

# The impact of QoT on Estimation and Control



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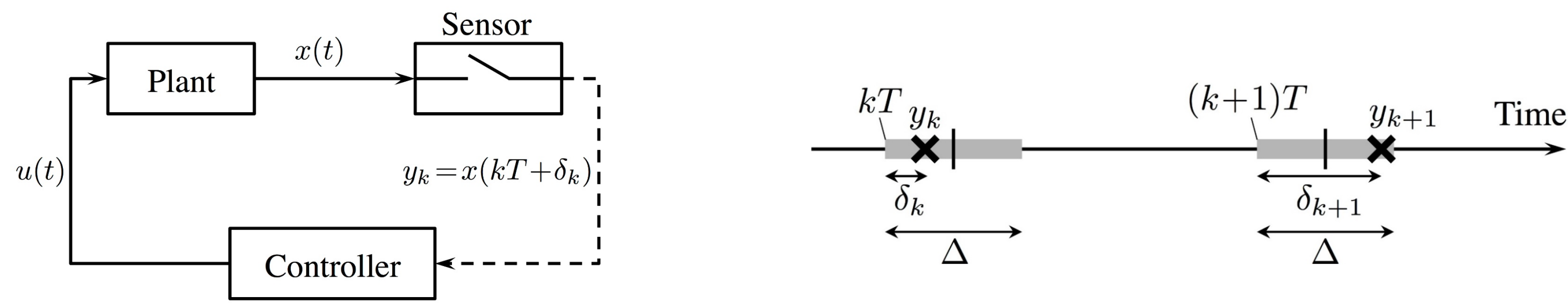
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## Stabilization under clock offsets

