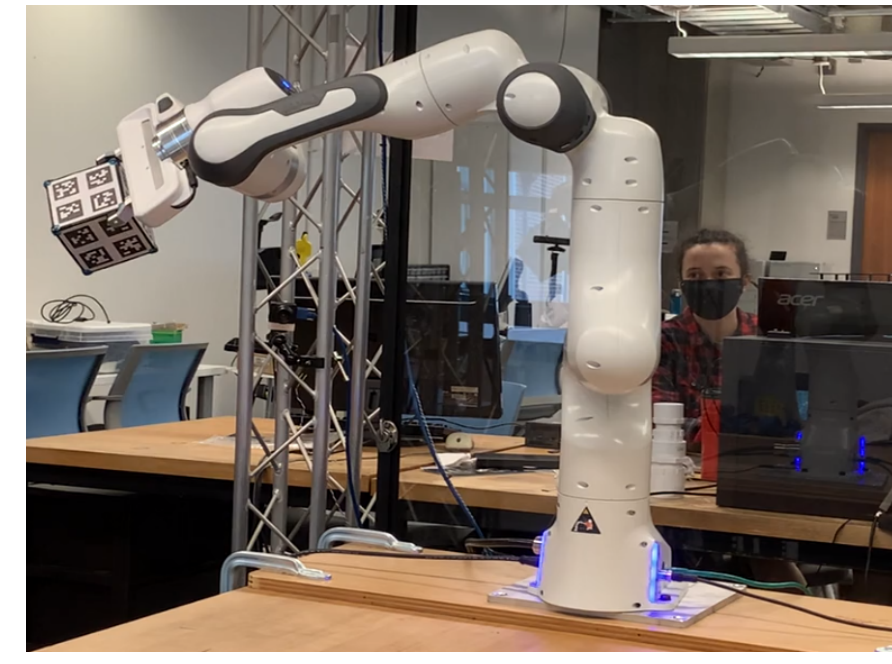


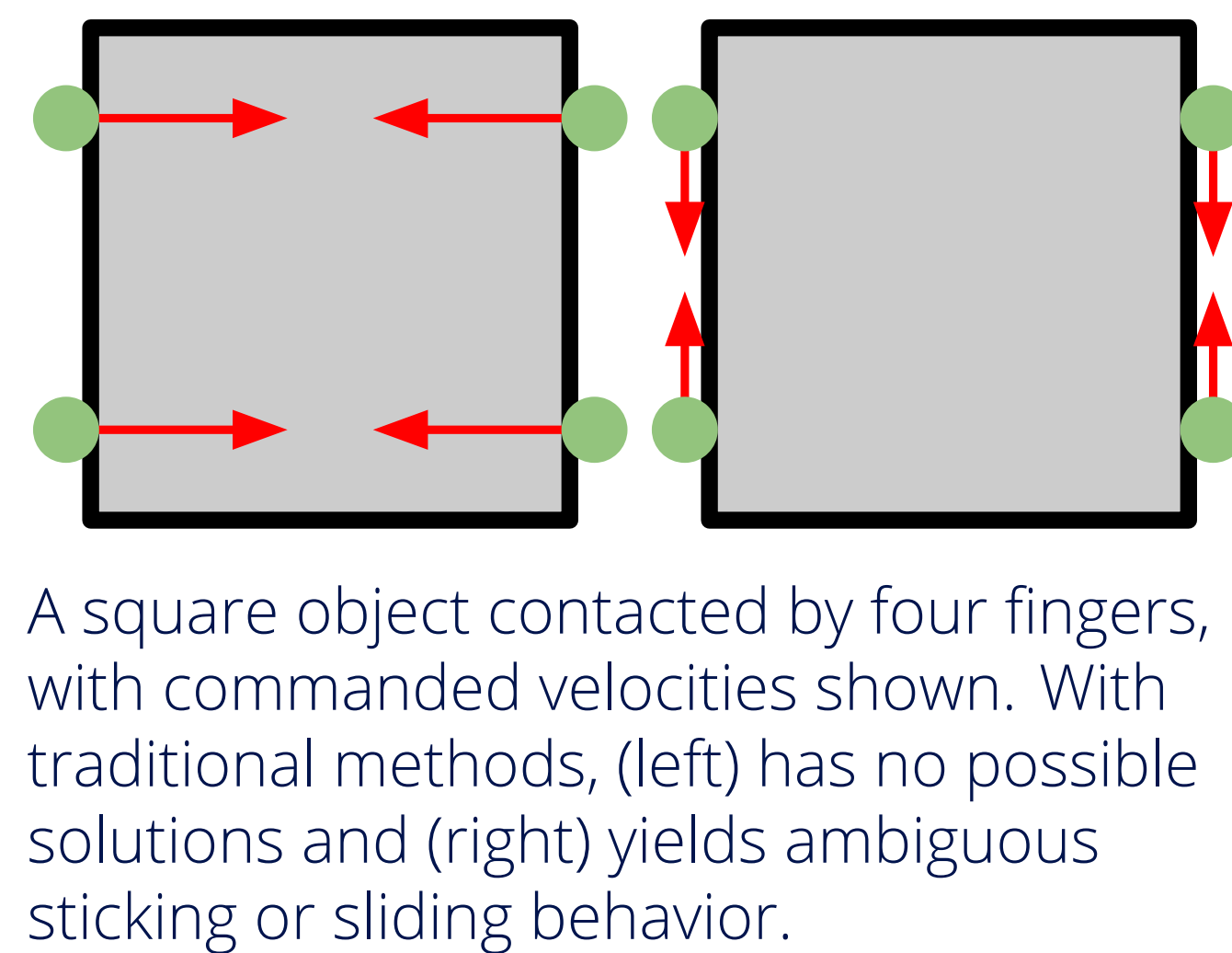
## INTRODUCTION

- Frictional contact is the **fundamental behavior** of robot locomotion and manipulation.
- However, in uncertain environments, robots move slowly and cautiously, often avoiding, rather than embracing, contact.
- To enable complex, dynamic manipulation, this project made fundamental advances