

# Rules of the Road: Formal Guarantees for Autonomous Vehicles with Behavioral Contract Design

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<https://vehical.org>

## Abstract:

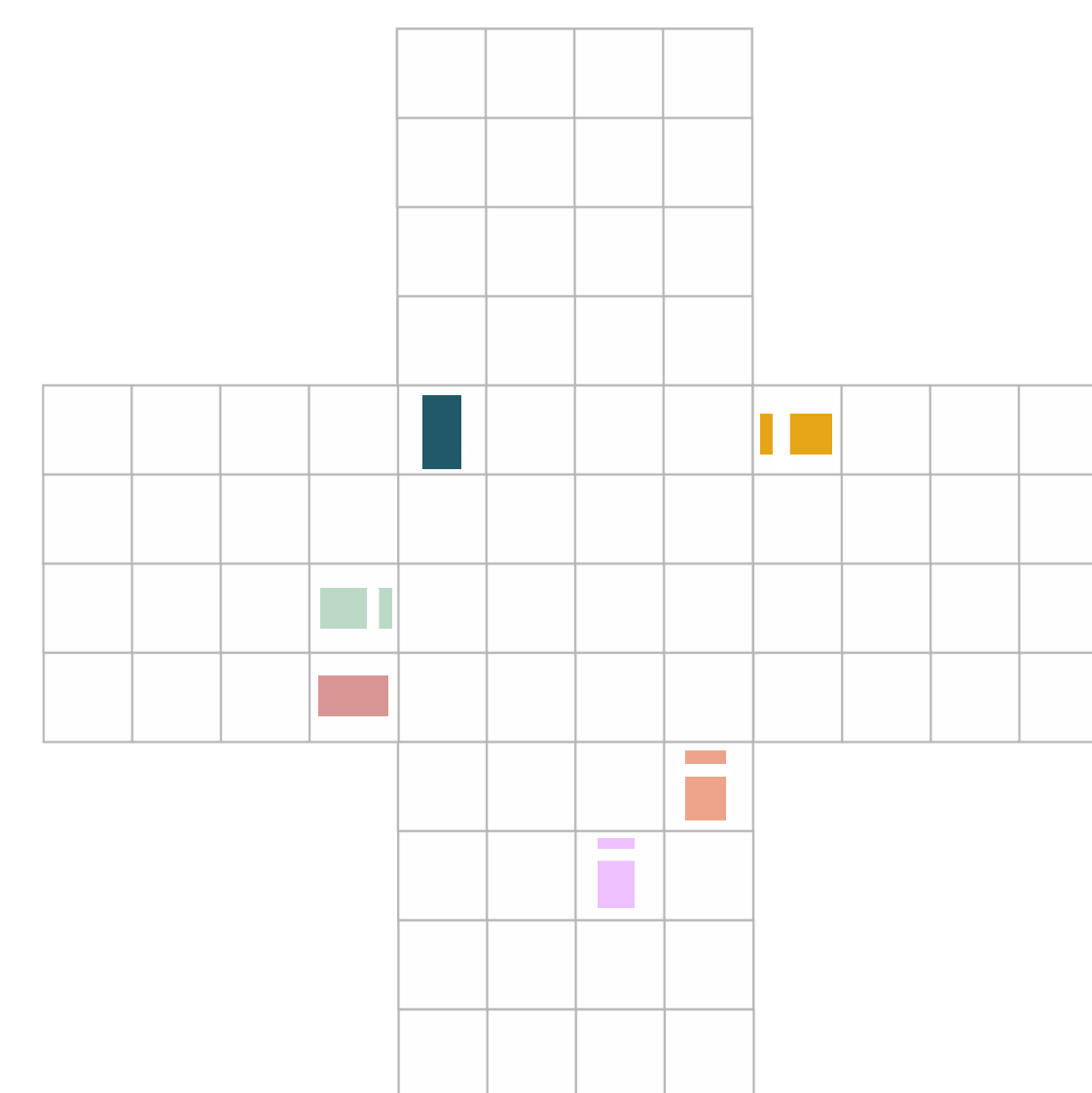
The ability to make formal guarantees on safety and performance for autonomous vehicles in **highly-interactive, dense environments** largely remains unsolved. With a **well-defined behavioral contract**, we can not only provide **formal guarantees** on agent safety and progress, but we also have a mechanism for **assigning blame** when accidents invariably occur. In this paper, we define a behavioral contract for a particular class of agents on a **road network environment** in a **quasi-simultaneous discrete-time game**. We provide **proofs of correctness** of the behavioral contract and **validate our results** in simulation.

## Challenge:

How do we design a **high-level decision making** strategy for autonomous agents in **highly-interactive** environments to behave **'correctly'**, i.e. be safe, be lawful, and make progress towards its destination?

