

# Powered Prostheses: Minimizing Multi-Activity Motor Torque Through Parallel Elasticity and Convex Optimization

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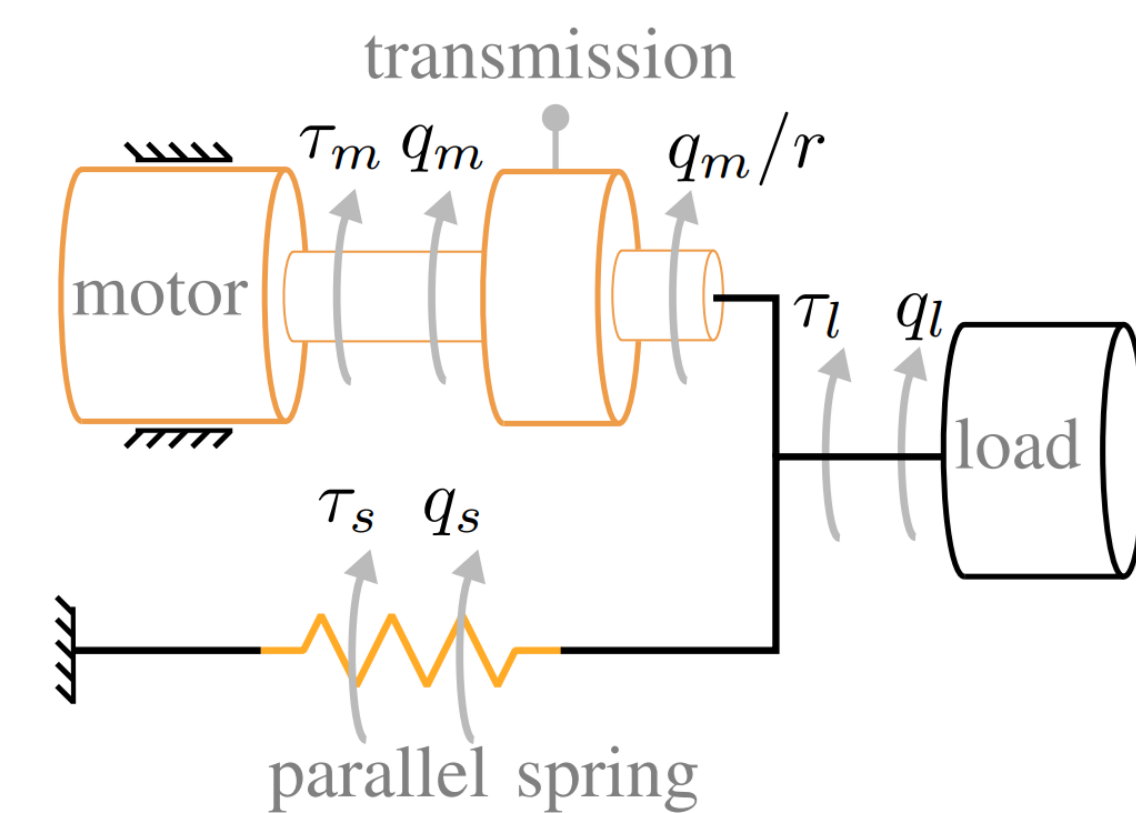
## Challenge: Multi-activity Torque-reducing PEA Design

Popular design methods focus on minimizing energy/torque of a single activity, which causes the spring to increase torque during other activities.