**Q:** What if sensor/controller clocks are not synchronized?

**A:** Clock offset introduces distortion and may render the system unstable.



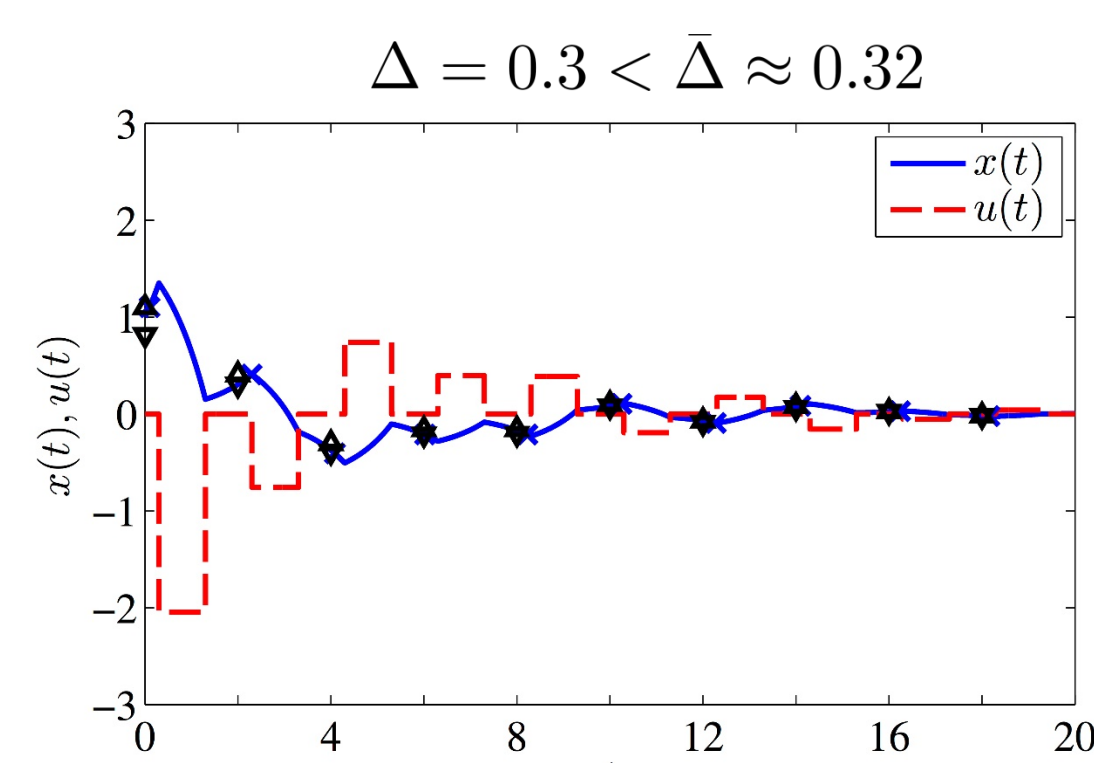
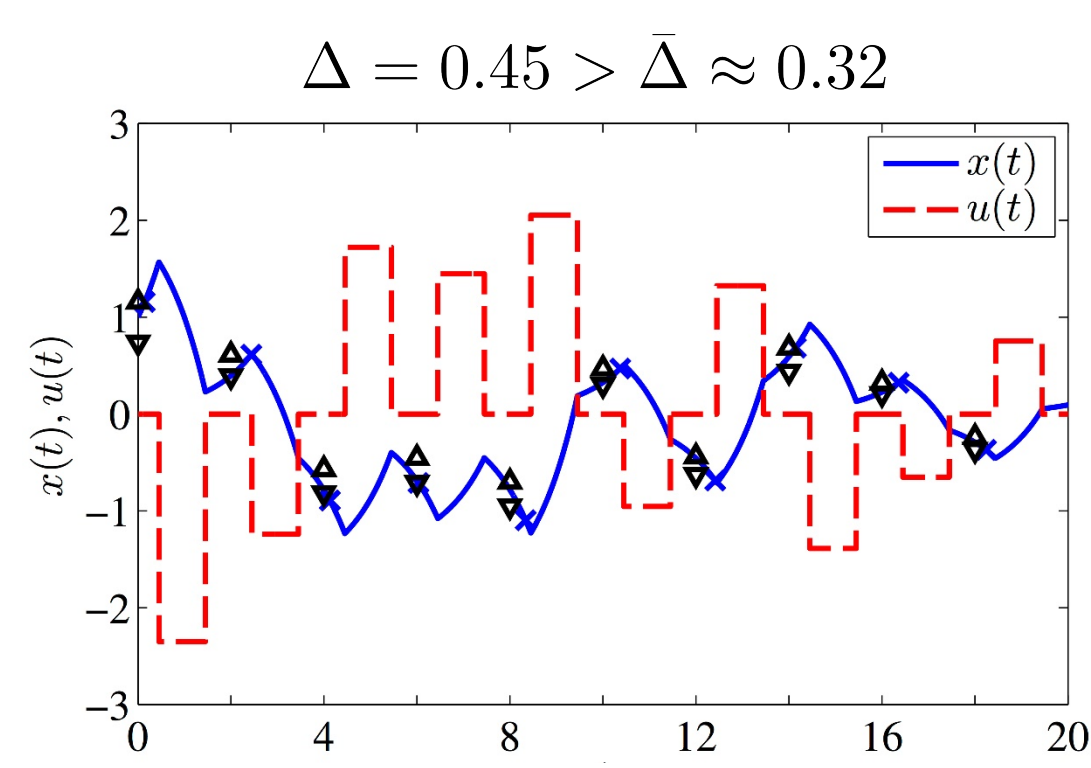
**Goal:** Determine limitations on the clock offset tolerable for stabilization.

### Stabilizability with infinite bit-rate

**Plant with scalar-valued state:**  $\dot{x} = \lambda x + b u, x \in \mathbb{R}$

- If  $\lambda > 0$  is small enough, then all clock offsets
- Otherwise an upper bound  $\Delta$  on  $\delta_k$  is derived.

