



Massachusetts Institute of Technology



*The Action Lab*

Newman Laboratory for Biomechanics  
and Human Rehabilitation



# Collaborative Research: Towards Robots with Human Dexterity

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Disclosure: Neville Hogan holds equity in Bionik Laboratories,  
which manufactures human-interactive technologies for rehabilitation

NRI- 1637824 (Hogan)

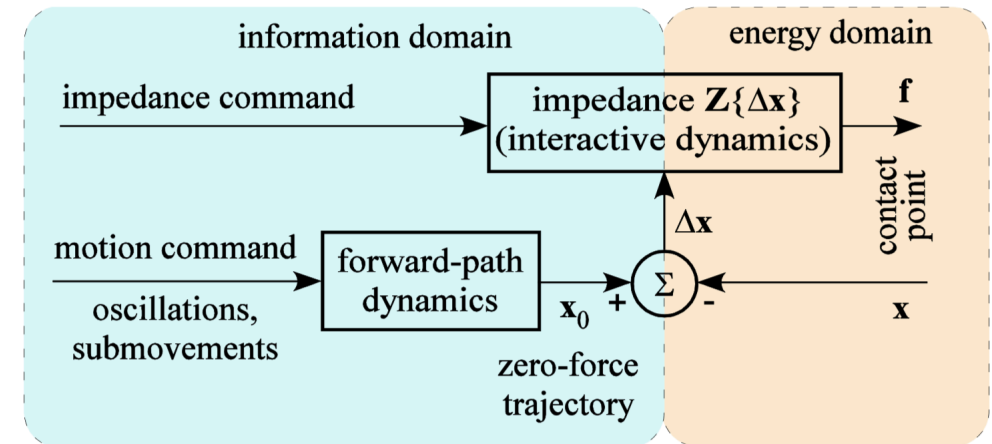
NRI- 1637854 (Sternad)

# Understanding Human Dexterity



- **Premise: Studying humans may facilitate**
  - Improved robot control
    - Scale-up to many DOF
  - Physical human-robot collaboration
- **Hypothesis: Humans use dynamic primitives**
  - To work around neural limitations
- **Dynamic primitives: Robust attractors of low-level dynamics**
  - Limit cycle (rhythmic oscillation)
  - Trajectory (stereotyped submovement)
  - Mechanical impedance (interactive behavior)

## Combine Primitives in a Nonlinear Equivalent Network



The 'equivalent source'

- Describes forward path dynamics
- Composed of motion primitives

The 'equivalent resistance'

