# Optimal Design of Robust Compliant Actuators for Ubiquitous Co-Robots



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# **Key problems to address:**

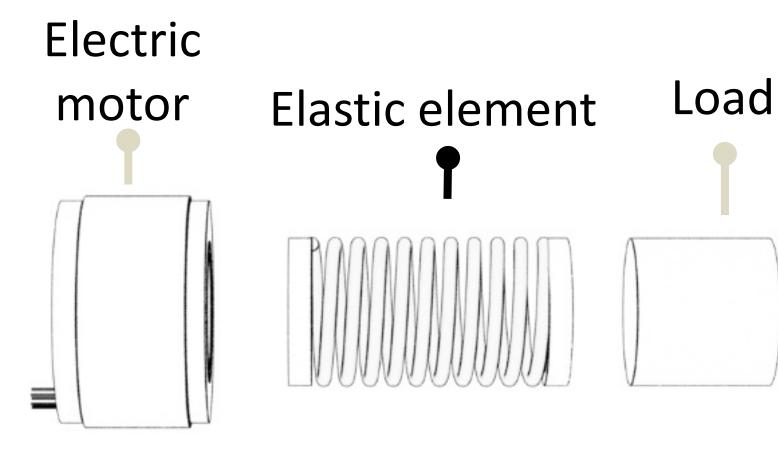
Framework for nonlinear springs acknowledging uncertainty

Achieve global solutions in polynomial-time

Solution independent of initial conditions

Avoid overdesign or underdesign resulting from safety factors

**Challenge:** Use series elasticity to minimize energy consumption and satisfy actuator constraints despite uncertainty



Series Elastic Actuator (SEA)

### **Scientific Impact:**

Formulate spring design of SEAs as a convex program

Framework to guarantee performance in uncertain environments

Bridge robust optimization and mechatronic design

# **Robust Convex Optimization Program**

Motor energy consumption (x: Spring compliance vector)

minimize  $\frac{1}{2}x^TQx + q^Tx + c$ subject to  $Ax \le b, \forall A, b \in \mathcal{U}$ 