in **physics-based modeling and model learning**, with a focus on capturing the hybrid discontinuities that challenge standard methods.
- This project developed model-based control algorithms, leveraging tactile sensing for reactive feedback and 30 Hz, real-time planning that intelligently makes and breaks contact.



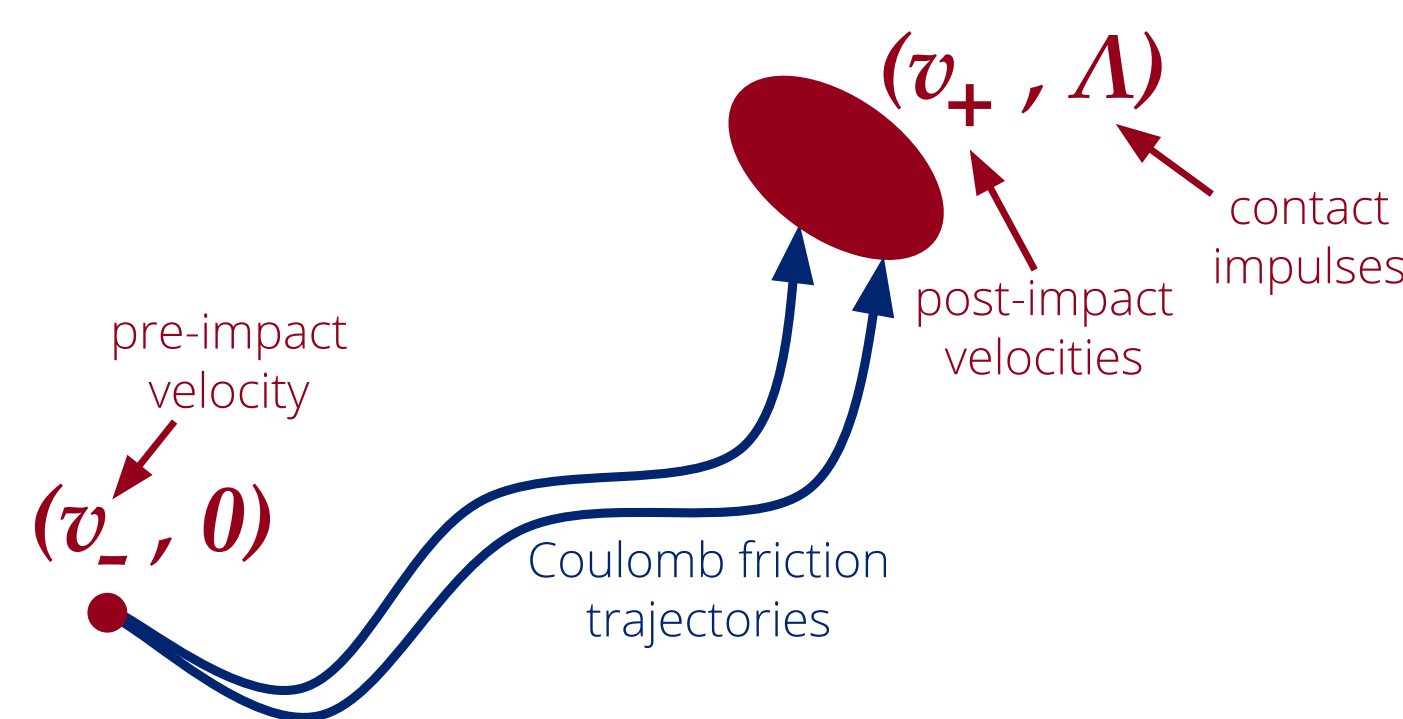
## QUASISTATIC MODELING [1]

