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The rapid growth of e-commerce demands has resulted in increased traffic of delivery trucks while slowing down the pace of delivery operations





Fly last-mile to the target position



The proposed delivery network is comprised of autonomous flying robots and existing transport **networks** (public and private ground vehicles).

Naira Hovakimyan





Srinivasa Salapaka



Wang

Lavanya

Marla



Marco

Pavone

Xiaofeng Wang

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MATTERNET

FLYTREX

DISCOVER

Wing"

zipline

Industrial players:

- ✓ Prime Time Air of Amazon
- ✓ FedEx
- ✓ UPS Flight Forward
- ✓ DHL Parcelcopter
- ✓ Wing
- ✓ Matternet
- ✓ Zipline
- ✓ Flytrex

Economic benefits (cost-benefit analysis per ARK Invest, 2015):

- ✓ Amazon's cost per package for delivery would be roughly 88 cents per parcel
- ✓ Market size: USD 860 million in 2021 (projected to reach USD 4,964 million by 2030)
- ✓ More than 2,000 drone deliveries are occurring each day worldwide

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A glimpse into the market

map:

- ✓ Drone-service providers
- ✓ Business internal services

□ Industry sectors:

- ✓ Retail
- ✓ Food
- ✓ Mechanical Supplies
- ✓ Industrial Materials

	Drone Service Providers (DSPs)				Business-Internal Services							
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Challenge Content

- Efficiency and Effectiveness: co-existing with traditional ground delivery system
- **Coordination and collaboration**: synergistic drone and ground networks in the last-mile delivery in populated urban areas
- Human-machine interaction: people's safety and comfort with drones flying around

Scientific Impact

- Efficient package flow and network design
- Safe and robust robot motion execution
- Socially accommodative robot motion planning

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Broader Impact

- New discoveries on drone networks interfacing with people
- New solutions to the supply chain
- Improvement to transportation networks
- New applications of wireless sensor networks

Impact on society

- A step forward for incorporating drones into daily life.
- More efficient logistics for better e-commerce experience.
- Less congested traffic in urban transportation

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A Simulator for Integration of Drone Delivery Technologies (Hovakimyan group)

ROS/Gazebo based simulator for drone delivery

- Popular simulation environment with rich programming package support
- Ample resources for multi-modal vehicles and sensors
- Rich interfaces to incorporate new technologies and future development





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A Novel Index of Human Safety Perception (Collaboration: Hovakimyan and R. Wang)











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Award ID#: 1830639 September 7, 2018





Quantify defensive response **as peak head acceleration:** within a time window before time-of-contact

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Motion planning with human safety perception (Collaboration: Hovakimyan and R. Wang)



H. Yoon, C. Widdowson, T. Marinho, R. F. Wang and N. Hovakimyan, "A Path Planning Framework for a Flying Robot in Close Proximity of Humans," 2019 American Control Conference (ACC), 2019, pp. 5254-5259.



- Observation:
- Camera image
- Physiological sensor
- IMU

Hidden state:

- User's guess on the path
- User intention
- Emotional state

Reinforcement Learning (online) under incomplete state observation



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Risk-sensitive Rendezvous (Hovakimyan group)



A computationally tractable algorithm for **risk-aware rendezvous planning**

- Planning over multiple possible paths;
- Sampling based method relying on cross-entropy information updates.

G. Haberfeld, A. Gahlawat, and N. Hovakimyan, "Risk-Sensitive Rendezvous Algorithm for Heterogeneous Agents in Urban Environments." 2021 American Control Conference (ACC). 2021



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Uncertainty Quantification for Trajectory Optimization (Marla group)



- Drones in urban areas are subject to high degree of wind uncertainty
- Winds are dynamic and non-stationary
- Use drones as sensors to collect wind/weather information along their paths

Offline and online policies for exploring the airspace:

- Offline: design a set of times and trajectories using a nested partition structure with minimum regret;
- Online: design trajectories based on package deliveries with lowest expected cost

Use data from Bureau of Transportation Statistics and airline schedules in the National Airspace System

• Flight times and fuel burn can be **reduced** by 5% on average using our policies

J. Gao, A. Mani, L. Marla, "Sensing in Airspace for Sequential O-D Aircraft Routing", under review at Operations Research.