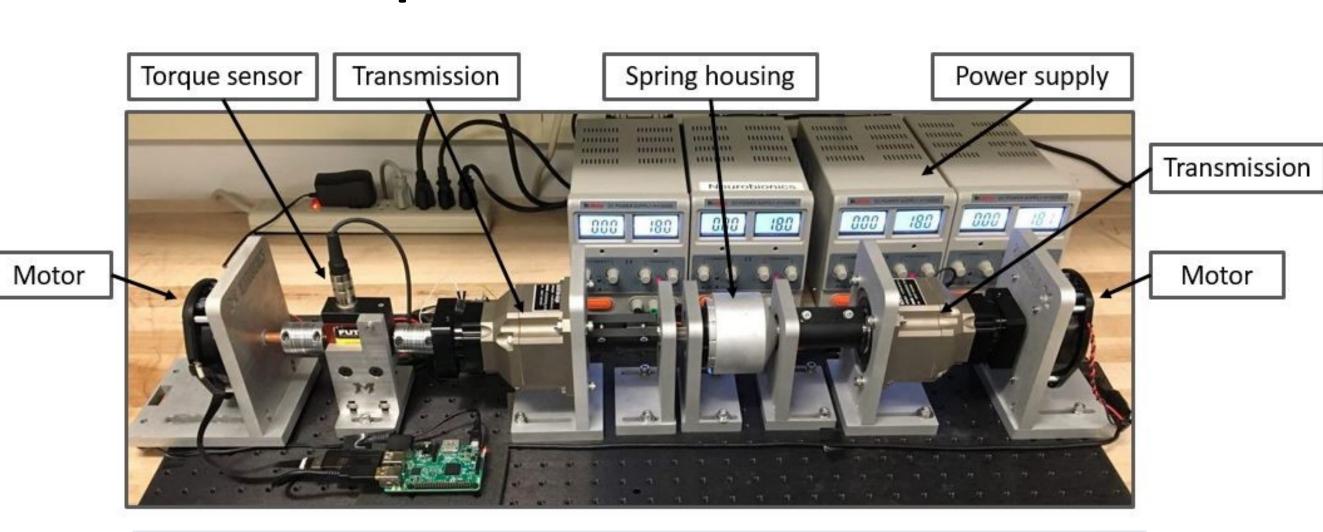
# Constraints

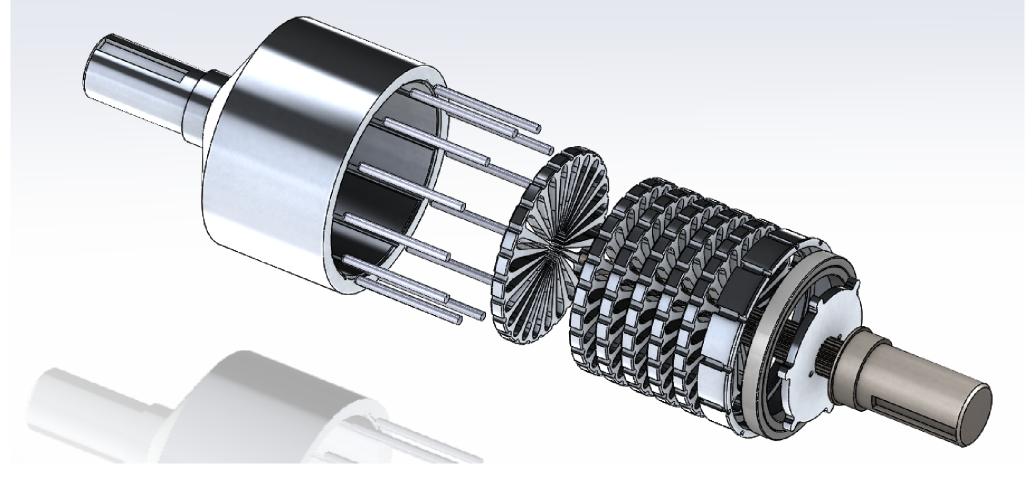
Motor torque Motor velocity Spring elongation