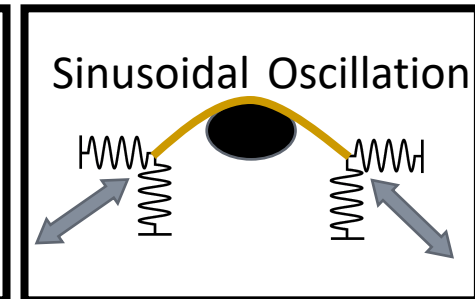
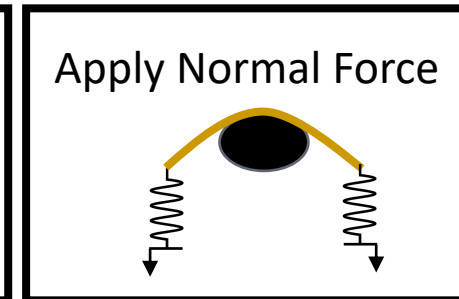
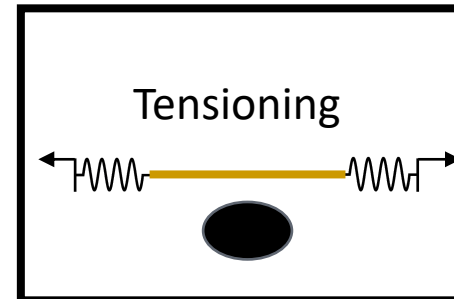
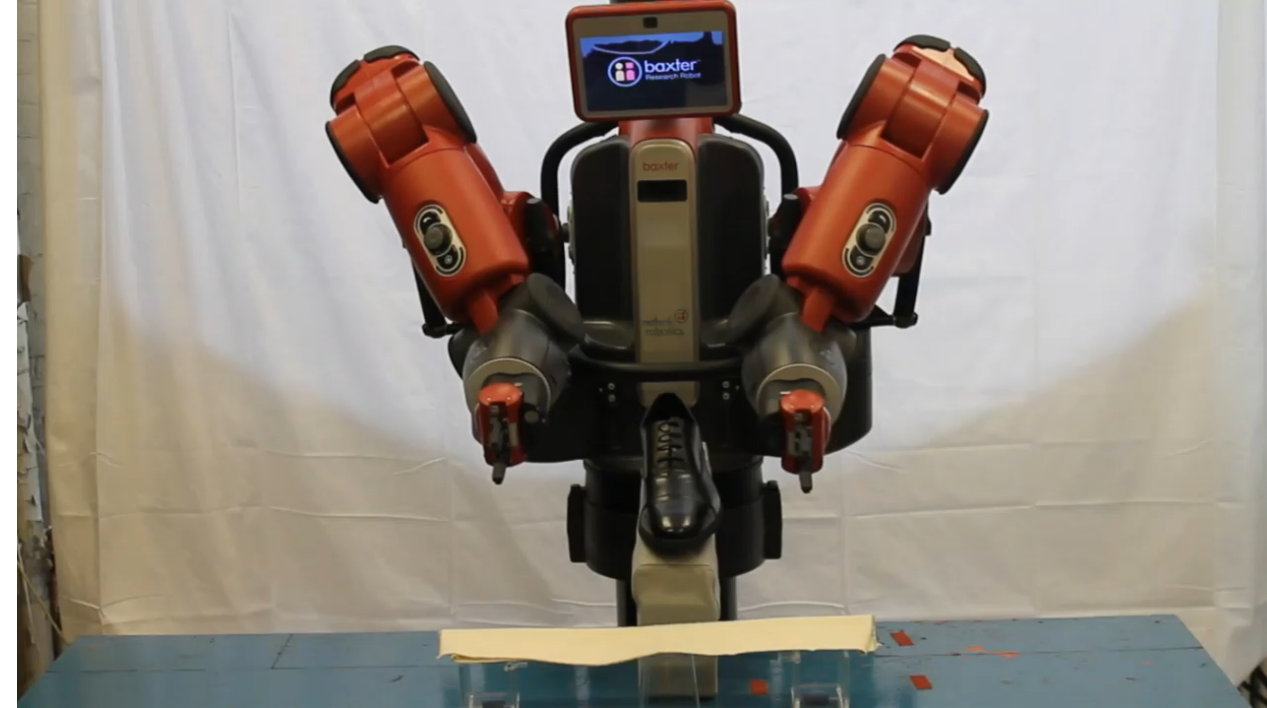
- Describes interactive dynamics
- Composed of impedances

A 'neo-classical' approach?

# Mechanical Impedance Compositionality



- **Compositionality: Impedances superimpose even if non-linear**
  - Map desired end-point stiffness  $f = k(x_0 - x)$  to configuration space  $\tau = J(\theta)^T k(x_0 - L(\theta))$
  - Define configuration controller  $\tau_j = K(\theta_n - \theta)$  and add  $\tau_{net} = J(\theta)^T k(x_0 - L(\theta)) + K(\theta_n - \theta)$
- **Notable features:**
  - No inverse kinematics—works at singularities
  - Makes control modular and versatile
    - Flexible object
    - Multi-arm coordination
    - Contact and non-contact phases