Prior, quasistatic approaches are fundamentally unable to capture grasping and jamming. We have developed a **comprehensive model for quasistatic manipulation**. By replacing pure velocity control with a more realistic force law, we derive a computationally efficient model for unification of pushing and grasping.

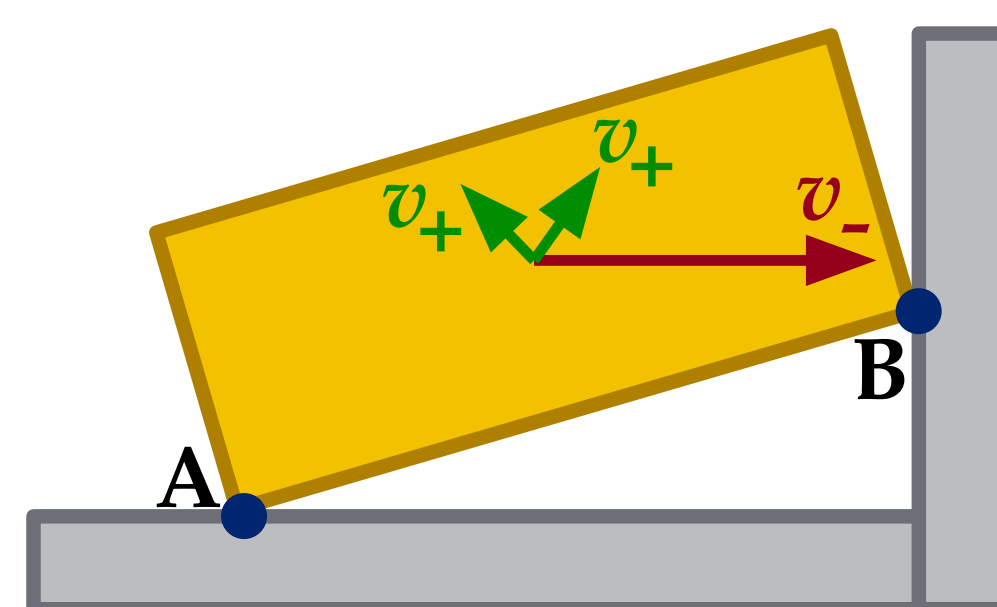


## SIMULTANEOUS CONTACT [2, 3]

- Simultaneous frictional impacts between rigid bodies are **pervasive, extremely sensitive, and poorly understood**.
- We developed a continuous-time rigid body model that for **set-valued simulation and reasoning over contact ambiguity**.
- The result is a **single differential inclusion**, with solution guarantees, that unifies continuous-time simulation and impact events.