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$C\mathcal{L}_1$ - \mathcal{GP} : Contraction \mathcal{L}_1 with Bayesian Learning (Hovakimyan group)

- Safety certificates in the form of tubes from the CL₁- GP framework which enables safety during learning
- Natural framework for learning using \mathcal{GP} :
 - guaranteed performance during the learning transients
 - improved performance of the L₁ adaptive controller,
 i.e., smaller tubes
 - improved quality of the planned trajectory





A. Gahlawat, A. Lakshmanan, L. Song, A. Patterson, Z. Wu, N. Hovakimyan, E. Theodorou, "Contraction L1-Adaptive Control using Gaussian Processes," In Proceedings of 3rd Learning for Dynamics and Control Conference, 2021



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Performance improvement with safety guarantees (Hovakimyan group)



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Robust CCM: Tube-Certified Trajectory Tracking (Collaboration: Hovakimyan and Pavone)

- The controller and state tubes are jointly optimized through solving convex optimization problems involving statedependent linear matrix inequalities (LMIs)¹
- The resulting controller has **explicit disturbance rejection** property
- It provides certificate tubes for both states and control inputs in a unified way
- Under certain assumptions, it proves to yield tighter state tubes than the CCM-based approach², which
 - first designs a controller for the **nominal** system, and
 - then derives the tube for the disturbed system using input-to-state stability analysis



1 Zhao, Lakshmanan, Ackerman, Gahlawat, Pavone, Hovakimyan. *Tube-Certified Trajectory Tracking for Nonlinear Systems with Robust Control Contraction Metrics*. IEEE RA-L, 2022. 2 Singh, Landry, Majumdar, Slotine, Pavone. *Robust Feedback Motion Planning via Contraction Theory*, IJRR, 2019.



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An efficient and scalable framework for multi-drone delivery (Pavone group)



- Assigning drone routes to deliver packages while avoiding conflicts between drones;
- Striving to **minimize the overall delivery time** of all the packages in the system;
- Utilizing **public transit network** over large urban areas.



S. Choudhury, K. Solovey, M. Kochenderfer and M. Pavone, "Efficient Large-Scale Multi-Drone Delivery Using Transit Networks," ICRA 2020: 4543-4550.

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Solution: two-stage algorithmic approach with theoretical guarantees (Pavone group)

We decompose the problem into **task allocation** and **routing for multiple drones** to deliver multiple packages to minimize make span.



S. Choudhury, K. Solovey, M. Kochenderfer and M. Pavone, "Efficient Large-Scale Multi-Drone Delivery Using Transit Networks," ICRA 2020: 4543-4550.



- Our approach quickly solves scenarios with up to hundreds of drones delivering thousands of packages over large urban areas.
- By allowing drones to utilize existing public transit infrastructure, drones can increase their effective delivery range by **at least x2.5**



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Simultaneous Facility and Path Optimization (Salapaka group)



A framework for **simultaneously** solving facility location and path optimization

- Considering **both static and dynamic** spatial networks;
- A novel **stage-wise viewpoint** of the paths to design the decision variable space;
- Optimization via maximum entropy principle.



Pick-Up/Drop-Off Depot LMDP Network Design for the City of Urbana-Champaign

- Apartment street address from CU city website.
- **Google API** to obtain latitude-longitude co-ordinates of the apartment.
- Solving Parameterized Markov Decision Problem

Srivastava, Amber, and Srinivasa M. Salapaka. "Simultaneous Facility Location and Path Optimization in Static and Dynamic Networks." IEEE Transactions on Control of Network Systems 7.4 (2020): 1700-1711.

