L1-Simplex

- The fundamental assumption of model-based controllers is the availability of a good model of the underlying dynamics in consideration. The large model mismatch induced operational environment therefore poses a formidable threat to the reliability of control systems, especially in the time-critical and safety-critical environments.
- **Main idea:**
 - Incorporate finite-time model learning into L1-Simplex to update the system model when any deviation from the safety envelope occurs.
 - Leverage sample-complexity bounds to achieve fast and reliable model learning.

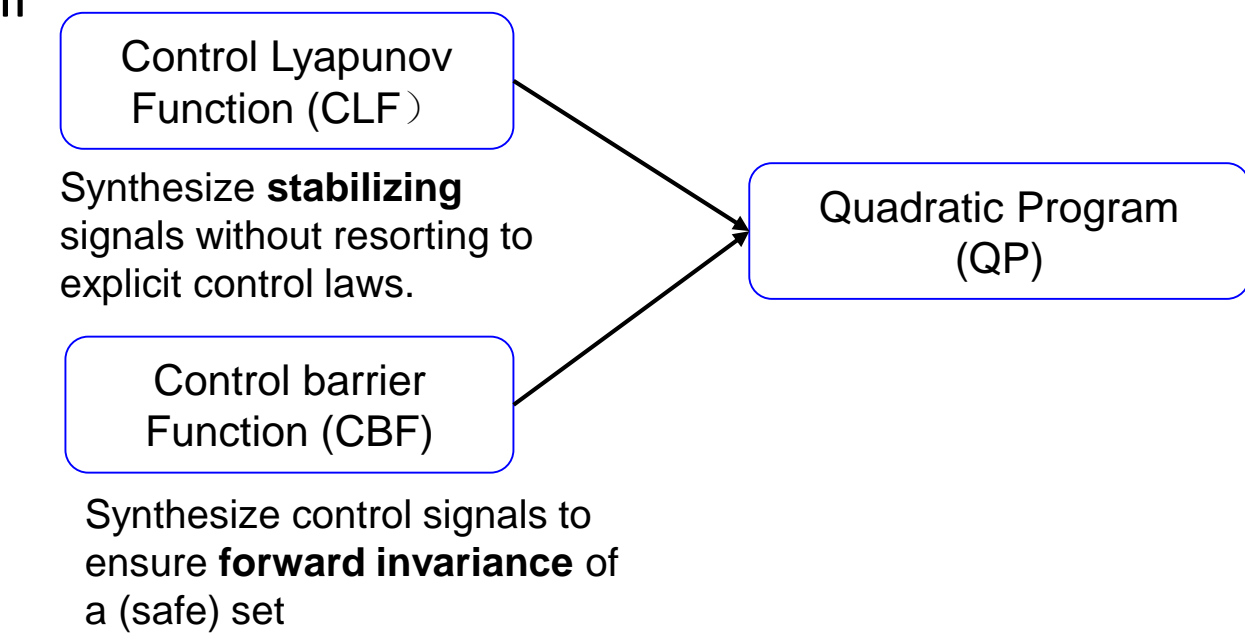


AutoRally: unforeseen driving environment

Safe velocity regulation

Adaptive Robust Quadratic Programs

- QP performance and/or safety guarantee will be compromised in the presence of **model uncertainties and disturbances**.
- Growth rate of the uncertainty is bounded with prior known constants, such that the **uncertainty with computable error bounds can be estimated**.
- Adaptive robust QP: handle **both state-dependent uncertainties and disturbances**, and guarantee satisfaction of **safety-related CBF conditions**:



$$u^*(t, x) = \arg \min_{(u, \delta) \in \mathbb{R}^{m+1}} \frac{1}{2} u^T H(x) u + p \delta^2 \quad (\text{aR-QP})$$

$$\text{s.t. } L_f V(x) + L_g V(x) u + V_z(x) \dot{d}(t) + \|V_x(x)\| \gamma(T) + \alpha(V(x)) < \delta, \quad (\text{R-CLF})$$

$$L_f h(x) + L_g h(x) u + h_z(x) \dot{d}(t) - \|h_x(x)\| \gamma(T) + \beta(h(x)) > 0, \quad (\text{R-CBF})$$

$$u \in U.$$

- Estimate the pointwise value of the uncertainty with computable error bounds.
- Formulate a **robust QP** using the estimated uncertainty and the error bounds.