# Human Interaction with a Kinematic Constraint



## Subjects turned a crank while instructed to:

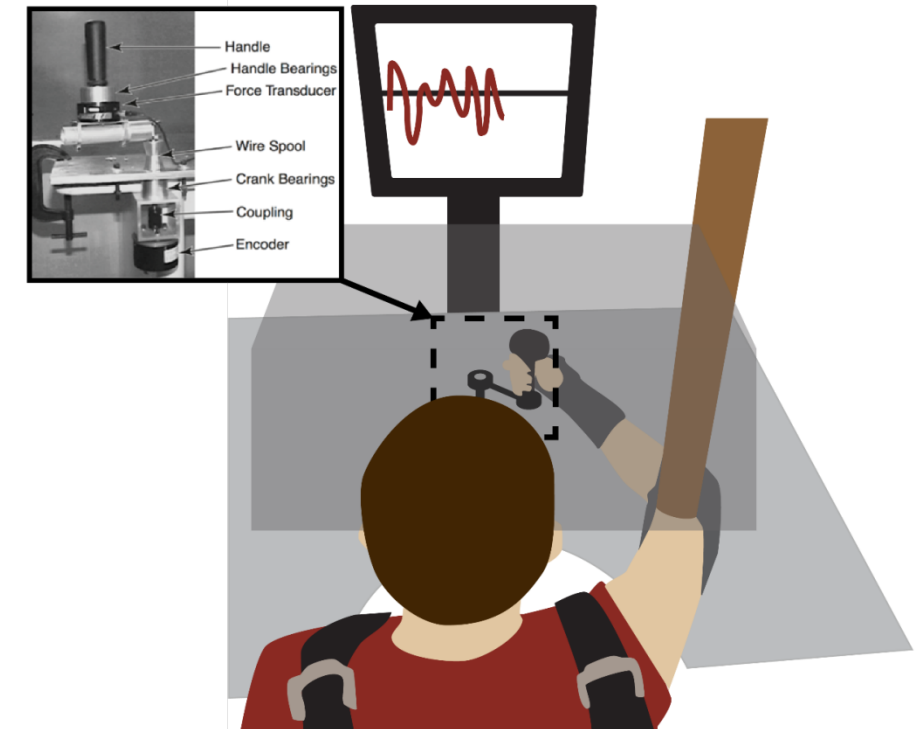
- Turn at different constant speeds: slow, medium, fast
- CW or CCW
- The hand was occluded from view
- Visual speed feedback was provided

## Main result: Despite instruction and feedback

- Speed varied systematically with crank angle
- Normal force varied systematically about zero

## Underlying motion command:

- Describe interaction dynamics as mechanical impedance  $Z\{\cdot\}$ 
  - $F(t) = Z\{\Delta x(t)\}$
  - $\Delta x(t) = x_0(t) - x(t)$
- Subtract off interaction dynamics
  - $x_0(t) = x(t) + Z^{-1}\{F(t)\}$



$x_0(t)$  = zero-force trajectory (ZFT)

# Zero-Force Trajectory Revealed Underlying Structure



## Zero-Force Trajectory

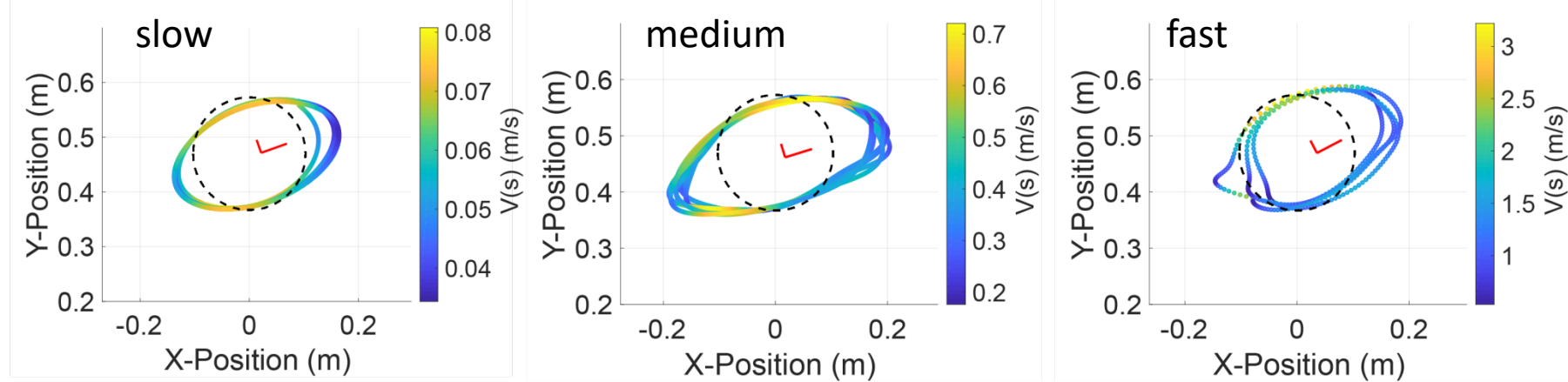
- Roughly elliptical path
- Speed minima and curvature maxima coincided