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Parameterized Sequential Decision-Making problems (Salapaka group)



$$\min_{\boldsymbol{\mu},\boldsymbol{\zeta},\boldsymbol{\eta}} J^{\boldsymbol{\mu}}_{\boldsymbol{\zeta}\boldsymbol{\eta}}(s) = \mathbb{E}_{p_{\boldsymbol{\mu}}} \left[\sum_{t=0}^{\infty} \alpha^{t} c \left(x_{t}(\boldsymbol{\zeta}), u_{t}(\boldsymbol{\eta}), x_{t+1}(\boldsymbol{\zeta}) \right) | x_{0} = s \right] = \sum_{\omega \in \Omega} p_{\boldsymbol{\mu}}(\omega | s) \ \bar{c}(s, \omega)$$

$$p_{\mu}: \omega \to [0,1] \text{ and } \omega = (a_0, x_1, a_1, x_2, \dots) - p_{\mu}(\omega|s) = \mu(a_0|s)p(x_1|a_0, s)\mu(a_1|x_1)p(x_2|x_1, a_1) \cdot$$

- state, action parameters: $\zeta = \{\zeta_s\}, \eta = \{\eta_a\}$
- cost and dynamics: c(s, a, s'), p(s'|s, a)

Generalized the approach to **Parameterized Sequential Decision-Making problems**

- Maximum entropy principled based framework
- Routing + Resource allocation on a common platform
- Models many combinatorial optimization problems (e.g., network design, planning, supply chain, scheduling, Markov decision processes, reinforcement learning, model predictive control)

Srivastava, Amber, and Srinivasa M. Salapaka. "Parameterized MDPs and Reinforcement Learning Problems--A Maximum Entropy Principle Based Framework." arXiv preprint, arXiv:2006.09646 (2020).



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Education and Outreach (Hovakimyan, X. Wang)

Senior undergraduate design projects



Autonomous drone landing on a non-cooperative ground vehicle



Outreach

PI Hovakimyan's visit to Montessori school of C-U to showcase robotics to elementary-age students.



Students and postdocs funded									
	Completed	Ongoing	Total						
Postdoc	4	2	6						
PhD	12	5	17						
Master	3	4	7						
Undergraduate	17	5	22						

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Safe Control Identify Prioritize Build Human's Psychology With Mobility Service Safety Perception **Experiments** Guarantees System Requests Model Design Solve Optimal Safe Feedback Socially-Aware Safe Delivery Scheduling **Motion** Motion Rendezvous Network Policy Planning Planning Commodity (Package) Flow Safe and Robust Socially-Accommodative **Problem and Network Design** Motion Execution **Cooperative Motion Planning** Algorithmic foundations: Lift abstractions of robustness to the Studying effects of greeting voice Hardness proofs sense of distributions on PSD Accounting for uncertainty • Tube certificates in the space of Female vs male voice Faster solvers . distributions Studying effects of social context Information-sharing across operators Deploy tube-based safety controllers Invoking the hidden Markov and drones to real vehicles model-based RL Extension to urban air mobility Stanford

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Conclusion and Future Work

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Incomplete list of publications