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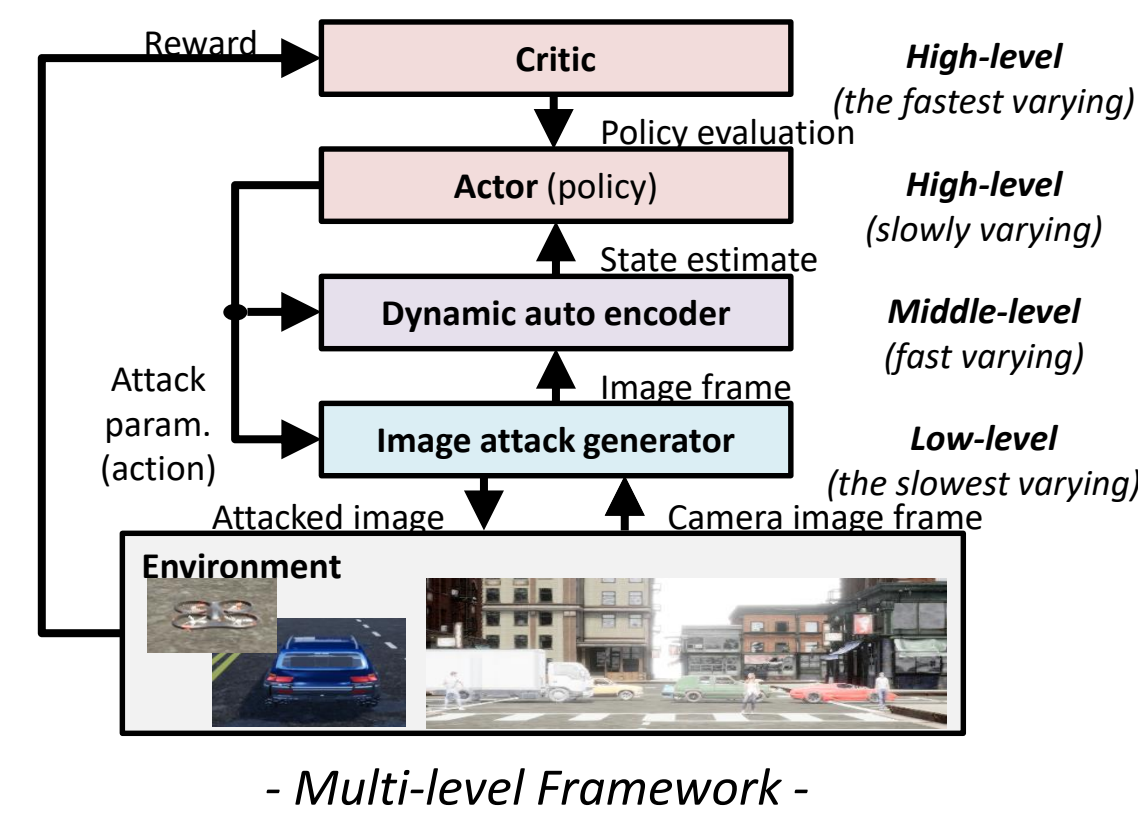
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Learning Image Attacks

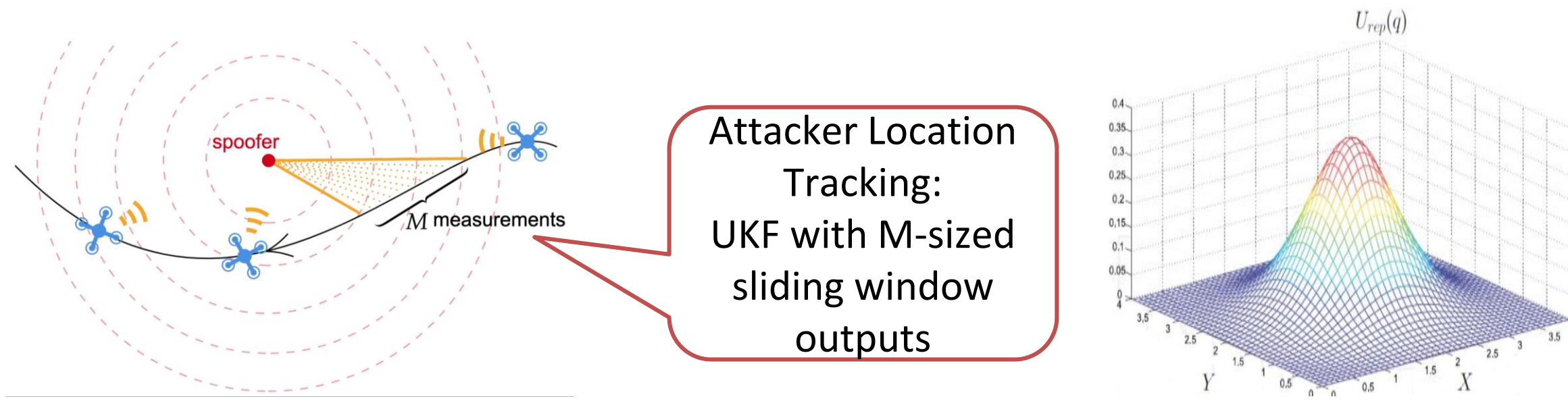
- Deep neural network perception module in autonomous vehicles are **vulnerable to adversarial attack**.
- Faster **online** recursive image attack with **state estimator** is needed for vision guided autonomous vehicles.



- Multi-level Framework -

Safety Constrained Control Framework

- To avoid intolerable sensor drifts for UAVs in GPS denied environment, the UAVs are desinged to adapt **at the planning level**.



Attacker Location Tracking: UKF with M-sized sliding window outputs

Time-delayed repulsive potential function

$$\min_u \sum_{i=k}^{k+N} \hat{x}_{i+1}^T Q_i \hat{x}_{i+1} + u_i^T R_i u_i + \sum_{i=k^a+k^e}^{k+N} U_{rep}(D_i)$$

$$\text{s.t. } \hat{x}_{i+1} = A \hat{x}_i + B u_i$$

$$h(\hat{x}_i, u_i) \leq 0$$

$$\text{for } i = k, k+1, \dots, k+N,$$