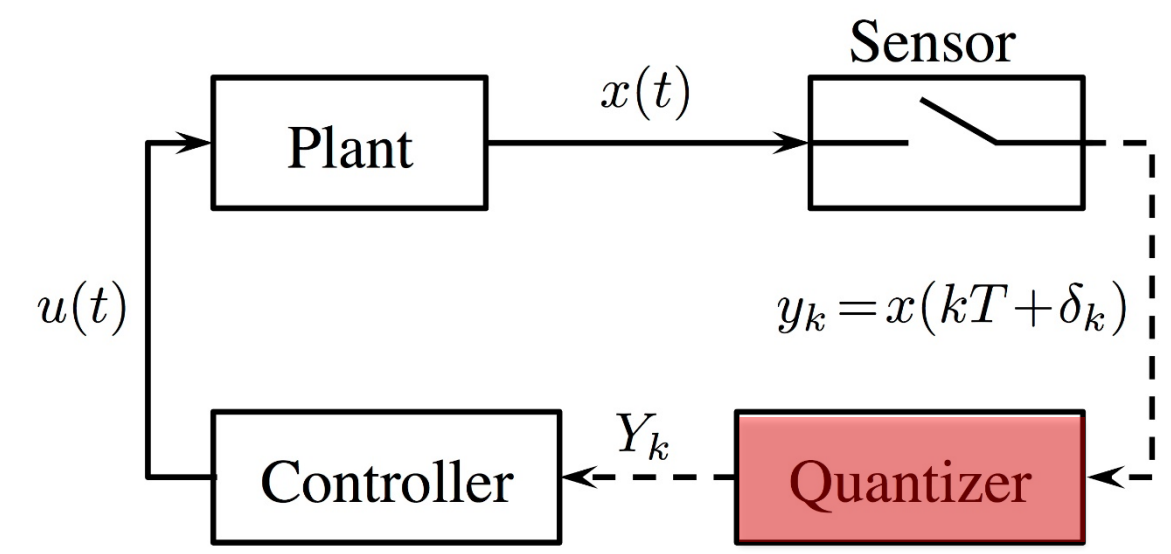
$\delta_k$  are tolerable.