Similar to a speed-curvature relation widely reported in unconstrained motion

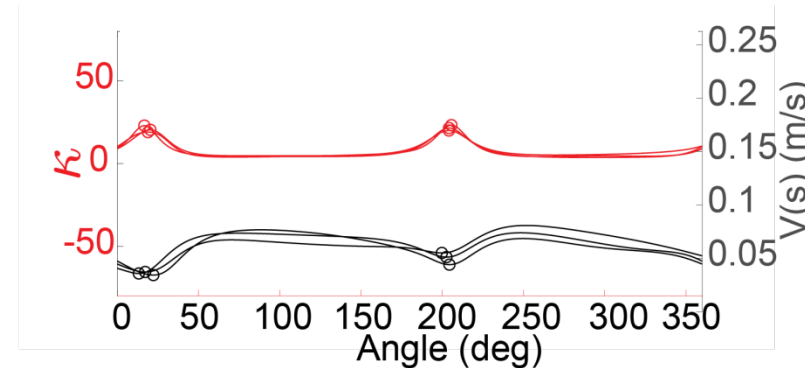
- **The “1/3 power law”**

## Dynamic Primitives

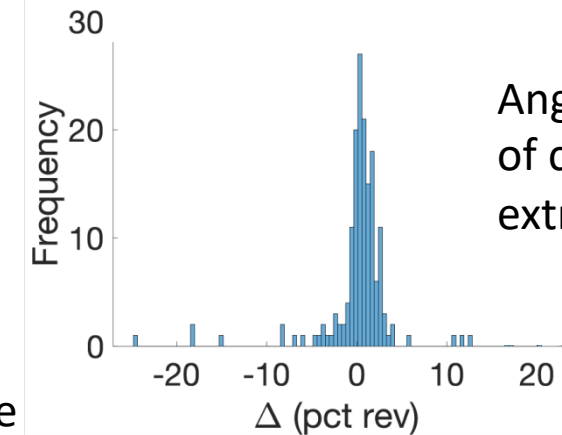
- Consistent with underlying motion composed of two primitive oscillations



Zero-force trajectories. Red lines denote major & minor axes of best-fit ellipse

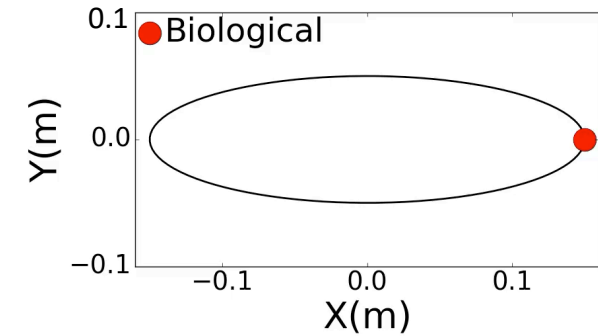


Zero-force trajectory speed and curvature

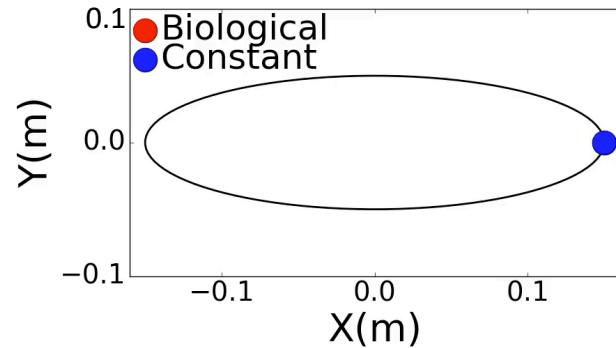


Angular separation of corresponding extrema

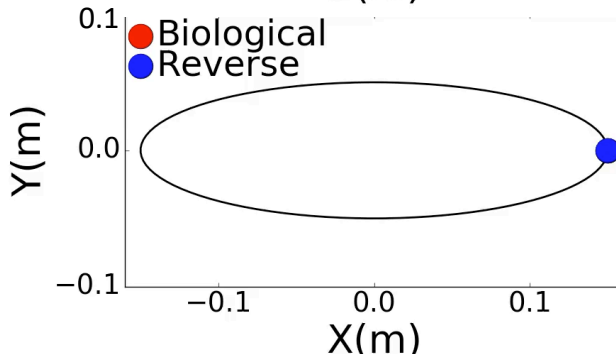
# Human Interaction with a Moving Constraint: 1/3 Power Law