Linear elastic element

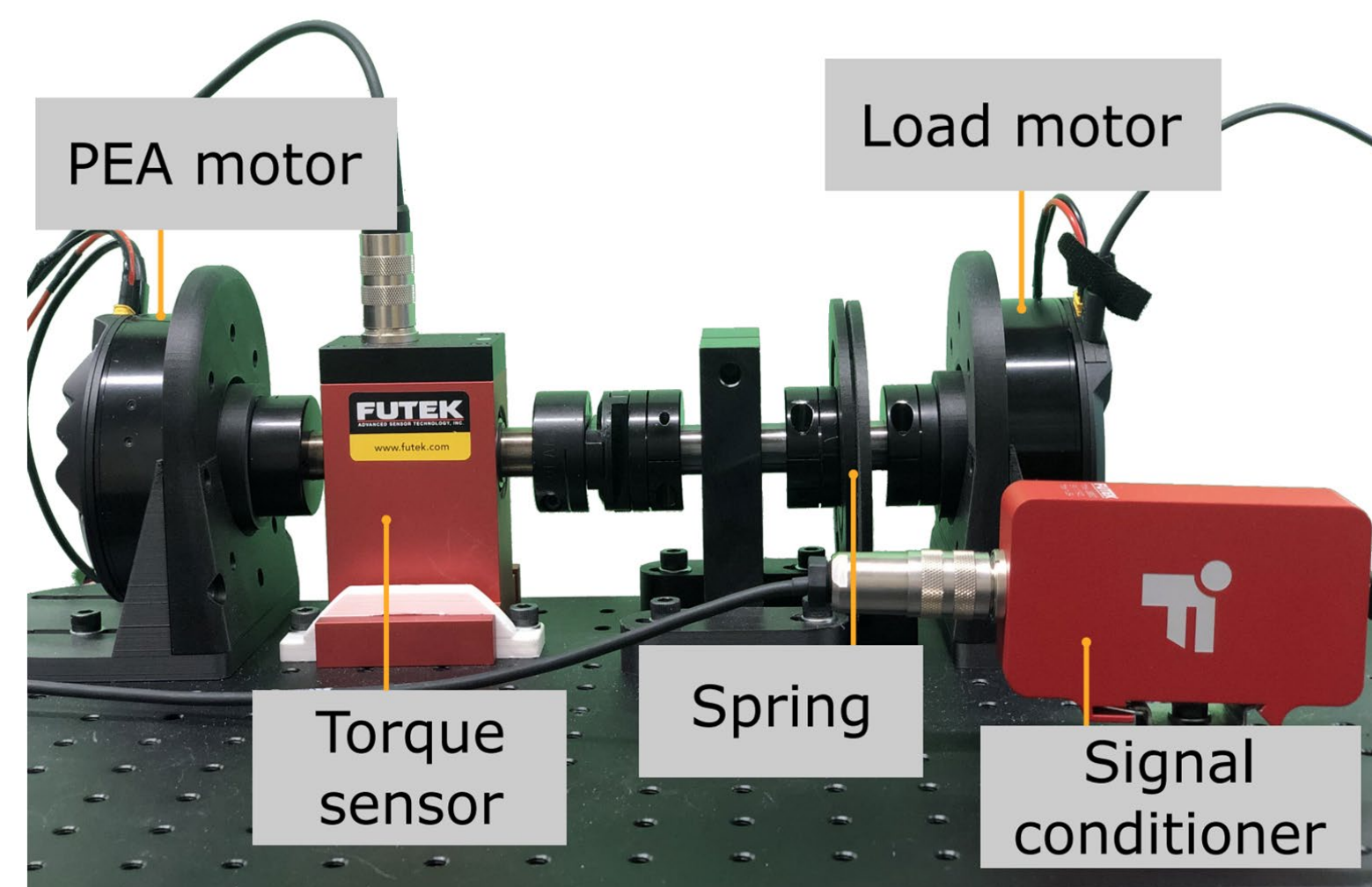
$$\tau_s = kq_s$$

Motor torque is an **affine function** of optimization variables (i.e. spring stiffness and preload torque)