Extremely challenging because:

- Robot-freezing problem and unbounded rationality.
- Joint action space grows exponentially.
- Other agents can act to intentionally make safety impossible.
- Can't satisfy all road rules all the time, which to violate?



## Scientific Impact:

Agent strategy (defined in a discrete-game and in specific road network environments that provides:

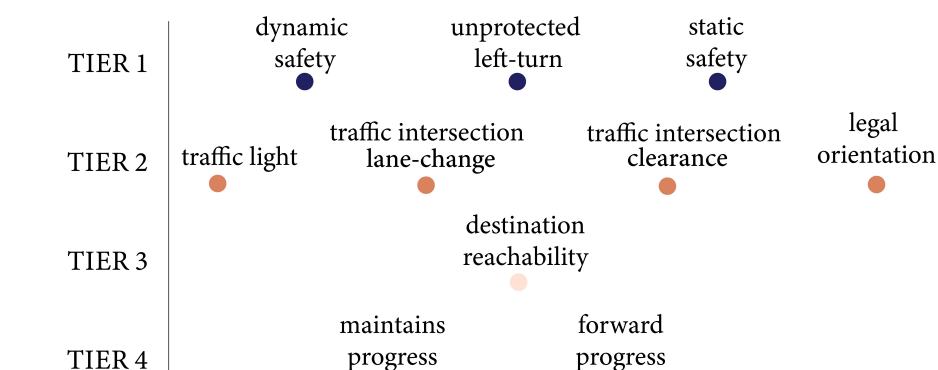
### Safety guarantee

**Safety Theorem**  
 Given that all agents  $Ag \in \mathcal{A}$  in the quasi-simultaneous game  $\mathcal{G}$  select actions in accordance to the **agent protocol** defined, we can show the **safety property**:  
 $P \Rightarrow \Box Q$   
 $P$  assertion that the game is in a state where every agent has a backup plan action that is safe.  
 $Q$  assertion that agents **never occupy the same grid point** at the same time.

### Performance guarantee

**Liveness Theorem**  
 Given the **sparsity conditions** hold, and that all agents  $Ag \in \mathcal{A}$  in the quasi-simultaneous game  $\mathcal{G}$  select actions in accordance to the agent protocol defined, we can show **all agents will eventually reach their respective destinations**.

### Scalability & Interpretability



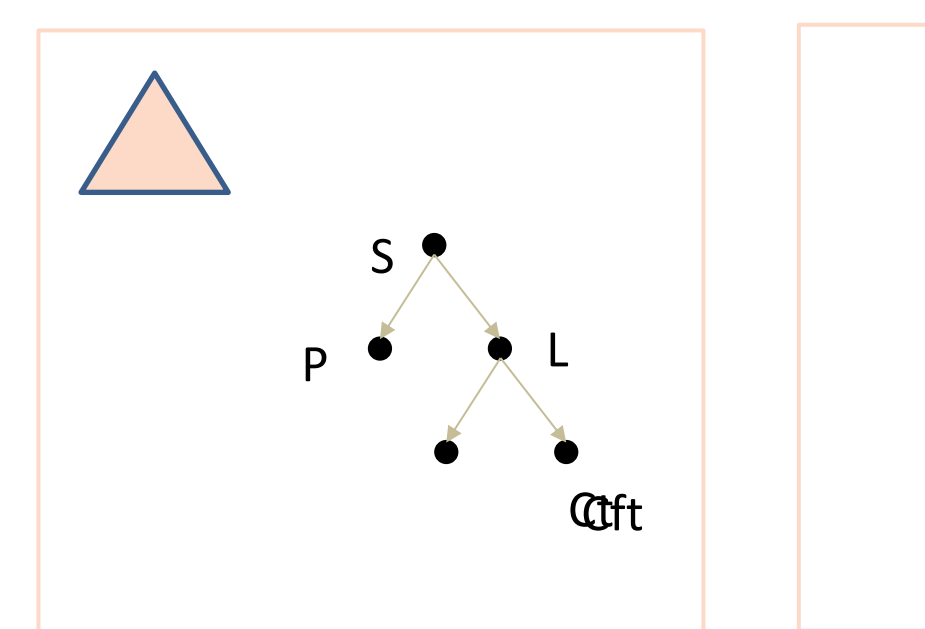
### Notion of Blame/Liability

$C_j = (A_j, G_j)$   
 $\forall j \in \mathcal{J}. \forall i \in \mathcal{J} - j. G_j \subseteq A_i$   
**Definition 11.2** (Blameworthy action). A *blameworthy action/strategy* is one in which an agent violates its guarantees, thereby causing another agent's assumptions not to be satisfied and thus resulting in an unwanted situation where blame must be assigned.