**b = 1/3**



**b = 0**

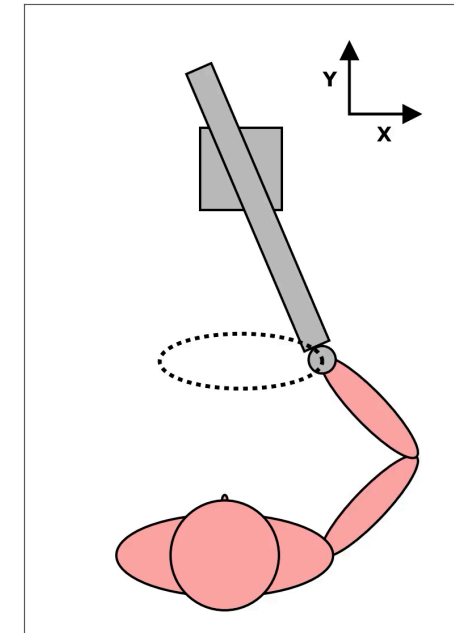
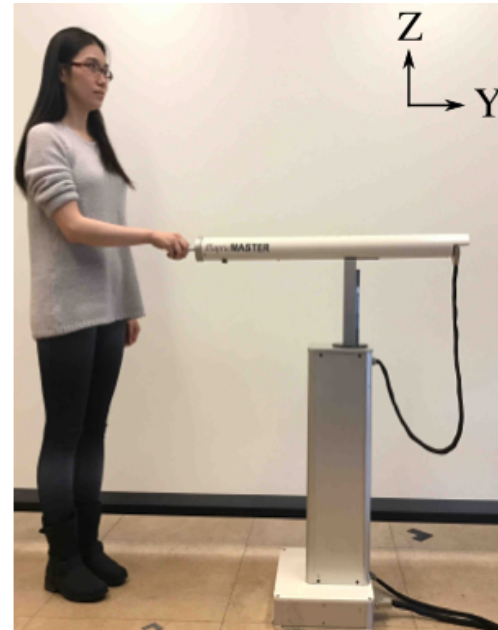