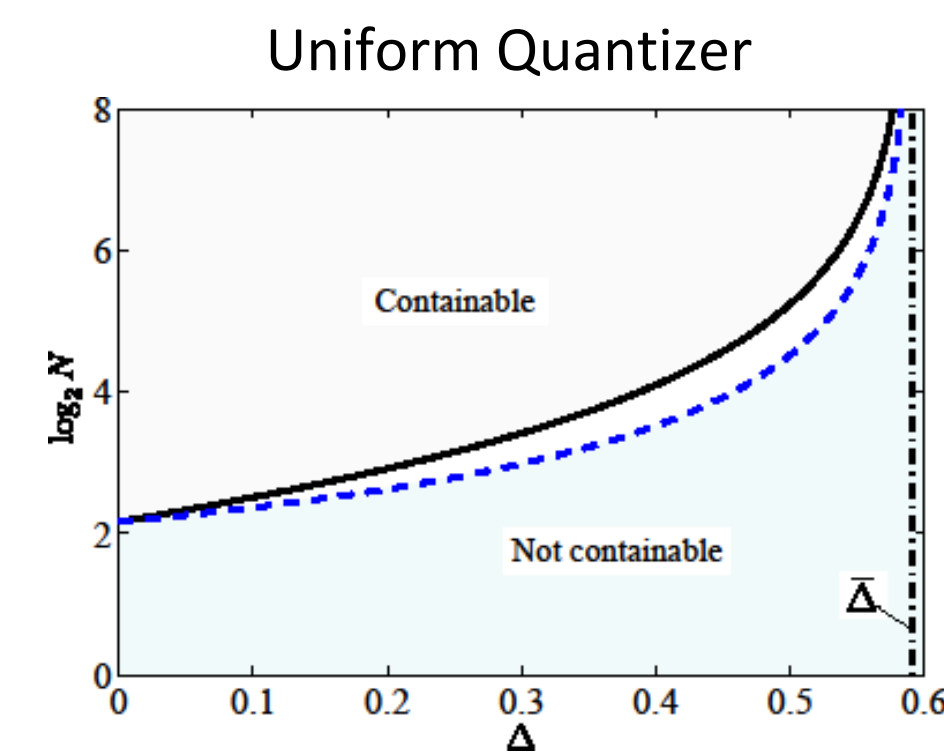
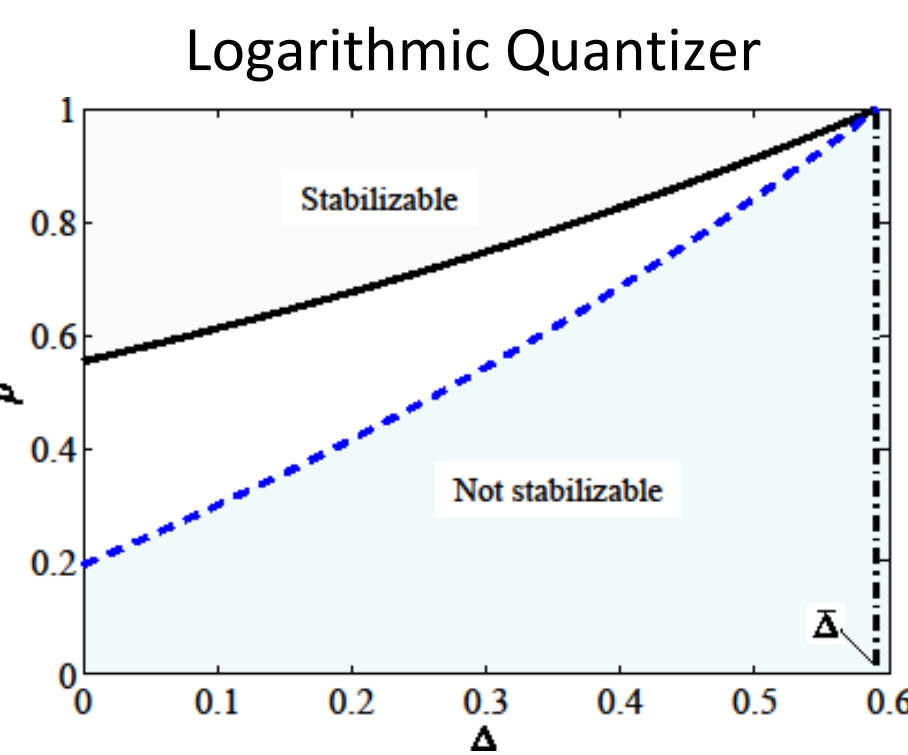
**Plant with vector-valued state:**  $\dot{x} = A x + B u, x \in \mathbb{R}^n$

- If the matrix  $A$  has at least two distinct eigenvalues, then all clock offsets  $\delta_k < T$  are tolerable.