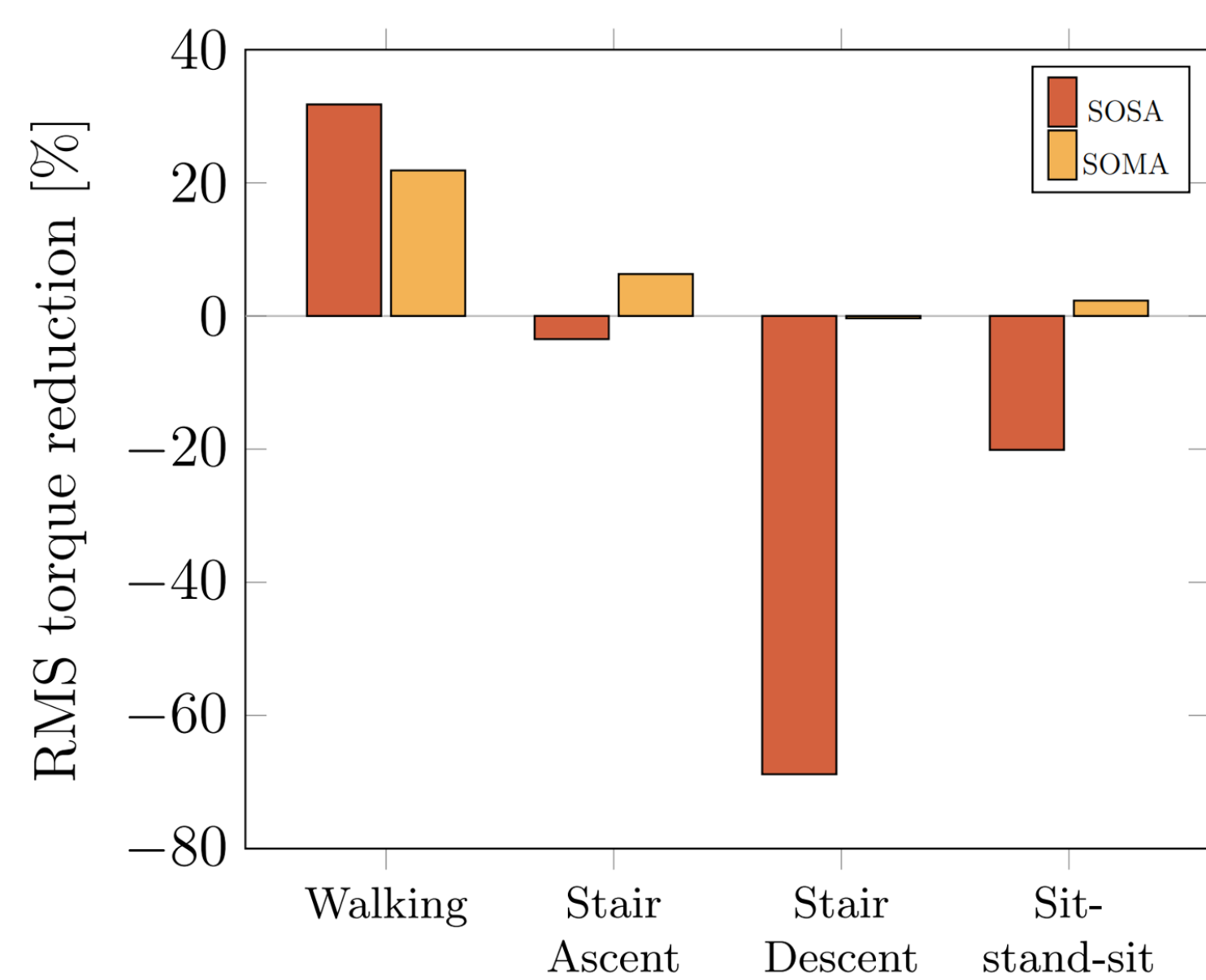


$$\tau_m = \tau_c - \frac{1}{r}(-kq_s + 1\tau_p)$$

$$\tau_c = I_m \ddot{q}_m + b_m \dot{q}_m + \mu \text{sign}(\dot{q}_m) - \frac{\tau_l}{r}$$



Dynamometer to simulate a prosthetic ankle



Spring optimized for a single activity (SOSA) vs. spring optimized for multiple activities (SOMA)

## Solution: A Globally Optimal Design for Multiple Activities

Key features:

- RMS torque reduction for **multiple tasks**.
- Convex optimization framework.
- Solutions computed within **polynomial time**.

