## NSF:CPS:1035658, Exploratory Research: Safety-Oriented Hybrid Verification of Medical Robotics

Matthew Might, Ganesh Gopalakrishnan, John Hollerbach, Dennis Parker University of Utah: School of Computing and Department of Radiology

**Motivation and goal** The whole-system design and modeling of complex medical robotics involves analog sensors and actuators; discrete software controllers; piecewise, non-linear, discontinuous biological tissues/media; and probabilistic human administrators.

In the best case, the failure of such systems risks limb. In the worst, life.

*The goal of our project is to explore and investigate paradigms for the whole-system design, modeling and formal verification of cyber-physical-biological systems.* 

**Motivating application** To ground this project in practice, the motivating application is MRgHIFU: an MR-guided robotic surgeon wielding a high-frequency ultrasound as a scalpel for noninvasive surgical ablation of cancerous tissue. We selected this system because (1) it has clear humanitarian broader impacts, (2) it has demanding clinical safety requirements acting as a barrier to formal approval and clinical adoption, and (3) modeling and verification of the system and those requirements requires a complex synthesis of components with nonlinear behavior.

**Research objectives** Our specific research objective is the exploration and investigation of paradigms for the whole-system design, modeling and verification of cyber-physical-biological systems.

**Scientific directions** We are developing and investigating flow-driven-transducer networks as a paradigm for the design and modeling of cyber-physical-biological systems. Such networks formally model heterogenous systems with discrete, continuous and probabilistic components. Specific approaches being investigated include hybrid and timed automata, abstract-interpretive inference thereof and model-checking techniques for non-linear differential equations.

**Techniques and findings** Findings to date include (1) a prototype core calculus for MATLAB— $\lambda_M$ —to support analysis and modeling of high-level controllers; (2) a formal framework for flow-driven transducer networks; (3) abstract interpretive methods for hybrid specification synthesis; (4) probabilistic automata to model healthcare workers; and (5) characterizations of safety and liveness for cyber-physical-biological systems.

**Keywords** MRgHIFU, medical robotics, tumor ablation, hybrid systems, flow networks, model-checking, abstract interpretation, hybrid automata, formal verification