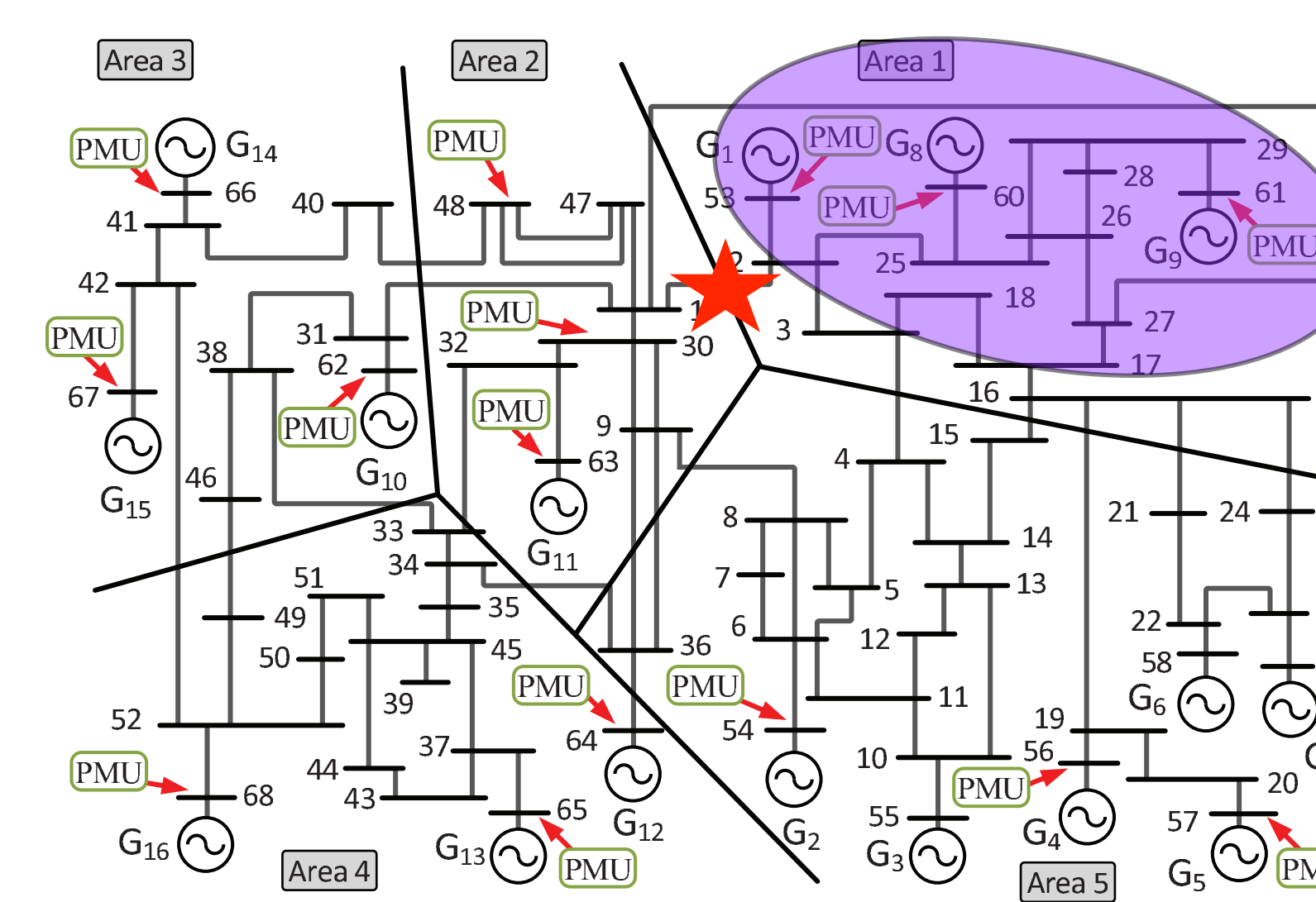
## Control with quantized measurements



- A larger clock offset requires a finer quantization.
- Necessary conditions and sufficient conditions for stabilizability.