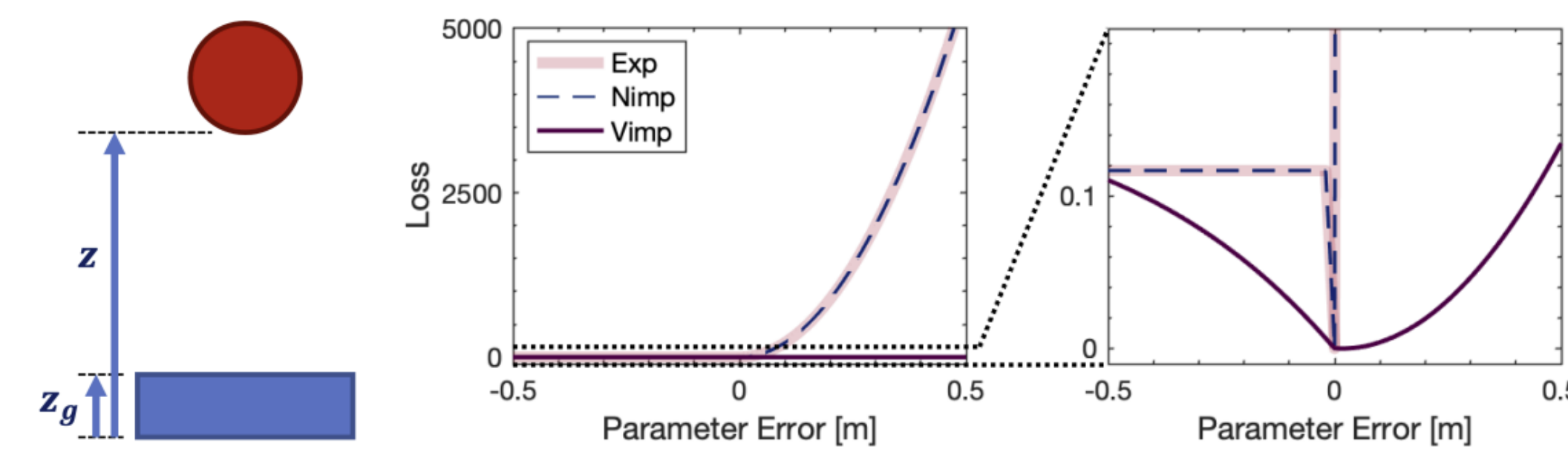


Non-uniqueness emerges even without simultaneous impact. A block sliding into a wall will have sensitive behaviors due to propagation of impact events.

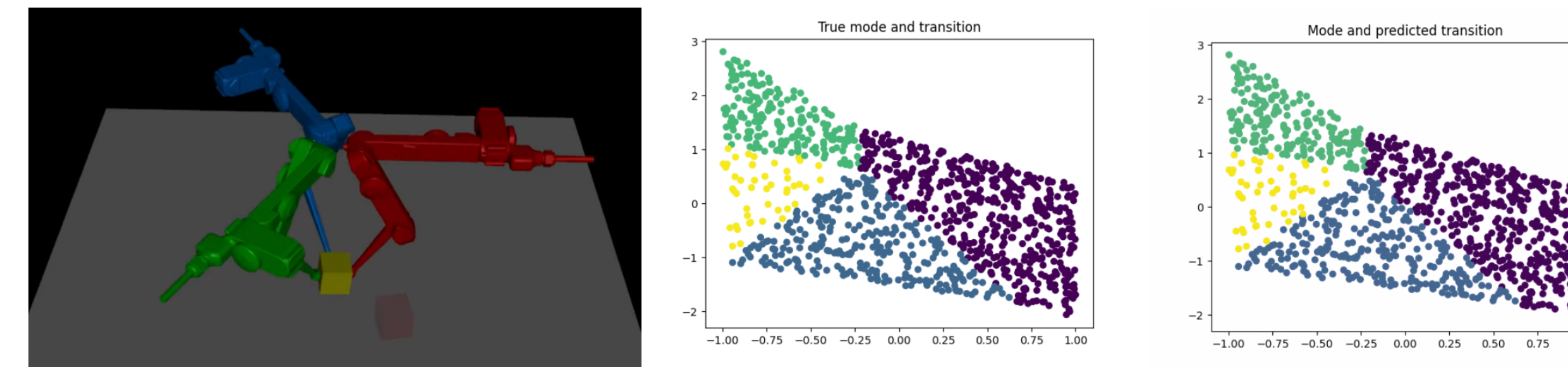


## LEARNING DISCONTINUITY [4, 5, 6]

- Standard ML biases toward continuity and simplicity, are fundamentally at odds with multi-contact robotics.
- Even for simple examples, like a bouncing ball, while our **intuitive understanding of the motion** is simple, the mapping  $x_k \rightarrow x_{k+1}$  is discontinuous at impact events.
- Smoothing** used in physics simulators artificially simplifies the problem, where empirical results show a direct correlation between stiffness (hard being more realistic) and learning error [6].
- Implicit learning**, leveraging complementarity structure, can dramatically reshape stiff optimization landscapes enabling learning to **provably generalize better** to unseen data [4].