**b = -1/3**

Humans display a specific scaling of velocity with curvature

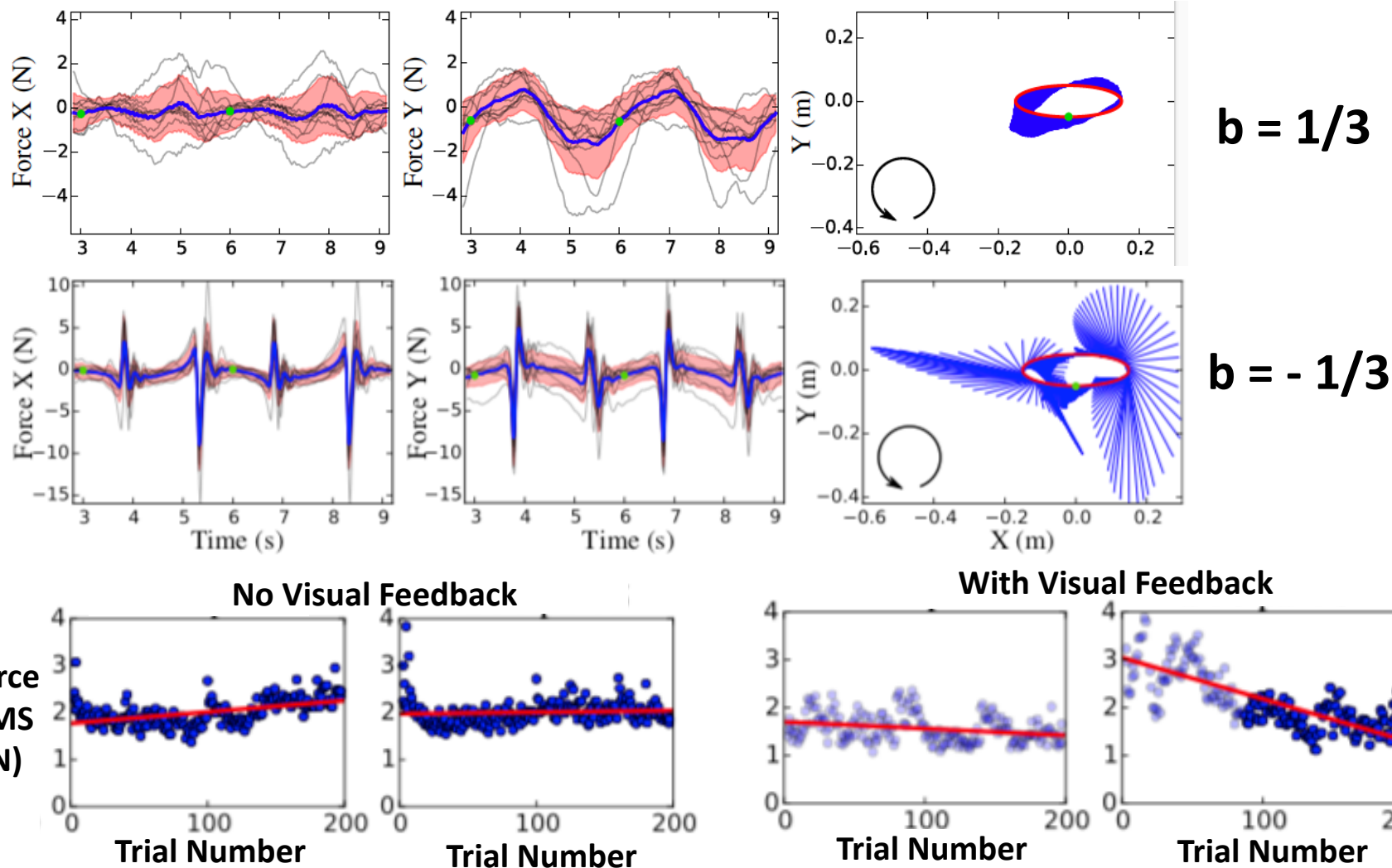
$$v(t) = K r(t)^b$$

**v**: tangential velocity, **r**: radius of curvature, **b**: 1/3





# Humans Cannot Perform Non-Biological Velocity Patterns



- Humans exert greater forces with greater deviations from  $b = 1/3$ .
- Humans do not learn non-biological velocity-curvature patterns without visual feedback.

# Human Interaction with a Complex Object



## How Do Humans Manipulate Complex Objects?

- Long delays imply heavy reliance on predictive control based on an internal model
- But complex internal models seem unlikely