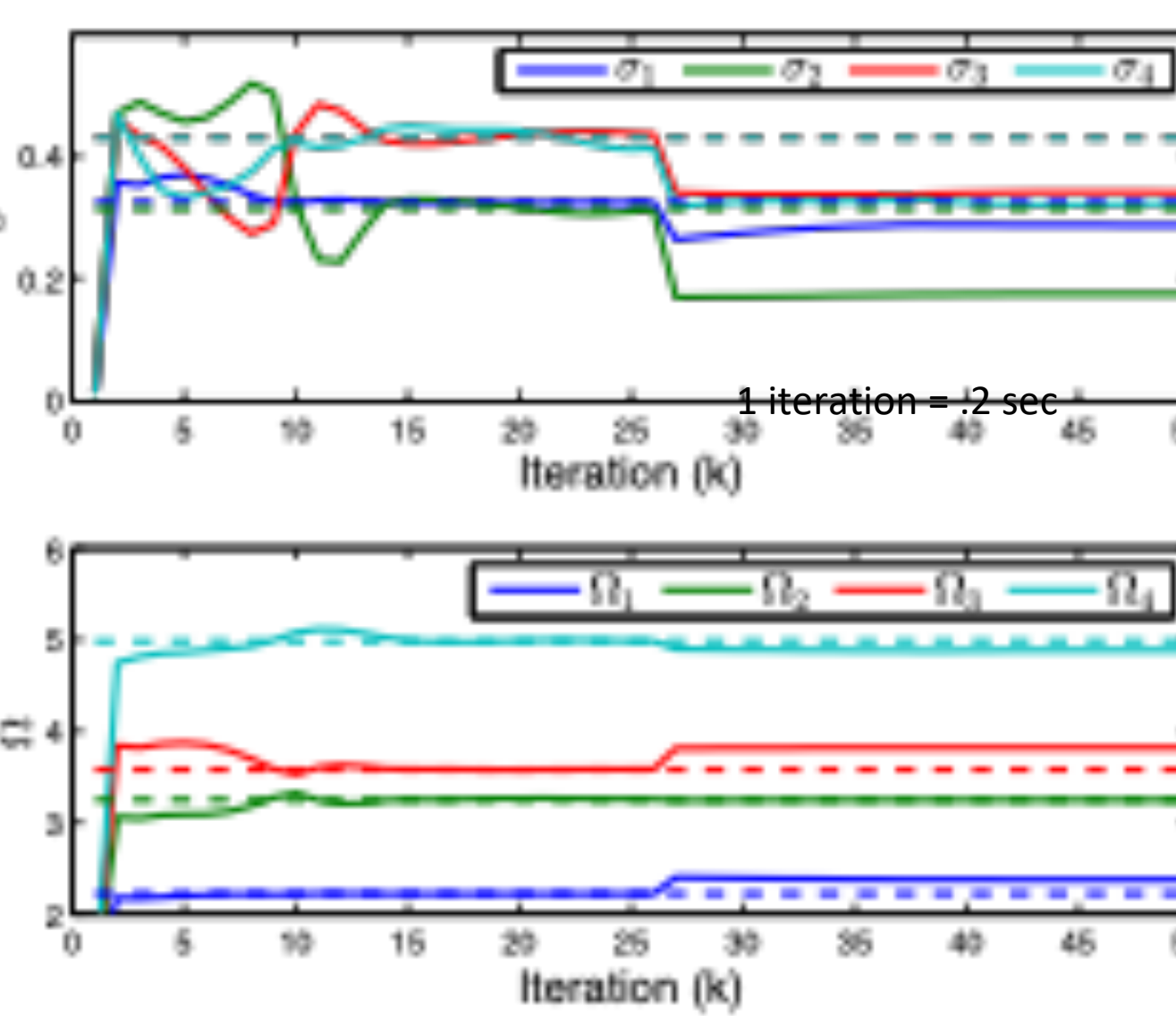


## Detection of grid oscillations under attacks



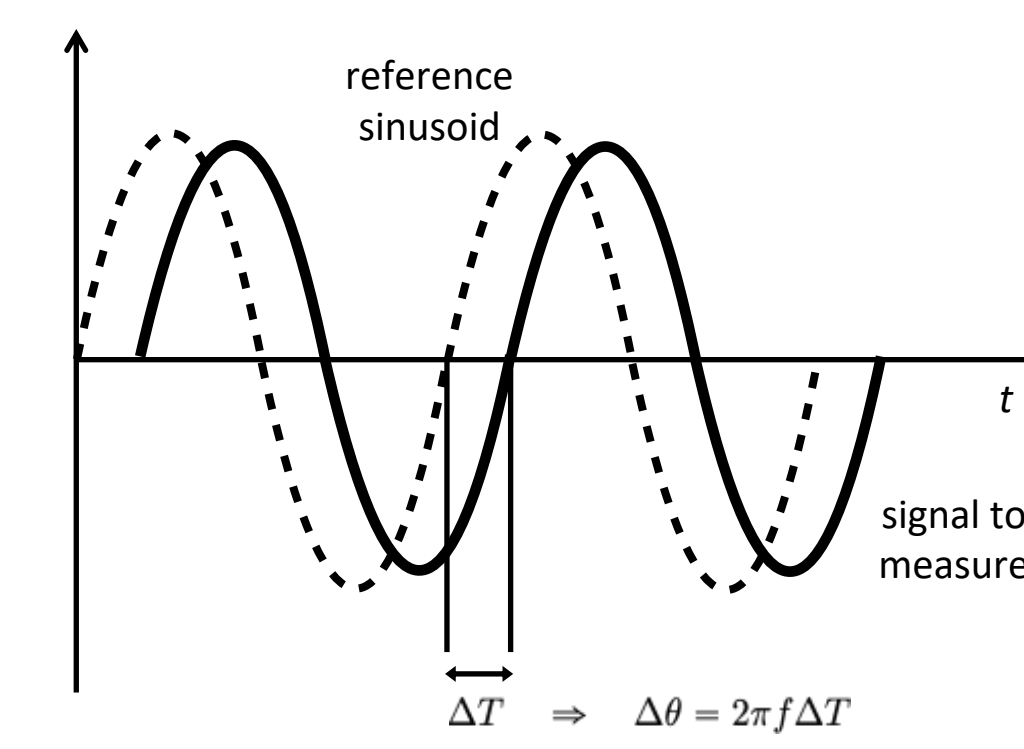
- Disturbances lead to oscillations in voltage/current phase and frequency
- PMU (phase) measurements can be used to estimate