Tracking Measurements Produced by DNNs Forrest Laine, Anish Muthali, Claire Tomlin

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Object Detection from Cameras





Object Tracking from Cameras Bounding Box Detections



Chapman-Kolmogorov Updates:

$$p(x_{k}|z_{1:k-1}) = \int p(x_{k}|x_{k-1}) p(x_{k-1}|z_{1:k-1}) dx_{k-1}$$

$$p(x_{k}|z_{1:k}) = \frac{p(z_{k}|x_{k}) p(x_{k}|z_{1:k-1})}{p(z_{k}|z_{1:k-1})}$$

$$p(z_{k}|z_{1:k-1}) = \int p(z_{k}|x_{k}) p(x_{k}|z_{1:k-1}) dx_{k}$$



Object Distribution

Process Model

Measurement Model

Bounding Box Detections



 $x = (p_x, p_y, v_x, v_y, w, h) \text{ OR } \emptyset$

Detections measure: $z = (p_x, p_y, w, h) \text{ OR } \emptyset$

Each object track has the following state:



Object Tracking from Cameras Bounding Box Detections

Most important modeling choice in tracker design is measurement model:

$$p(\bar{z}_k = z_k | \bar{x}_k = x_k)$$
 True Positive

 $p(\bar{z}_k = \emptyset \mid \bar{x}_k = \emptyset)$ True Negative

How should these be chosen? Especially for DNN measurements? OOD?





$$p(\bar{z}_k = z_k | \bar{x}_k = \emptyset)$$
 False Positive

 $p(\bar{z}_k = \emptyset | \bar{x}_k = x_k)$ False Negative

Object Tracking from Cameras Bounding Box Detections

Ideally, for each measurement \bar{z}_k , we could estimate the uncertainty internal to the DNN regarding the sensor input:

$p(\bar{z}_k o_k, D)$	Thi
	mea
Training Dataset	$p(\bar{z})$
Camera input Measurement	$p(\bar{z}$

However, for bounding box detections, it is not clear how to extract this distribution.





s distribution could serve to inform our asurement models used in tracking better

$$\bar{z}_k = z_k \,|\, \bar{x}_k = \emptyset)$$

 $\bar{z}_k = \emptyset \,|\, \bar{x}_k = x_k)$

Object Tracking from Cameras Pixel-Level Detections

The output at each pixel is a 2D value $y_k^{i,j}$ which is arg-maxed to obtain a detection (e.g. 1 = object, 0 = not)

Using off-the-shelf variance propagators, we are able to obtain an estimate of $p(y_{k}^{i,j} | o_{k}, D)$ in the form of a gaussian distribution.

This distribution can then be propagated through the arg-max function (via particles or other) to obtain a probability of occupancy $p(z_k^{i,j} = 1 | o_k, D)$.

This distribution can be decomposed into <u>detection</u> and <u>uncertainty</u>

https://arxiv.org/abs/1908.00598







Object Tracking from Cameras Pixel-Level Detections

The measurement models used with pixel-level detections (with uncertainties) needs some special care.

The track representation remains the same as before: $x = (p_x, p_y, v_x, v_y, w, h)$, as is the form of $p(x_{k+1} | x_k)$.

However we now consider measurements to be *collections of pixel detections*, which are assumed to be independent of other neighboring measurements.

Need to define:

$$p(\bar{z}_k = z_k \,|\, \bar{x}_k = x_k)$$

$$p(\bar{z}_k = z_k | \bar{x}_k = \emptyset)$$





Probability of True Positive

Probability of False Positive

Object Tracking from Cameras Probability of True Positive



$$d = \min_{a,b} ||a - b|| \qquad B_a :=$$

$$s \cdot t \cdot a \in B_a$$

$$b \in B_b \qquad B_b :=$$



$$\left(1 - p_{fp} - (1 - p_{fp})p_{tp} \ e^{-(\frac{d}{\alpha})^2}\right) + \frac{u_{k,i,j}}{2}$$

- Box defined by track center, width, height
- Box defined by pixel center, width, height

Object Tracking from Cameras Probability of False Positive

Probability of False Positive:





 $p(z_{k,i,j} = 1 | \bar{x}_k = \emptyset) = u_{k,i,j}(1 - p_{fp}) + \frac{u_{k,i,j}}{2}$



Object Tracking from Cameras Tracking Overview

- 1. Cluster network output pixels in to groups
- For each cluster, assign to an existing track (using M-distance) or birth new track 2.
- 3. For each track, compute prediction distributions
- 4. For each track, sample particles from predicted distribution
- 5. For each particle $p_{k,l}$, compute weights $= p(\bar{z}_k | \bar{x}_k = p_{k,l}) = \prod_{m=1}^M p(\bar{z}_{k,m} | \bar{x}_k = p_{k,l})$





6. Fit distribution to particles based on weights to normalize. Compute POE for track, and kill if needed