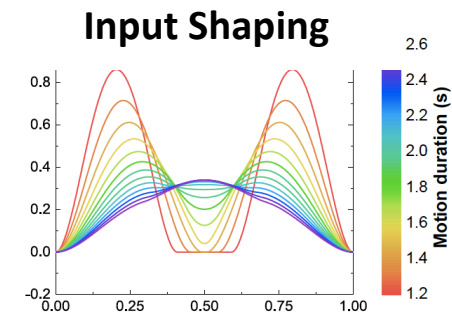
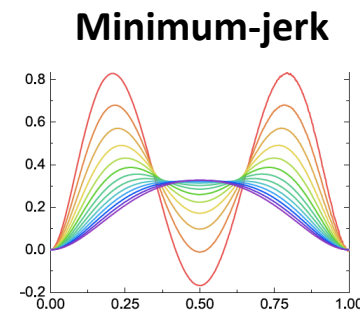
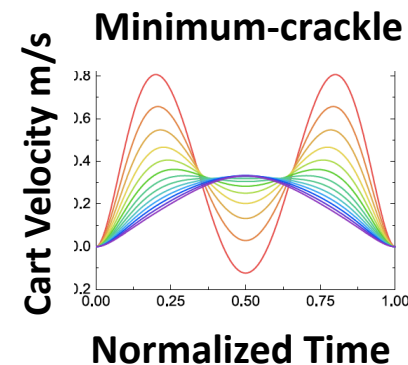
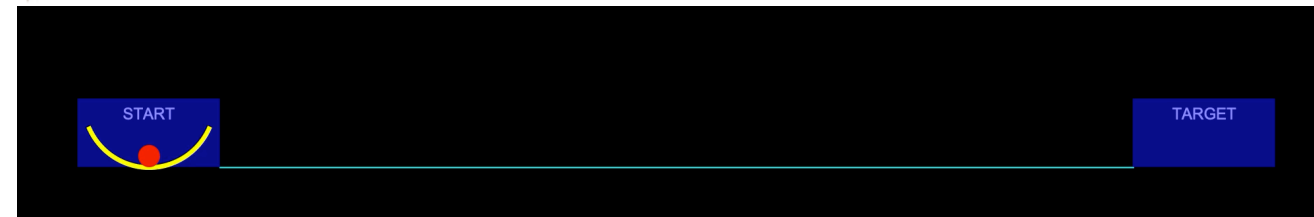
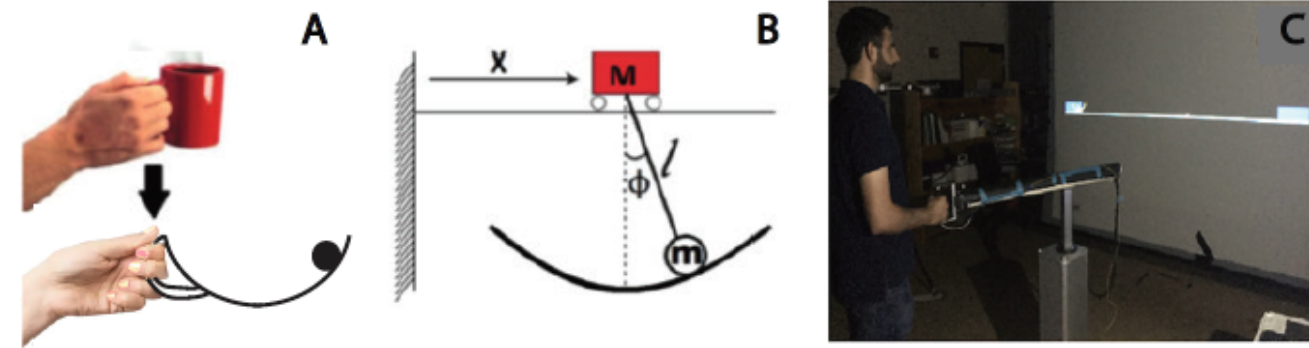
## Overall Hypothesis:

Humans simplify control by using dynamic primitives

- Control via Input Shaping eliminates residual vibrations

## Alternative Hypotheses:

- Using optimization

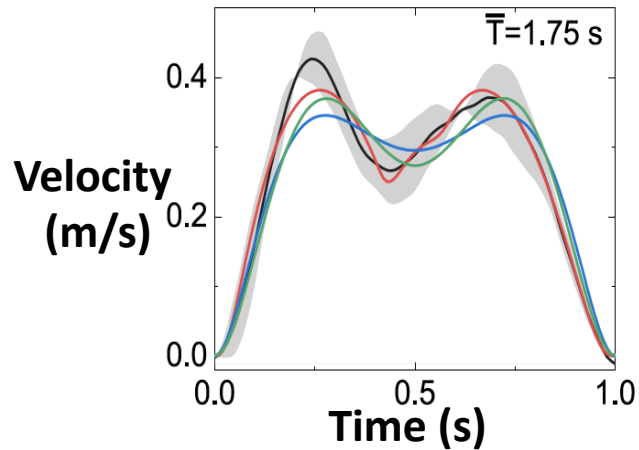




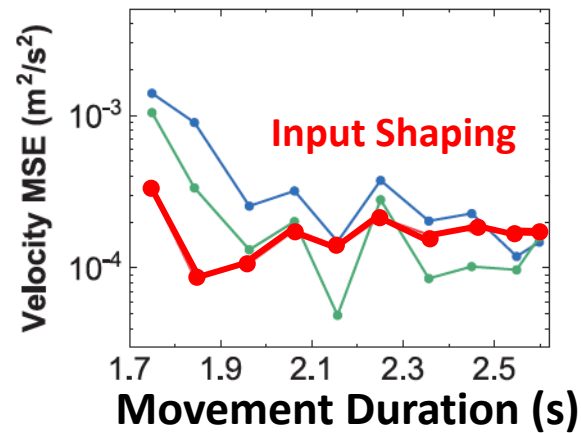
# Input Shaping with Two Submovements is the Best Control Strategy