Conference Proceedings

- 1. H. J. Yoon, P. Zhao, C. Tao, C. Widdowson, R. F. Wang, N. Hovakimyan, and E. Theodorou, "Socially Aware Motion Planning for a Flying Robot with Model Predictive Path Integral Control," ICRA 2019 Workshop.
- 2. H. Yoon, C. Widdowson, T. Marinho, R. F. Wang and N. Hovakimyan, "A Path Planning Framework for a Flying Robot in Close Proximity of Humans," 2019 American Control Conference (ACC), 2019, pp. 5254-5259.
- 3. G. Haberfeld, A. Gahlawat, and N. Hovakimyan, "Risk-Sensitive Rendezvous Algorithm for Heterogeneous Agents in Urban Environments." 2021 American Control Conference (ACC), pp. 3455-3460, 2021.
- 4. G. Haberfeld, A. Gahlawat, and N. Hovakimyan, "Safe Sampling-Based Air-Ground Rendezvous Algorithm for Dense Street Maps." 2021 International Conference on Unmanned Aircraft Systems (ICUAS), pp. 413-422, 2021.
- 5. A. Gahlawat, A. Lakshmanan, L. Song, A. Patterson, Z. Wu, N. Hovakimyan, E. Theodorou, "Contraction L1-Adaptive Control using Gaussian Processes," In Proceedings of 3rd Learning for Dynamics and Control Conference, 2021
- 6. S. Choudhury, K. Solovey, M. Kochenderfer, M. Pavone, "Efficient Large-Scale Multi-Drone Delivery Using Transit Networks," In Proceedings of the International Conference on Robotics and Automation (ICRA), pp. 4543-4550, 2020.
- 7. R. Sinha, J. Harrison, S. Richards, M. Pavone, "Adaptive Robust Model Predictive Control with Matched and Unmatched Uncertainty," Accepted for presentation at American Control Conference, 2022.
- 8. P. Zhao, Y. Mao, C. Tao, N. Hovakimyan, X. Wang, "Robust Adaptive Quadratic Programs using Control Lyapunov and Barrier Functions." IEEE Conference on Decision and Control, 2020
- 9. R. Abdelfattah, X. Wang, S. Wang, "TTPLA: An Aerial-Image Dataset for Detection and Segmentation of Transmission Towers and Power Lines." Asian Conference on Computer Vision (ACCV), 2020.
- 10. L. Yang, S. Dauchert, X. Wang, "A Framework for Predictive Control of Sampled-Data Systems Using Sporadic Model Approximation," American Control Conference, 2021

Journal Publications

- 1. J. Gao, A. Mani, L. Marla, "Sensing in Airspace for Sequential O-D Aircraft Routing", under review at Operations Research.
- 2. P. Zhao, A. Lakshmanan, K. Ackerman, A. Gahlawat, M. Pavone, N. Hovakimyan. "Tube-Certified Trajectory Tracking for Nonlinear Systems with Robust Control Contraction Metrics". Accepted for publication by IEEE Robotics and Automation Letters (RA-L), 2022.
- 3. S. Choudhury, K. Solovey, M. Kochenderfer, M. Pavone, "Efficient Large-Scale Multi-Drone Delivery Using Transit Networks," Journal of Artificial Intelligence Research, 2021.
- 4. S. Choudhury, K. Solovey, M. Kochenderfer, M. Pavone, "Coordinated Multi-Agent Pathfinding for Drones and Trucks over Road Networks", Autonomous Agents and Multiagent Systems, 2022
- 5. A. Srivastava, S. Salapaka. "Parameterized MDPs and Reinforcement Learning Problems--A Maximum Entropy Principle-Based Framework". IEEE Transactions on Cybernetics, 2021.
- 6. A. Srivastava, S. Salapaka. "Simultaneous Facility Location and Path Optimization in Static and Dynamic Networks." IEEE Transactions on Control of Network Systems, 2020.
- 7. J. Tao, L. Yang, Z. Wu, X. Wang, H. Su. "Lebesgue-Approximation Model Predictive Control of Nonlinear Sampled-Data Systems. IEEE Transactions on Automatic Control. 65 (10) pp. 4047-4060, 2020.
- 8. J. Tao, C. Wei, J. Wu, X. Wang, P. Shi, "Nonfragile Observer-Based Control for Markovian Jump Systems Subject to Asynchronous Modes." IEEE Transactions on Systems, Man, and Cybernetics: Systems. Pp. 1-8, 2019
- 9. W. Yan, B. Zhang, G. Zhao, S. Tang, G. Niu, X. Wang, "Battery Management System with Lebesgue Sampling-Based Extended Kalman Filter," IEEE Transactions on Industrial Electronics, vol. 66, no. 4, 3227-3236, 2019.
- 10. J. Tao, Z. Xiao, Z. Li, J. Wu, R. Lu, P. Shi, X. Wang, "Dynamic Event-Triggered State Estimation for Markov Jump Neural Networks With Partially Unknown Probabilities," IEEE Transactions on Neural Networks and Learning Systems, DOI: 10.1109/TNNLS.2021.3085001, 2021.