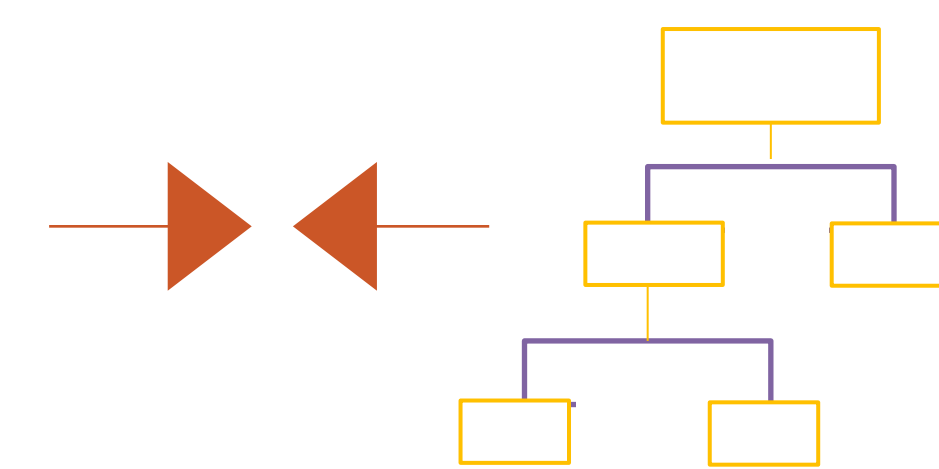
## Solution:

Propose the design of a behavioral protocol agents should use to select actions.  
 Strategy ensures agents are always entitled to safely execute their backup plan action (i.e. maximal braking)

### Pt. 1 Behavioral Profile



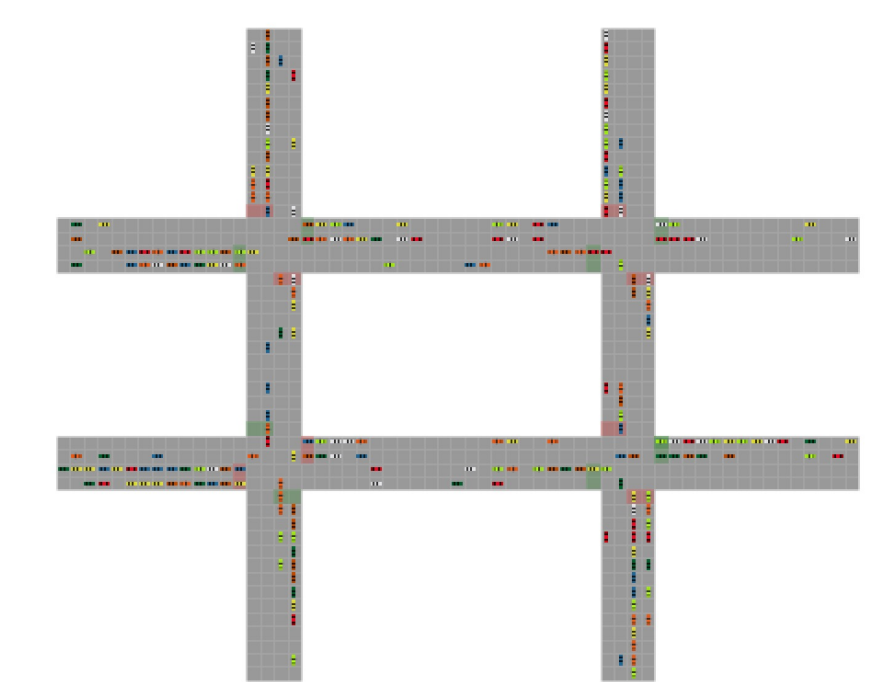
### Pt. 2 Conflict Resolution Scheme



## Proofs

1. Safety: no collisions.
2. Performance: agents make progress towards destinations. (under sparsity assumptions)

## Simulations



## Broader Impact on Society

- Adoption of this type of framework will lead to safer and more interpretable autonomous vehicles on the road..
- Serves as a novel framework for designing vehicle behavior with the collective in mind (instead of the individual).
- Could be integrated alongside data-driven/machine learning approaches.

## Broader Impact: Education and Outreach



Designed and hosted workshop on 'Building Effective Research Collaborations' to teach grad students communication and conflict prevention/management skills. Resources can be found:  
<http://healthycollab.caltech.edu/>

## Quantifying Broader Impact:

- Potential to design autonomous vehicle algorithms that reduce number of collisions on the road.
- Also could help inform design of autonomous vehicle road rules and regulations.