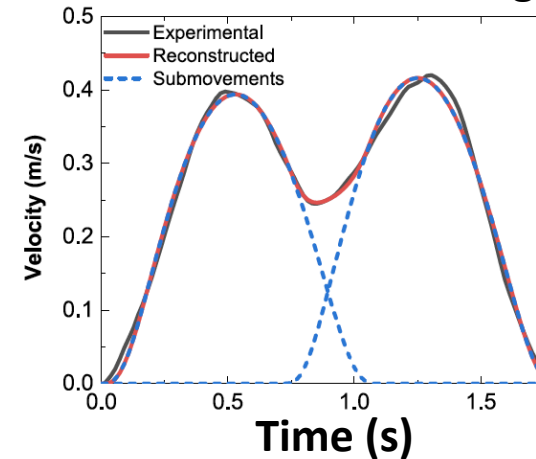
Data and Models



Different Model Fits



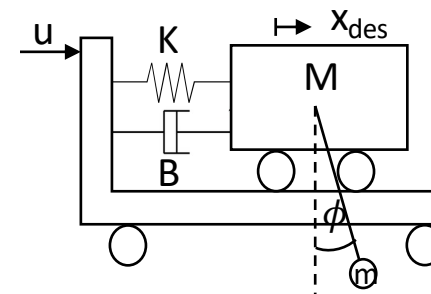
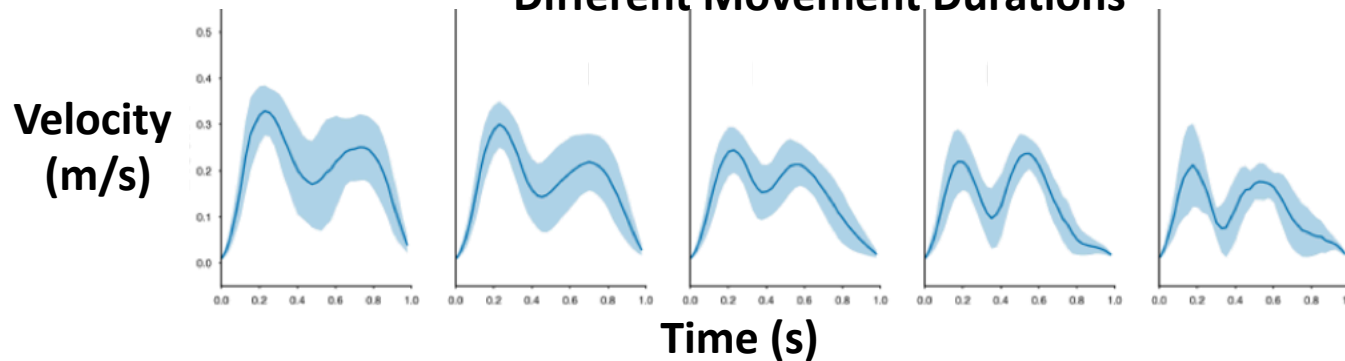
Submovement Fitting



Two submovements fit the human velocity profile

Input shaping →  
**Dynamic Primitives**

Different Movement Durations



**Next Step:** Asymmetric profile indicates presence of impedance

# Compositionality Simplifies Scale-Up to Many DOF



- **Readily extends to two (or more) arms**
  - Connected at a common end-point
  - Interacting with a common object
  - Net end-point stiffness is  $k_{both} = k_l + k_{j,l} + k_r + k_{j,r}$
- **Superimpose open-chain single arm controllers**
  - Left arm:  $\tau_{net,l} = J(\theta_l)^T k_l (x_{0,l} - L(\theta_l)) + K_l(\theta_{n,l} - \theta_l)$
  - Right arm:  $\tau_{net,r} = J(\theta_r)^T k_r (x_{0,r} - L(\theta_r)) + K_r(\theta_{n,r} - \theta_r)$
- **No closed-chain kinematic computation**
- **No inverse kinematic computation**