### Uncertainty

Load kinematics
Load kinetics
Unmodeled dynamics
Spring manufacturing

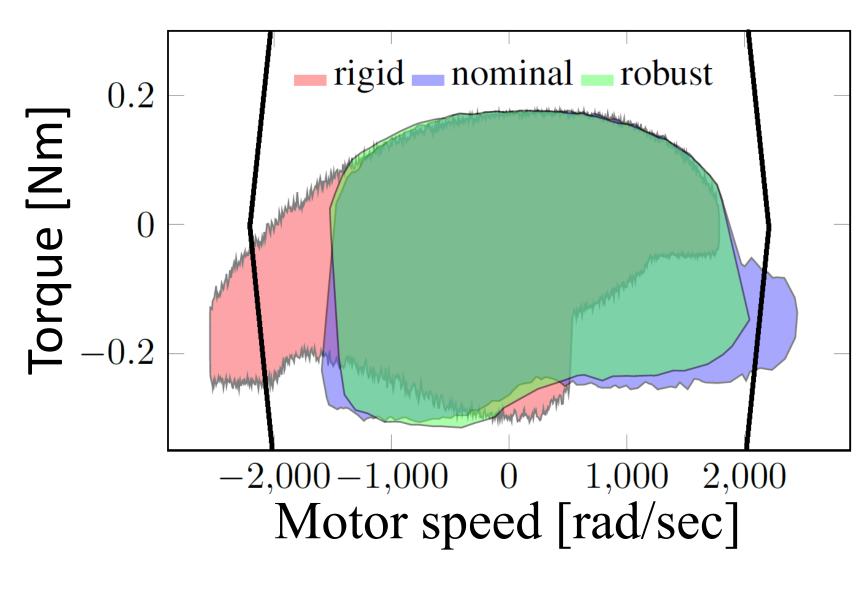
#### **Experimental Testbed**



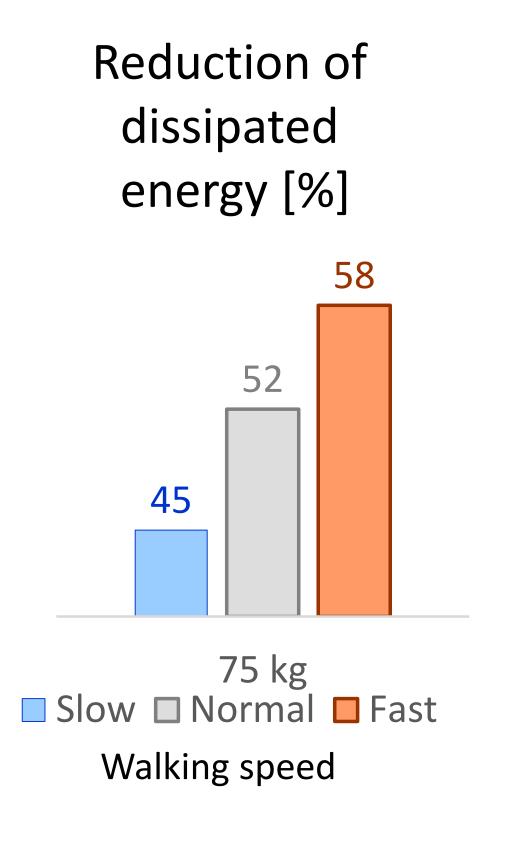


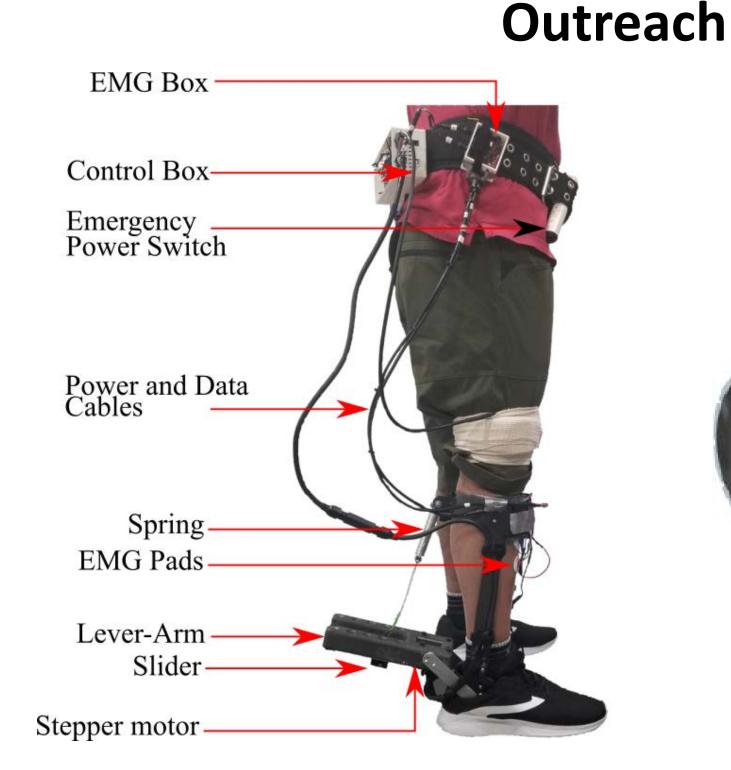
Rotational Springs can connect in parallel to modify stiffness

#### **Simulation Results**

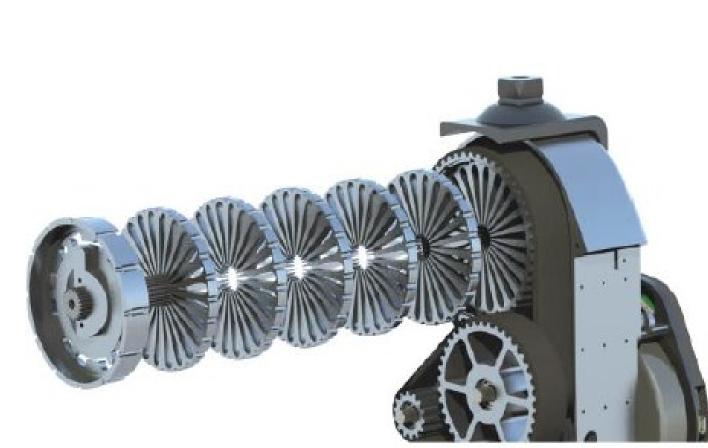


Simulation results: SEA for a powered prosthetic ankle. Not too rigid, not too soft to guarantee actuator constraints. (Nominal: 217.4 N·m/rad, Robust: 243.4 N·m/rad)





Senior design project – UT Dallas



Open Source Leg – U. Michigan