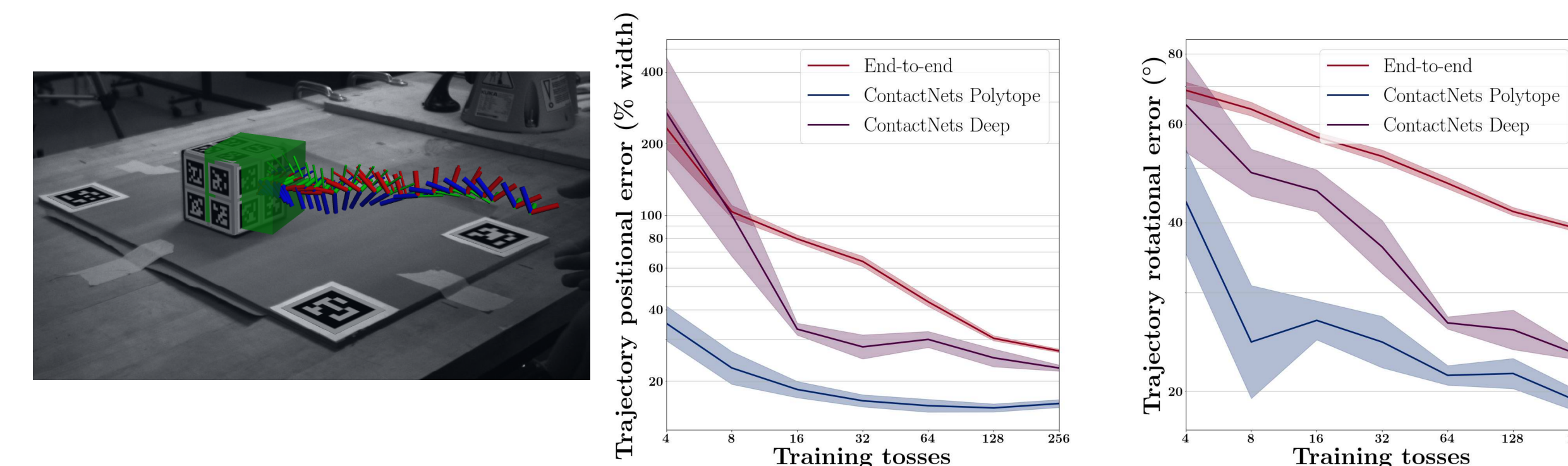
- These approaches scale to piecewise-affine systems with thousands of pieces and contact-rich manipulation [5].



## CONTACTNETS [7]

**ContactNets** learns discontinuous physics without introducing artificial smoothing.

- A physics-inspired representation, generalizing geometry and friction with neural networks, is a **smooth encoding of discontinuity**.
- Direct simulation of candidate models leads to poorly conditioned training. Via **bilevel optimization**, we **hypothesize** potential forces that must simultaneously correspond to a candidate model and match observed data.



Using motion capture, we toss a cube against the ground and record its rolling, bouncing, and sliding trajectories. While standard DNNs struggle to learn from limited data, ContactNets variations are able to rapidly segment the discontinuous modes and achieve highly accurate trajectory rollouts with only seconds of data.

## CONTACT-AWARE CONTROL SYNTHESIS [8, 9, 10, 11]

The challenge in contact-rich manipulation lies in the discontinuous dynamics, due to frictional forces and impacts. Model dynamics as a Linear Complementarity System (LCS)

$$\begin{aligned} \dot{x} &= Ax + Bu + C\lambda, \\ 0 &\leq \lambda \perp Dx \geq 0. \end{aligned}$$

Two algorithms:

- Lyapunov stable** control policies  $u = Kx + L\lambda$  that leverage tactile feedback. Synthesize by solving a **bilinear matrix inequality**
- Consensus Complementarity Control (C3)**: real-time MPC that explores potential contact sequences. Consensus ADMM formulation that leverages complementarity structure.