complex eigenvalues associated with these oscillation—*hopefully stable!*

$$y_i(t) = \sum_{k=1}^N \alpha_{k,i} e^{-\sigma_k t} \cos(\Omega_k t + \phi_{k,i})$$



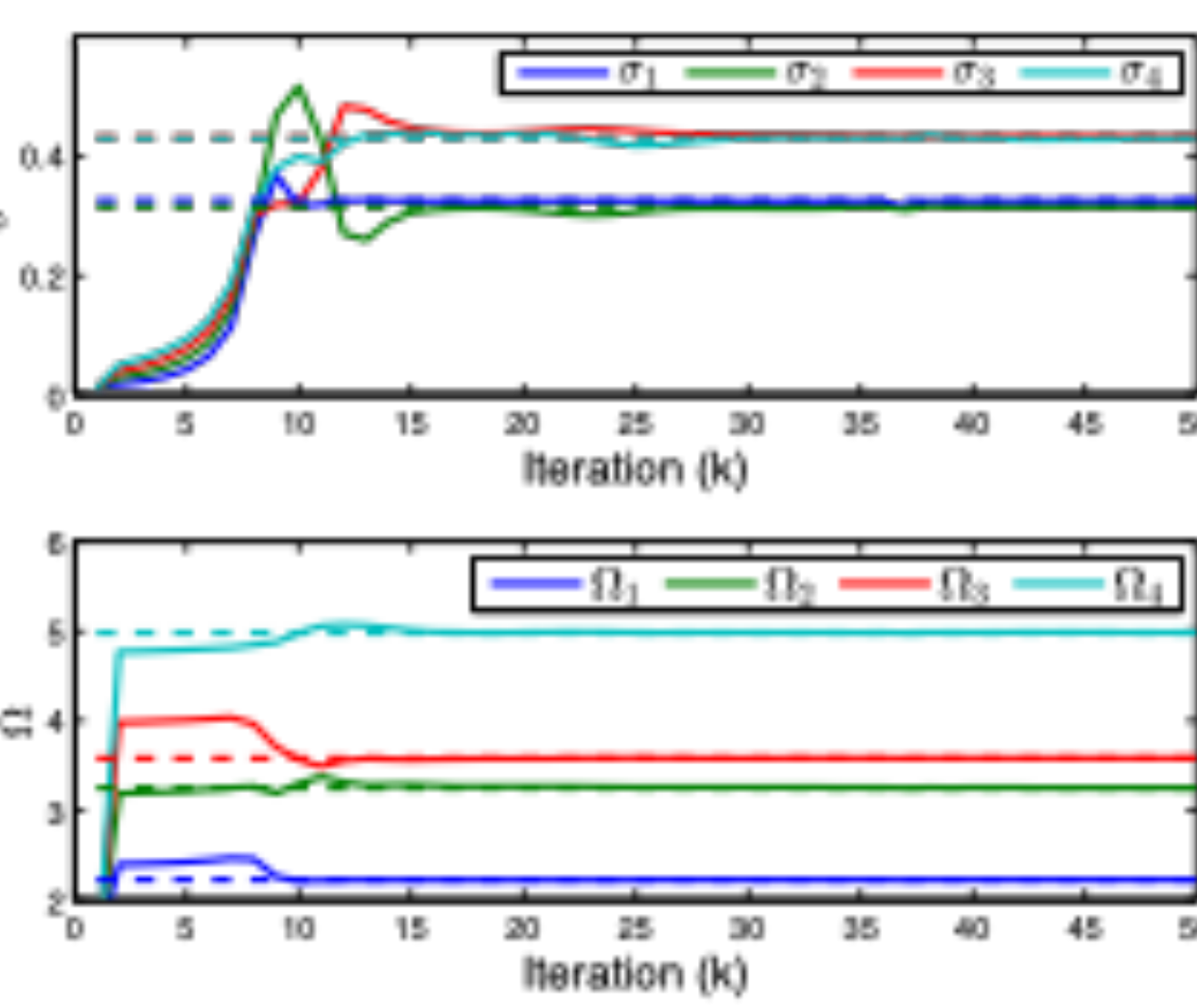
**Estimation using distributed Prony algorithm**