Single activity:

$$\min_{k, \tau_p} \|\tau_m\|_2, \quad \text{s.t. } k > 0$$

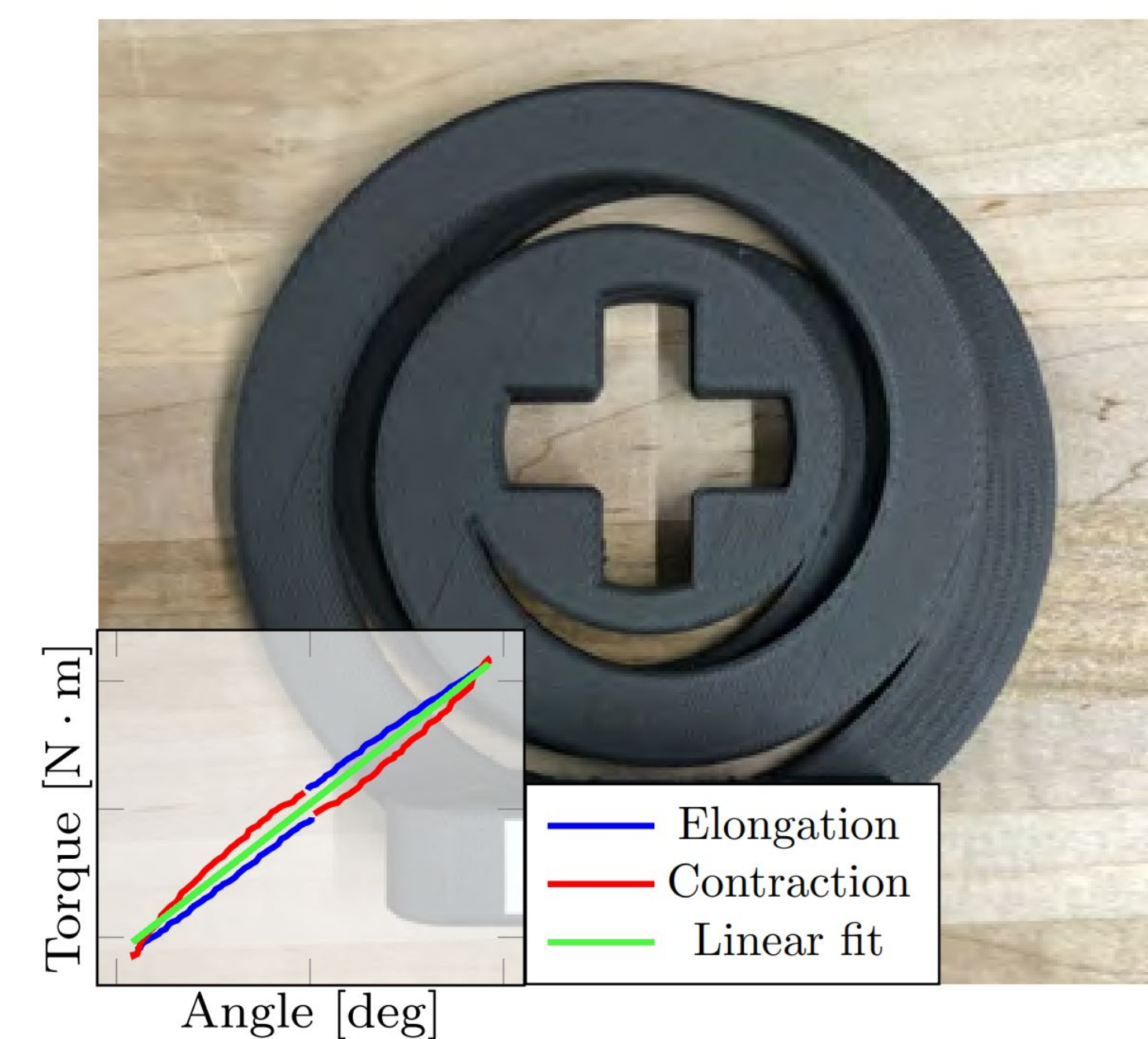
Multiple Activities:

$$\min_{k, \tau_p} \|\tau_{m,1}\|_2, \quad \text{s.t. } k > 0$$

$$\|\tau_{m,2}\|_2 \leq \|\tau_{c,2}\|_2$$

$$\vdots$$

$$\|\tau_{m,x}\|_2 \leq \|\tau_{c,x}\|_2$$



Spring optimized for

**single activity** 5.02 N · m/rad  
**multiple activity** 3.28 N · m/rad

Scientific Impact:

- Parallel elastic actuators reduce motor torque for multiple tasks
- Convex optimization framework
- Torque-oriented design paradigm contrary to the traditional energy-oriented approach

Societal Impact:

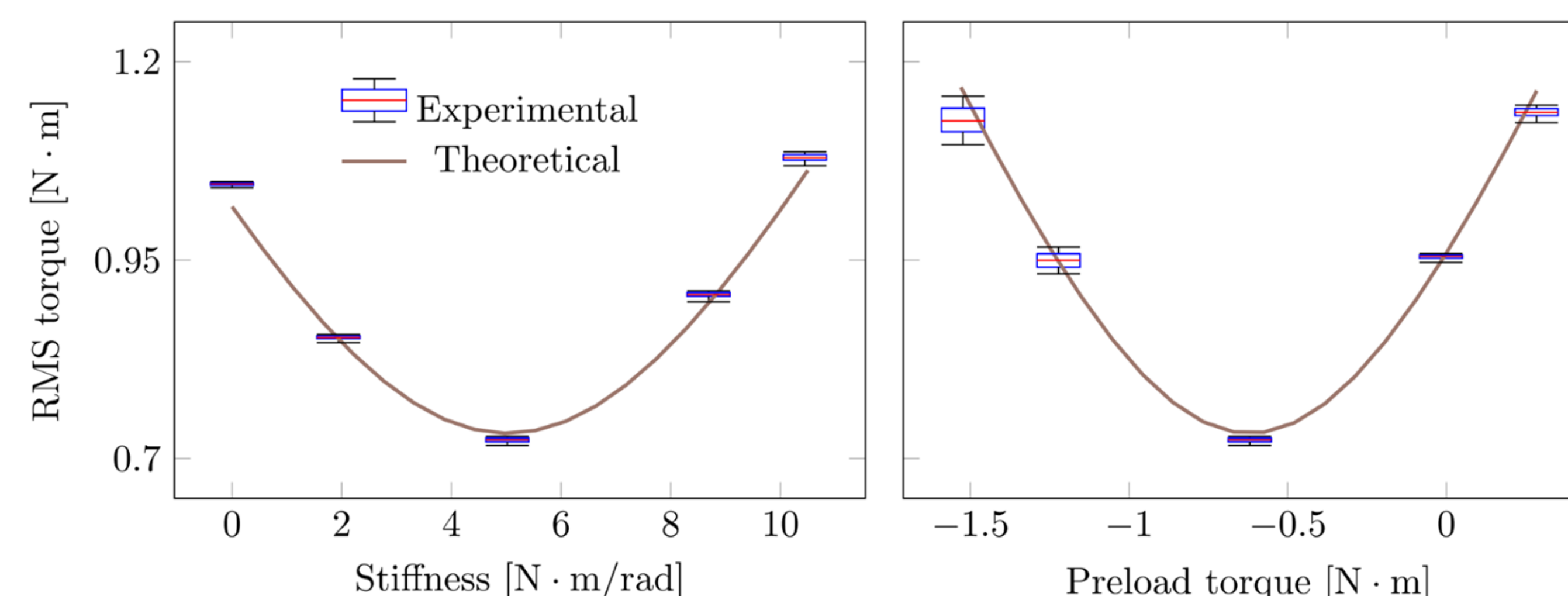
Users will experience **lower metabolic cost** during walking, stair ambulation, and sit-stand transitions due to a lighter prosthesis enabled by a globally optimal parallel spring that reduces motor torque requirements.