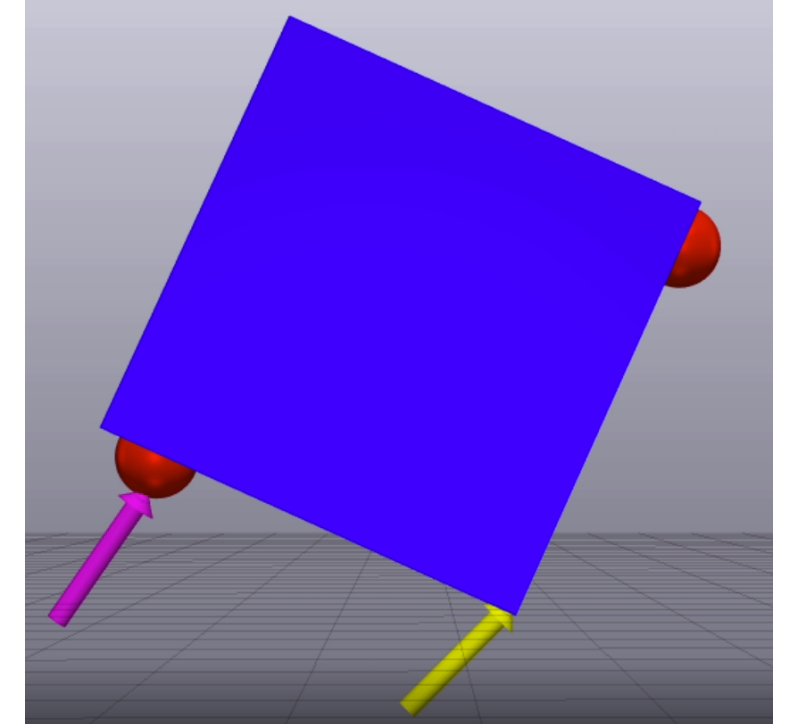
## EXAMPLE: CART-POLE WITH SOFT WALLS

- The pole impacts two foam walls, often at high speeds.
- Linearization cannot reason about the walls, but LCS controllers can.
- C3 and reactive tactile feedback stabilize the physical system.



## EXAMPLE: TWO-FINGER MANIPULATION

Two fingers (red) move across and manipulate a planar object (blue), where the object can also touch the ground. Normal and frictional forces are shown as arrows. C3 generates manipulation plans, reasoning about stick-slip transitions at three contact points. With a planning horizon of 10 steps, the controller runs at over 30 Hz.



- Mathew Halm and Michael Posa. A Quasi-static Model and Simulation Approach for Pushing, Grasping, and Jamming. In *The Workshop on the Algorithmic Foundations of Robotics (WAFR)*, Merida, Mexico, 2018.
- Mathew Halm and Michael Posa. Modeling and Analysis of Non-unique Behaviors in Multiple Frictional Impacts. In *Robotics: Science and Systems (RSS)*, Freiburg im Breisgau, Germany, 2019.
- Mathew Halm and Michael Posa. Set-valued rigid body dynamics for simultaneous frictional impact. *arXiv preprint arXiv:2103.15714*, apr 2021.
- Bibit Bianchini, Mathew Halm, Nikolai Matni, and Michael Posa. Generalization Bounded Implicit Learning of Nearly Discontinuous Functions. *Accepted to the 4th Annual Learning for Dynamics and Control Conference (L4DC)*, dec 2022.
- Wanxin Jin, Alp Aydinoglu, Mathew Halm, and Michael Posa. Learning Linear Complementarity Systems. *Accepted to the 4th Annual Learning for Dynamics and Control Conference (L4DC)*, dec 2022.
- Mihir Parmar\*, Mathew Halm\*, and Michael Posa. Fundamental Challenges in Deep Learning for Stiff Contact Dynamics. In *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, mar 2021.
- Samuel Pfrommer\*, Mathew Halm\*, and Michael Posa. ContactNets: Learning of Discontinuous Contact Dynamics with Smooth, Implicit Representations. In *The Conference on Robot Learning (CoRL)*, 2020.
- Alp Aydinoglu, V.M. Victor Preciado, and Michael Posa. Contact-Aware Controller Design for Complementarity Systems. In *IEEE International Conference on Robotics and Automation (ICRA)*, Paris, France, 2020.
- Alp Aydinoglu, Fazlyab Mahyar, Manfred Morari, and Michael Posa. Stability analysis of complementarity systems with neural network controllers. In *Proceedings of the 16th International Conference on Hybrid Systems: Computation and Control (HSCC)*, 2021.
- Alp Aydinoglu, Philip Sieg, Victor Preciado, and Michael Posa. Stabilization of complementarity systems via contact-aware controllers. *IEEE Transactions on Robotics (TRO)*, 2021.
- Alp Aydinoglu and Michael Posa. Real-Time Multi-Contact Model Predictive Control via ADMM. *Accepted to the IEEE International Conference on Robotics and Automation (ICRA)*, sep 2022.