- Oscillations due to a simulated three-phase fault at line connecting buses 1 and 2
- Estimation of 4 dominant oscillation modes
- Iterative version of two-step Prony algorithm with computation distributed among 5 Phase Data Concentrators (PDCs)
- Attack on Area 1 PMUs at iteration  $k = 26$
- Apparent decrease in estimated decay-rates  $\sigma_k$



**GPS spoofing**

- Broadcast radio signals that resemble a set of normal GPS signals that would be received at a different location and/or time
- Can be done with hardware under \$500 (Software Defined Radio), all software available for free download



**Estimation using resilient distributed algorithm:**

- Spatial consistency:**
  - compute *median* of estimates across PDCs
  - estimates that remain away from *median* by more than  $\delta$  cause PDC estimates to be ignored
- Time consistency (across iterations)**
  - each PDC should not update its current estimates by more than  $\epsilon$  per iteration
  - changes larger than threshold cause PDC estimates to be ignored

## Secure localization based on Time-of-Flight: Distributed Optimization Algorithm

**Q:** What if sensor clocks are not synchronized and the transmission is subject to a malicious attacks?

**A:** Timing mismatches and incorrect information effectively introduce error in the estimation!

- Devices exchange time-stamped messages between neighbors
- Time-of-flight measurements provide information about relative distance and clock parameters.
- Messages carry the current estimate of device position and clock parameters.
- Malicious agents can hijack some of the messages and alter the estimate or the timing information.

### Distributed Optimization Algorithm

- 1) Exchange messages.
- 2) At each node solve:  $\min_{x_i, a_i} f_i(x_i) + \sum_{j \in N_i} f_{ij}(x_i, x_j, a_{ij}) + \sum_{j \in N_i \cap N_j} f_{ji}(x_j, x_i, a_{ij}) + \gamma \|a_i\|_1$
- 3) Broadcast estimation to neighbors.
- 4) Return to 1) if tolerance not met.

Maximum Likelihood Estimation      Regularization

#### Additive attacks at several nodes

• The effect of the attack is mitigated.

• The attack signal origin and magnitude can be identified

• Redundancy is crucial when detecting outliers! Less measurements, more vulnerable.

## UCSB Publications

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(\*) collaboration with other NSF project partners