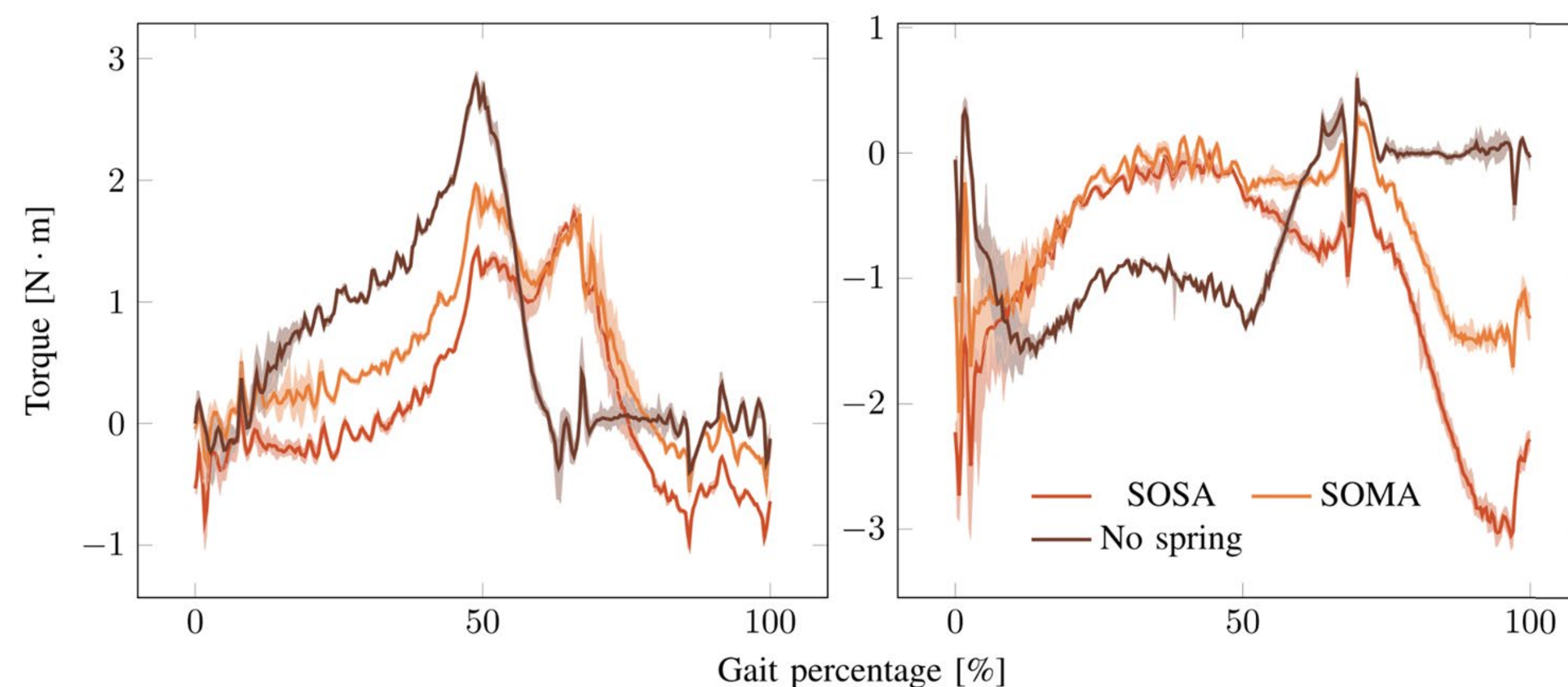
Open Source Leg  
www.opensourceleg.com

Educational Impact:

Dissemination with the Northern Indiana Amputee Support Group



RMS torque during one walking stride as a function of PEA stiffness and preload. Experimental validation that RMS torque is a convex function of spring stiffness and preload.



Torque of an actuator without the spring, with a spring optimized for walking (SOSA), and with a spring optimized for multiple activities (SOMA) during walking (left) and stair descent (right) for 50 strides.